

# Visualization and Animations in Mathematics Using PostScript and PDF

Prof. dr Miroslav Ćirić

University of Niš

Faculty of Sciences and Mathematics

## Introduction

**This lecture is a continuation of the talks given at**

- Workshop on Innovations in Teaching of Computer Science Courses, Niš, October, 2003;**
- Workshop on Teaching Methods in Computer Science Courses, Skopje, October, 2003;**
- Symposium on Innovation of Computer Science Curriculum in Higher Education: Retraining of Young teaching staff, Athens, February, 2004;**

- Seminar for Elementary and Secondary School Teachers in Mathematics and Informatics, January, 2004;
- Tempus Workshop on New Methods in Teaching of Mathematics, Novi Sad, October, 2004;

Also, it is partially based on a course for teachers and teaching assistants on our Department of Mathematics and Informatics, February-March, 2004.

The main goal of this lecture is to demonstrate the most important capabilities of  $\text{T}_{\text{E}}\text{X}$ , PostScript (i.e.  $\text{PSTricks}$ ) and PDF, when they work together.

A question that we meet very often in our work is

- ➡ How to prepare a nice looking presentation to be presented to our students or on a scientific conference?

This problem is especially difficult if the material that has to be presented contains a lot of mathematical symbols and complex mathematical formulas, as well as a lot of graphics.

As we know, the best system for typesetting such material is  $\text{T}_{\text{E}}\text{X}$ .

But, what is about graphics?

## Remarks on Graphics in T<sub>E</sub>X

- T<sub>E</sub>X is a system (program) for typesetting and text processing, intentionally designed for typesetting of material with a lot of mathematical symbols and complex mathematical formulas.
- T<sub>E</sub>X probably has the best algorithm for formatting paragraphs and building pages from them.
- To a very large extent, T<sub>E</sub>X was designed for the placement of characters on a page.
- It was implicitly assumed that the characters are alphabetic or mathematical.

- But,  $\text{T}_{\text{E}}\text{X}$  is not conceived to be a tool for working with graphics.
- Donald Knuth ( $\text{T}_{\text{E}}\text{X}$ 's creator) himself noted that
  - “If you enjoy fooling around making pictures, instead of typesetting ordinary text,  $\text{T}_{\text{E}}\text{X}$  will be a source of endless frustration/amusement for you, because almost anything is possible...”
- However, there are many ways in which graphics may be made part of  $\text{T}_{\text{E}}\text{X}$  documents.
- Generally speaking,  $\text{T}_{\text{E}}\text{X}$  offers two major facilities for integrating graphics and  $\text{T}_{\text{E}}\text{X}$ :
  - ⇒ using the **font interface**,
  - ⇒ involving the **`\special`** command.

## The Font Interface

- This approach is based on use of special fonts to build pictures.
- That can be done in various ways:
  - ⇒ Through simple font elements (that is, straight line segments, or curves) which can be assembled to give (fairly simple) pictures.
  - ⇒ Through METAFONT – a programming language used to typeset outline fonts. Here, METAFONT is used to create a single character which is our graphics (or whatever), etc.
- One of the best known examples of this approach is the  $\text{\LaTeX}$  `picture` environment.

- **Good sides of this approach are generality and portability.**
- **Seeing that everything is in  $\text{T}\text{E}\text{X}$ , we can also ensure that the relative weights of lines, the font sizes, the symbols, blend in well with the rest of the document.**
- **The key drawbacks of the special font approach are centered around the limited fonts which are available, both in the slope of lines and their thicknesses, and the limited range of curves.**



## The Special Command

- Donald Knuth, T<sub>E</sub>X's creator, provided the `\special` command as a hook for implementing “features” that are not available in the basic language.
- This command does not affect the output page being formatted, but T<sub>E</sub>X put the material, specified as an argument in the `\special` command, literally at the current point in the `.dvi` file.
- The dvi-driver has to interpret the received information and produce the output accordingly.

- The `\special` command allows us to access special features of a driver program that translates the `.dvi` output of  $\text{T}\text{E}\text{X}$  in the language understood by the output device.
- If this driver has mechanisms to include external graphics, then we can import such graphics.
- The price we pay is non-portability, since our source will contain calls to a non-standard interface.
- Authors of different drivers have implemented different conventions so that documents that contain direct calls to `\special` only work with a very restricted setup.
- However, the non-portability problem can often be solved translating the `.dvi` output into **PostScript**.

## Remarks on PostScript

- **PostScript is a programming language introduced by Adobe in 1985 and first appeared in the Apple LaserWriter.**
- **The main purpose of PostScript was to provide a convenient language in which to represent the printed page in a device independent manner.**
- **This device independence means that the image is described without reference to any specific device features (e.g. printer resolution) so that the same description could be used on any PostScript printer without modification.**

- PostScript is a page description language which describes a complete page at a time, rather than one line at a time, like a line printer.
- It is a high-level programming language, which is stack-oriented and uses “reverse Polish” or postfix notation.
- PostScript is a flexible language
  - ⇒ it includes looping constructs, procedures, and comparison operators,
  - ⇒ it supports many data types, including reals, Booleans, arrays, and strings,
  - ⇒ and complex objects, such as dictionaries.

- **Functions that do not exist, but which would be useful for an application, can be defined and then used like other PostScript operators.**
- **Thus, PostScript is not a fixed tool within whose limits an application must be written, but is an environment that can be changed to match the task at hand.**
- **PostScript has a large selection of graphics operators that allow it to precisely describe a desired page.**

- These operators control the placement of three types of graphics objects:
  - ⇒ **Text** in a wide variety of typefaces can be placed on a page in any position, orientation, and scale.
  - ⇒ **Geometric figures** can be constructed using PostScript graphics operators. These describe the locations of straight lines and curves of any size, orientation, and width, as well as filled spaces of any size, shape, and color.
  - ⇒ **Sampled images** of digitized photographs, free-hand sketches, or any other image may be placed on a page in any scale or orientation.
- All graphic objects may be easily rotated, scaled, and clipped to a specified portion of the output page.

## Integration of PostScript and T<sub>E</sub>X

- When a PostScript output device and a dvi-to-ps driver are used to print or display T<sub>E</sub>X files, T<sub>E</sub>X and PostScript work together, as a preprocessor and a postprocessor, respectively.
- The role of PostScript may simply be to render T<sub>E</sub>X's dvi typesetting instructions.
- However, the full power of PostScript can be accessed through `\special's` and through features, such as font handling, built into the dvi-to-ps driver.

- One can divide the PostScript enhancements to T<sub>E</sub>X into roughly four categories:
  - The use of PostScript fonts.
  - The inclusion of PostScript graphics files.
  - The coloring of text and rules.
  - Everything else.
- Most T<sub>E</sub>X-PS users are familiar with the first three categories.
- The most powerful tool for covering the fourth category is the **PSTricks** macro package.



## Remarks on PSTricks

- The **PSTricks** package started as an implementation of some special features in the **Seminar** document style/class, which is for making slides with  $\text{\LaTeX}2_{\epsilon}$ .
- It was created by Timothy Van Zandt (Princeton, USA) in 1994, and further developed by him and Denis Girou (Orsay, France).
- However, it has grown into much more.
- Some of its current features are:
  - ⇒ Graphics objects (analogous to  $\text{\LaTeX}$  picture commands such as `\line` and `\frame`), including lines, polygons, circles, ellipses, curves, springs and zigzags.

- ⇒ Other drawing tools, such as a picture environment, various commands for positioning text, and macros for grids and axes.
- ⇒ Commands for rotating, scaling and tilting text, and 3-D projections.
- ⇒ Text framing and clipping commands.
- ⇒ Nodes and node connection and label commands, which are useful for trees, graphs, and commutative diagrams, among other applications.
- ⇒ Overlays, for making slides.
- ⇒ Commands for typesetting text along a path.
- ⇒ Commands for stroking and filling character outlines.
- ⇒ Plotting macros, etc.

- A goal of PSTricks was to be compatible with any  $\text{T}\text{E}\text{X}$  format and any dvi-to-ps driver.
- Compatibility with the various  $\text{T}\text{E}\text{X}$  formats is not difficult to achieve, because PSTricks does not deal with page layout, floats or sectioning commands.
- However, compatibility with all dvi-to-ps drivers is an unattainable goal because some drivers do not provide the basic `\special` facilities required by PSTricks.
- But, all of PSTricks' features work with the most popular driver dvips, and most features work with most other drivers.

- PostScript language is used for performing complex computation within the printer engine, resulting in high quality, professionally looking printed documents.
- The same language can be also used for describing the screen output – the same code that is drawing to the screen can be used to draw to the printer without any translation.
- But, PostScript does not support multimedia, hyperlinks and some other things.
- In order to solve this problem, in the early 1990s Adobe Systems developed **PDF**.

## Remarks on PDF

- PDF is a simplified version of the PostScript language, aimed far more at high quality on-screen display, document exchange, and hypertextual applications, than at printing quality.
- It has a very efficient font-embedding/replacement system to allow fonts to travel with the documents.
- It possesses a structured storage system to bundle these elements into a single file, with data compression where appropriate.
- A PDF document is usually more compact than the equivalent PostScript document, and has better defined structure.

- In addition to that, PDF is extended to enable to
  - ☞ use of intra- and inter-document hyperlinks
  - ☞ various dynamic effects for page transitions
  - ☞ working with forms
  - ☞ calling external applications, sound and video
  - ☞ embedding JavaScript programs into a PDF document
  - ☞ and many other things
- This extension is known as **pdfmark**.

- The **pdfmark** operator is a PostScript extension which is only implemented in Acrobat Distiller (as opposed to PostScript printers).
- Using this operator, many non-layout-related features of a PDF file (that have no counterpart in PostScript) can be defined in the original document or in the corresponding PostScript code.
- When PostScript files containing pdfmarks are processed by Acrobat Distiller, the corresponding PDF is generated.

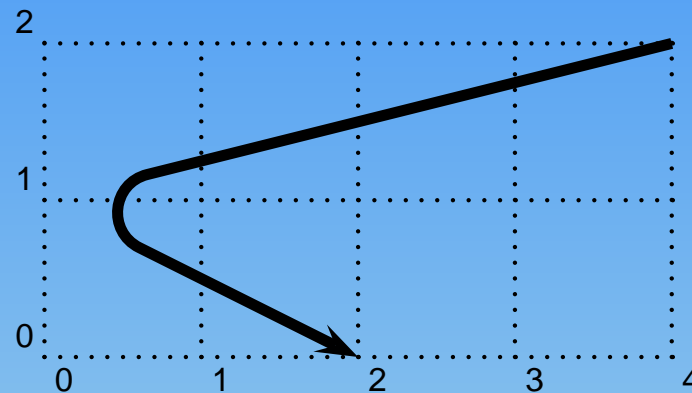
## Examples

- In this section we will give a number of examples demonstrating various capabilities of T<sub>E</sub>X, PostScript (PSTrics) and PDF.
- The examples are obtained in the following way:
  - ☞ they are written in T<sub>E</sub>X, using PSTrics macro package,
  - ☞ T<sub>E</sub>X's .dvi output is then converted to PostScript using the dvips driver, and
  - ☞ the PostScript file is converted to PDF using GhostScript.
- We have tried to select the most characteristic examples.



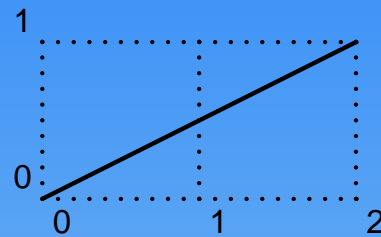
# Basic Graphics Objects

**An example of a line connecting 3 points  
(with a rounded corner)**



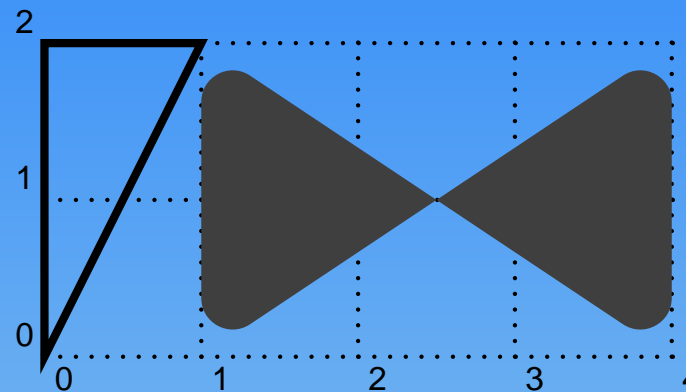
```
\psline[linewidth=2pt,linearc=.25]{->}(4,2)(0,1)(2,0)
```

An example of a simple line between two points



```
\qline(0,0)(2,1)
```

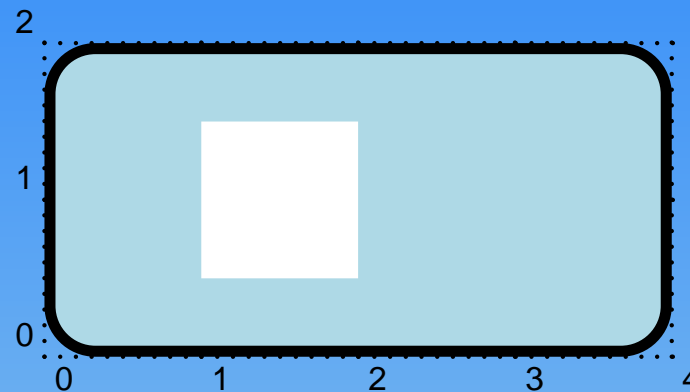
## Two simple examples of polygons



```
\pspolygon[linewidth=1.5pt](0,2)(1,2)
```

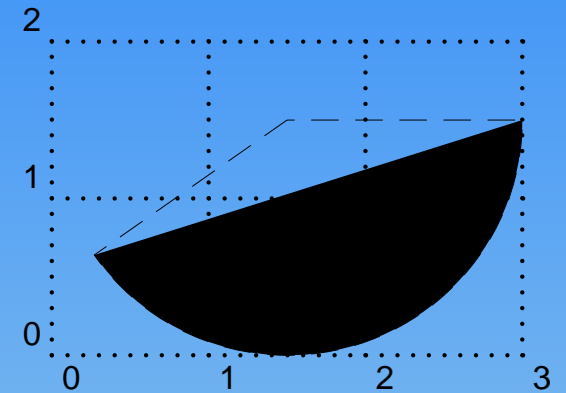
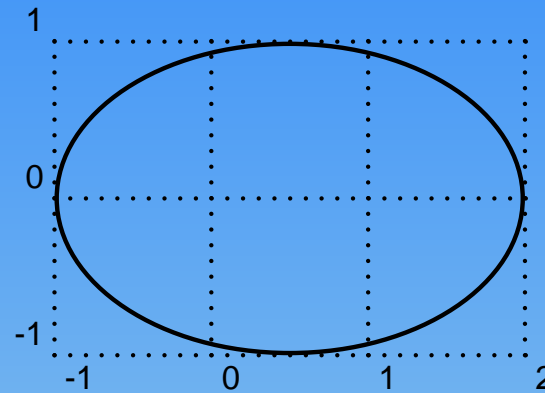
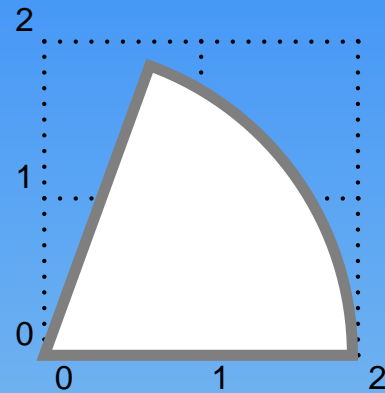
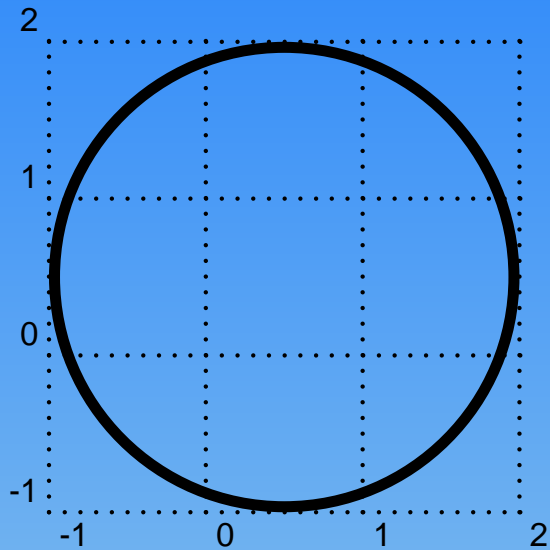
```
\pspolygon*[linearc=.2,linecolor=lightgray](1,0)(1,2)(4,0)(4,2)
```

## Two examples of frames



```
\psframe[linewidth=2pt,framearc=.3,fillstyle=solid,  
fillcolor=LightBlue](4,2)  
\psframe*[linecolor=white](1,.5)(2,1.5)
```

## Circle, Wedge, Ellipse and Arc



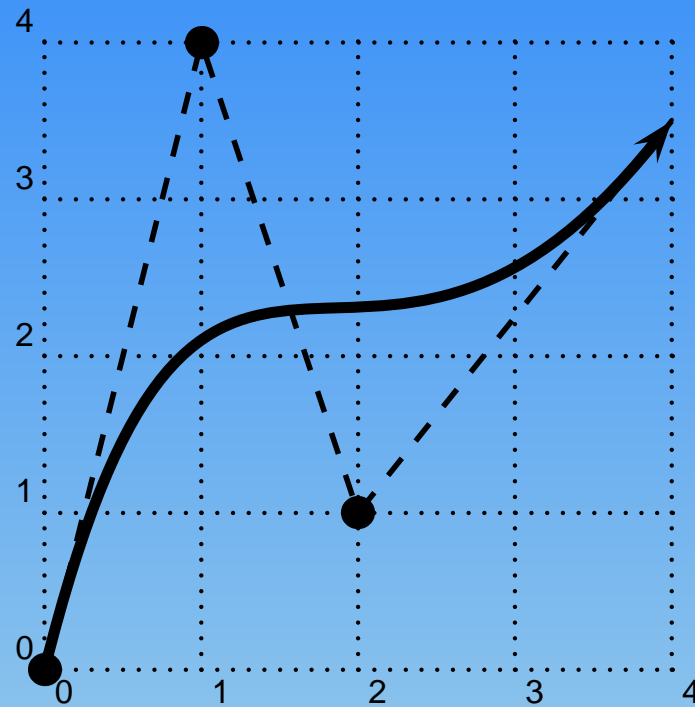
```
\pscircle[linewidth=2pt](.5,.5){1.5}
```

```
\pswedge[linecolor=gray,linewidth=2pt,fillstyle=solid]{2}{0}{70}
```

```
\psellipse[fillcolor=lightgray](.5,0)(1.5,1)
```

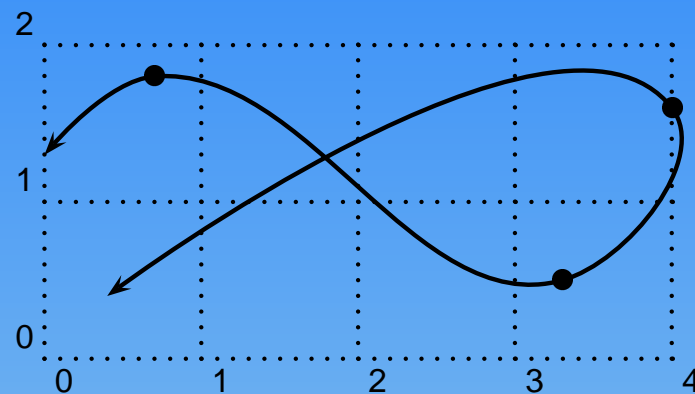
```
\psarc*[showpoints=true](1.5,1.5){1.5}{215}{0}
```

## An example of a Bezier curve



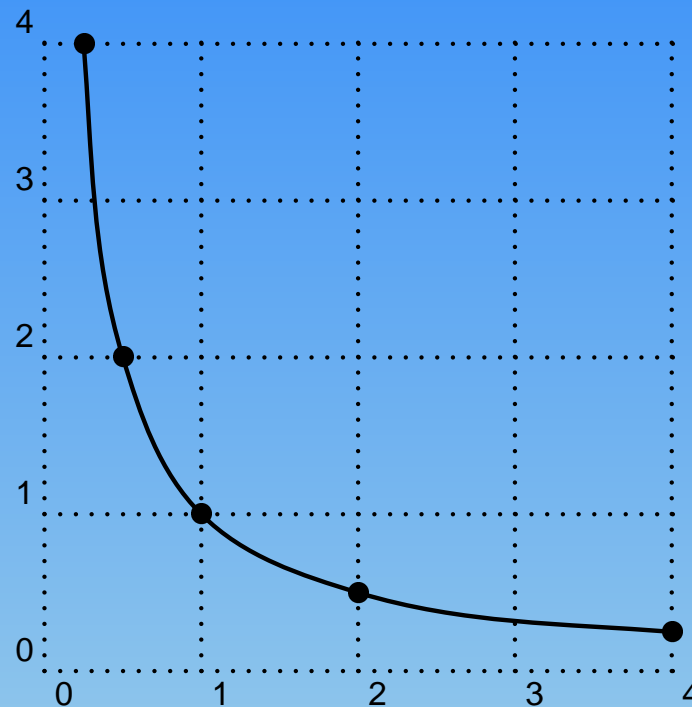
```
\psbezier[linewidth=2pt,showpoints=true]{->}(0,0)(1,4)(2,1)(4,3.5)
```

An example of an open curve interpolated through the points.



```
\pscurve[showpoints=true]{<->}(0,1.3)(0.7,1.8)(3.3,0.5)(4,1.6)(0.4,0.4)
```

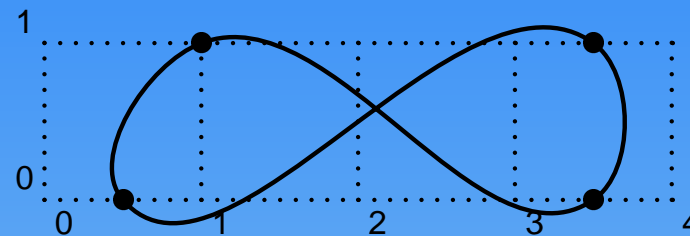
Like the previous example, but the curve is not extended to the first and last points



```
\psecurve[showpoints=true](.125,8)(.25,4)(.5,2)(1,1)(2,.5)(4,.25)(8,.125)
```

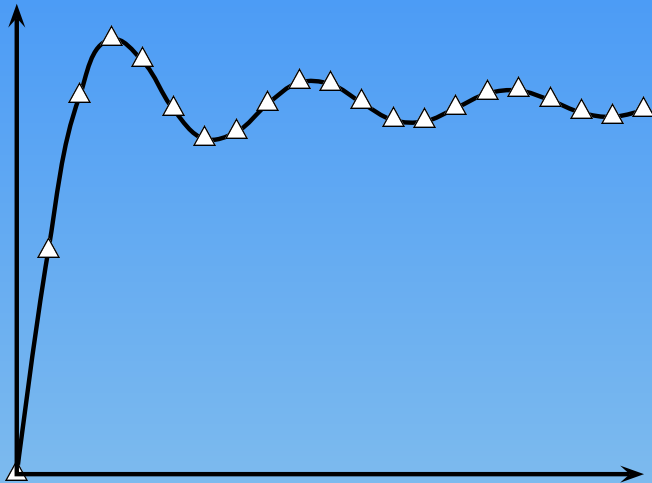


## A closed curve through the points



```
\psccurve[showpoints=true](.5,0)(3.5,1)(3.5,0)(1,1)
```

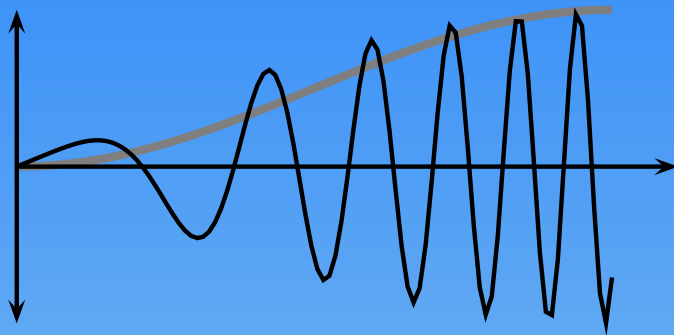
## Plots – plotting lists of data generated by other programs



```
\psset{xunit=.2cm,yunit=1.5cm}
\savedata{\mydata}[
  {{0,0}, {1.,0.946083}, {2.,1.60541}, {3.,1.84865},
  {4.,1.7582}, {5.,1.54993}, {6.,1.42469}, {7.,1.4546},
  {8.,1.57419}, {9.,1.66504}, {10.,1.65835}, {11.,1.57831},
  {12., 1.50497}, {13.,1.49936}, {14.,1.55621}, {15.,1.61819},
  {16.,1.6313}, {17.,1.59014}, {18.,1.53661}, {19.,1.51863},
  {20.,1.54824}}]
\dataplot[plotstyle=curve,showpoints=true,
  dotstyle=triangle]{\mydata}
\psline{<->}(0,2)(0,0)(20,0)
```

This is a plot of the function  $\text{Integral}(\sin(x))$ , and the data was generated by Mathematica

## Plots – plotting a function $f(x)$ (expressed in PostScript)

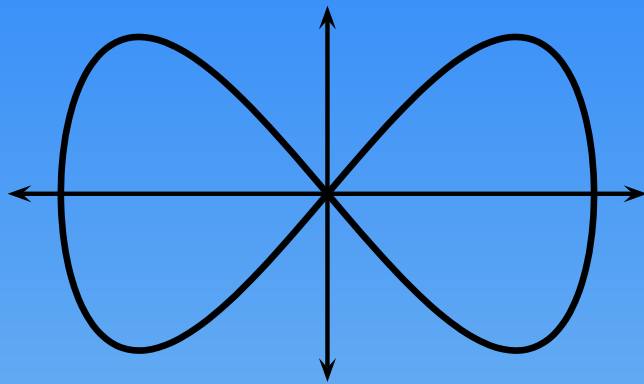


```
\psset{xunit=1.2pt}
\psplot[linecolor=gray,linewidth=1.5pt,plotstyle=curve]%
  {0}{90}{x sin dup mul}
\psplot[plotpoints=100]{0}{90}{x sin x 2 div 2 exp cos mul}
\psline{<->}(0,-1)(0,1)
\psline{->}(100,0)
```

These are the plots of the functions  $\sin^2 x$  and  $\sin x \cos\left(\left(\frac{x}{2}\right)^2\right)$

Note that PostScript is not designed for scientific computation, but it is good for graphing simple functions right from within  $\text{T}_{\text{E}}\text{X}$ .

## Parametric plots



```

\psset{xunit=1.2pt}
\psset{xunit=1.7cm}
\parametricplot[linewidth=1.2pt,plotstyle=ccurve]%
    {0}{360}{t sin t 2 mul sin}
\psline{<->}(0,-1.2)(0,1.2)
\psline{<->}(-1.2,0)(1.2,0)
    
```

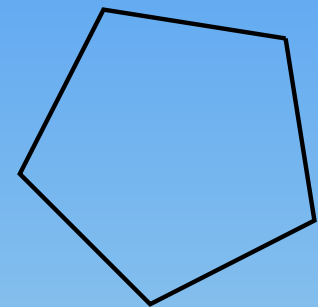
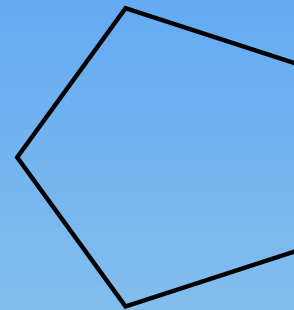
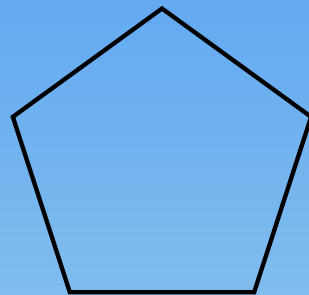
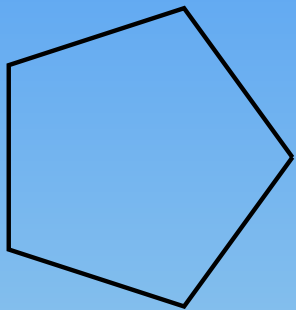
Here is a parametric plot of  $(\sin t; \sin 2t)$

## Complex Polygons

- A PSTricks package `pst-poly` allow to draw easily various kinds of regular or non regular polygons, using the unique macro `\PstPolygon`, with various customization parameters.
- It is also a good example of the great power and flexibility of PSTricks, as in fact it is a very short program (it body is only 100 lines long) but nevertheless really powerful.

**PolyRotation (real)** : rotation angle applied to the polygon  
(Default: 0 – no rotation).

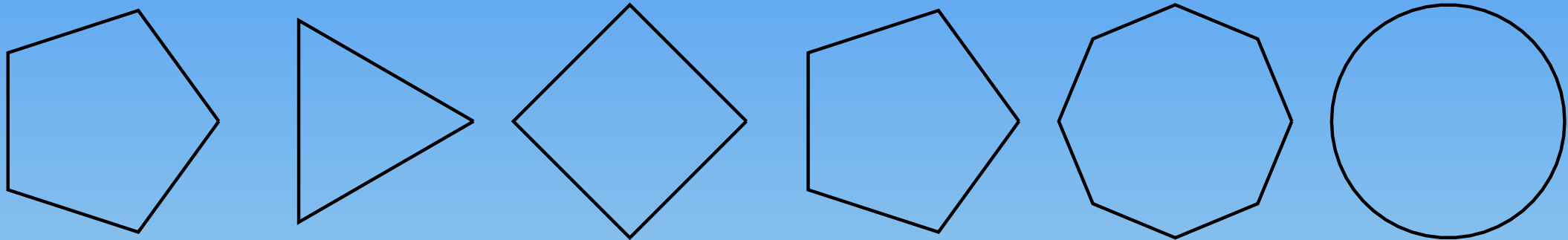
```
1 \PstPolygon \hfill  
2 \PstPolygon[PolyRotation=18] \hfill  
3 \PstPolygon[PolyRotation=36] \hfill  
4 \PstPolygon[PolyRotation=45]
```



**PolyNbSides (integer) : number of sides of the polygon (Default: 5).**

```

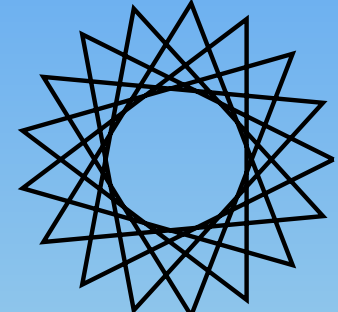
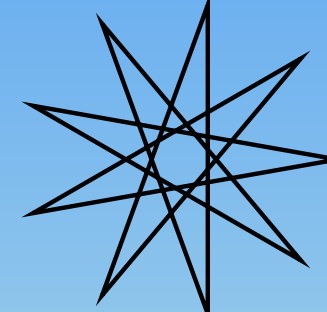
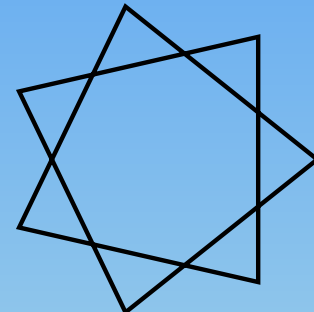
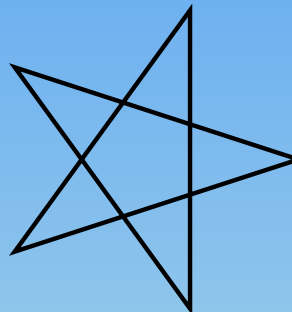
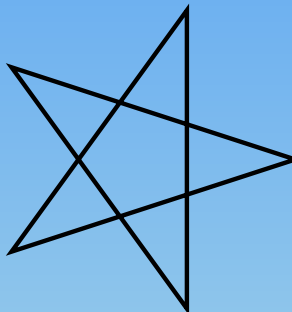
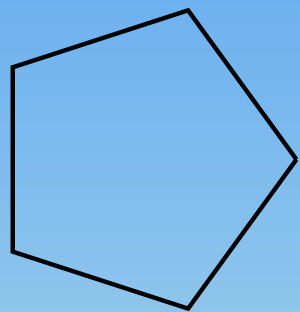
1 \PstPolygon \hfill
2 \PstPolygon[PolyNbSides=3] \hfill
3 \PstPolygon[PolyNbSides=4] \hfill
4 \PstPolygon[PolyNbSides=5] \hfill
5 \PstPolygon[PolyNbSides=8] \hfill
6 \PstPolygon[PolyNbSides=50]
    
```



**PolyOffset (integer)** : number of nodes to bypass to obtain each time the next one (Default: 1 — no node bypassed).

```

1 \PstPolygon \hfill
2 \PstPolygon[PolyOffset=2] \hfill
3 \PstPolygon[PolyOffset=3] \hfill
4 \PstPolygon[PolyNbSides=7,PolyOffset=2] \hfill
5 \PstPolygon[PolyNbSides=9,PolyOffset=4] \hfill
6 \PstPolygon[PolyNbSides=17,PolyOffset=6]
    
```

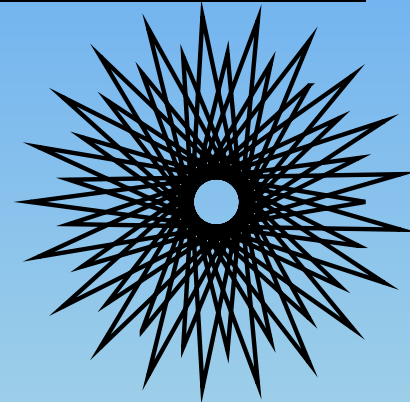
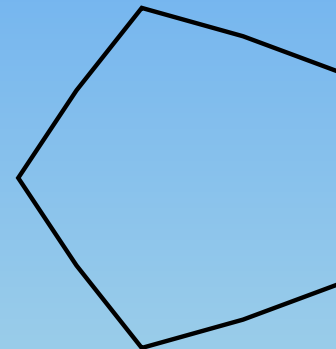
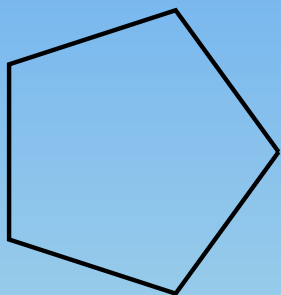




**PolyIntermediatePoint (real) : position of the intermediate point used to join each time the next node (Default: empty — not used).**

```

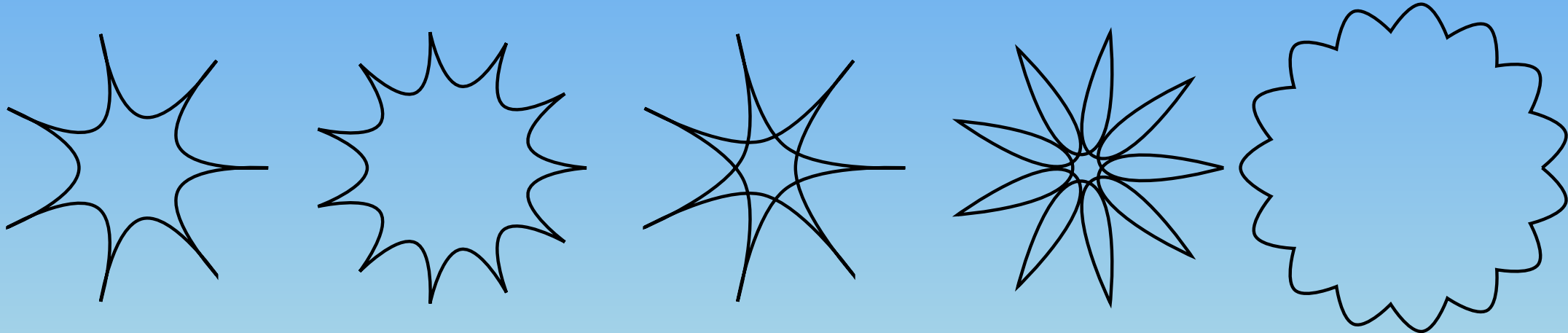
1 \PstPolygon \hfill
2 \PstPolygon[PolyIntermediatePoint=0.38] \hfill
3 \PstPolygon[PolyIntermediatePoint=0.2] \hfill
4 \PstPolygon[PolyIntermediatePoint=1.2] \hfill
5 \PstPolygon[PolyNbSides=7,PolyOffset=2,
6     PolyIntermediatePoint=0.38] \hfill
7 \PstPolygon[PolyNbSides=21,PolyOffset=2,
8     PolyIntermediatePoint=-1.25]
    
```



**PolyCurves (boolean)** : boolean value to choose between straight line and curve to join each time the next node  
**(Default: false – straight lines).**

```

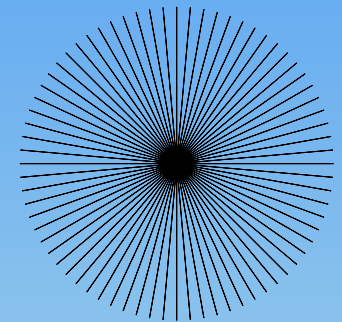
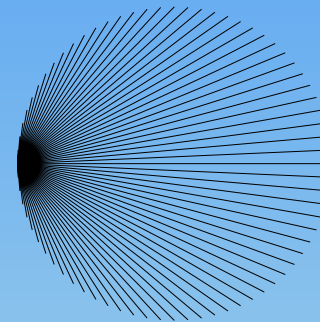
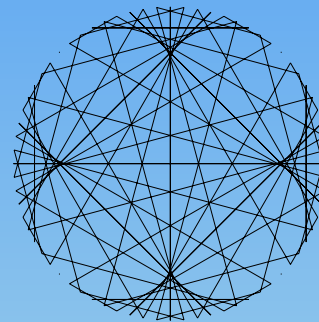
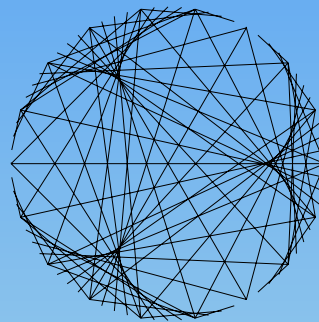
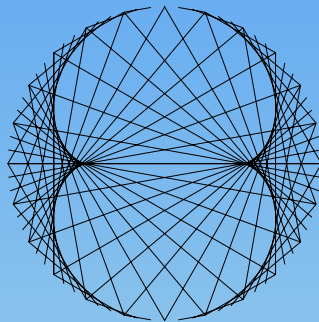
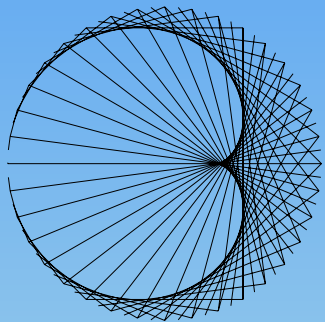
1 \psset{PolyCurves=true}
2 \PstPolygon[PolyNbSides=7,PolyIntermediatePoint=0.38] \hfill
3 \PstPolygon[PolyNbSides=11,PolyIntermediatePoint=0.6] \hfill
4 \PstPolygon[PolyNbSides=7,PolyIntermediatePoint=0.2,
5     PolyOffset=2] \hfill
6 \PstPolygon[PolyNbSides=9,PolyIntermediatePoint=0.1] \hfill
7 \PstPolygon[PolyNbSides=15,PolyIntermediatePoint=1.2]
    
```



**PolyEpicycloid (boolean)** : boolean value to choose between polygon and epicycloid (Default: false — polygon).

```

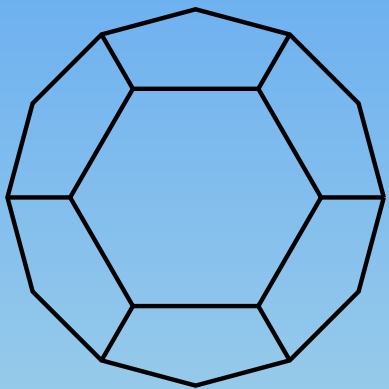
1 \psset{linewidth=0.001,PolyNbSides=72,PolyEpicycloid=true}
2 % Epicycloid of factor 1 is cardioid and of factor 2 nephroid
3 \multido{\i=2+1}{4}{\PstPolygon[PolyOffset=\i]\hfill}
4 \PstPolygon[PolyOffset=72]\hfill % Epicycloid of factor 71
5 \PstPolygon[PolyOffset=73]      % Epicycloid of factor 72
    
```



**PolyName (string)** : name of the polygon, useful to have different names for the nodes of different polygons (Default: empty — no name).

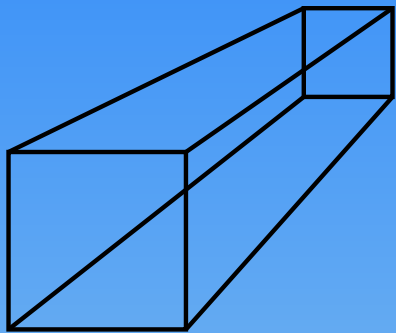
The center of the polygon has name PolyName0 and the nodes (vertices) have names PolyName1 to PolyNameN.

With this parameter, we can connect as we want nodes of different polygons:



```
1 \psset{PstPicture=false}
2 \begin{pspicture}(-1,-1)(1,1)
3   \PstPolygon[unit=0.8,PolyName=A,PolyNbSides=6]
4   \PstPolygon[unit=1.2,PolyName=B,PolyNbSides=12]
5 \end{pspicture}
6 \multido{\i=1+2}{6}{%
7   \ncline{A\the\multidocount}{B\i}}
```

It is also a way (limited in fact...) to define three dimensional objects in perspective:



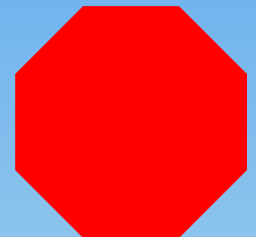
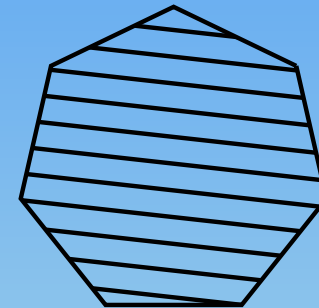
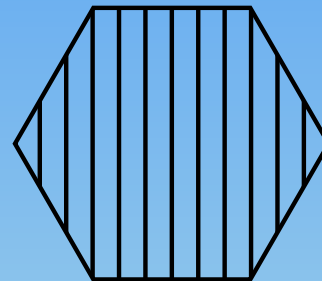
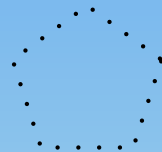
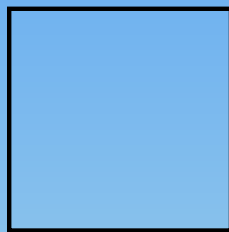
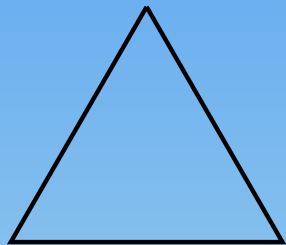
```

1 \psset{unit=0.8}
2 \begin{pspicture}(3,2.5)
3   % \PstSquare is described later
4   \rput[1b](0,0){\PstSquare[PolyName=A]}
5   \rput[1b](2.5,2){\PstSquare[unit=0.5,
6                       PolyName=B]}
7   \multido{\i=1+1}{4}{\ncline{A\i}{B\i}}
8 \end{pspicture}
    
```

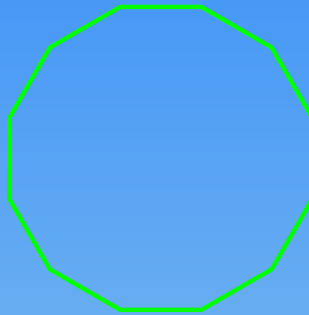
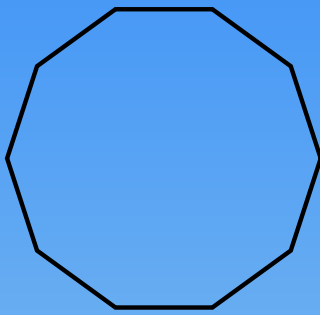
Some often used polygons and other related geometric objects are pre-defined, for immediate usage :

```

1  \PstTriangle \hfill
2  \PstSquare \hfill
3  \PstPentagon[unit=0.5,linestyle=dotted] \hfill
4  \PstHexagon[fillstyle=hlines,hatchangle=90] \hfill
5  \PstHeptagon[fillstyle=vlines] \hfill
6  \PstOctagon*[unit=0.8,linecolor=red]
    
```



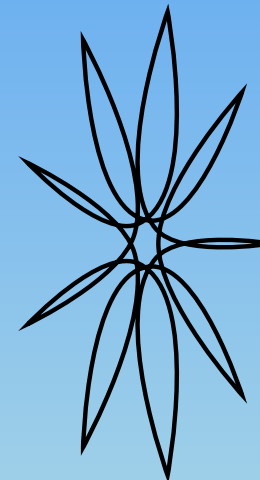
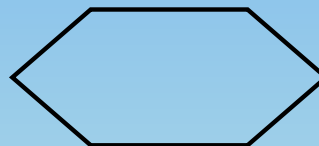
```
1 \PstNonagon[unit=0.5] \hfill  
2 \PstDecagon \hfill  
3 \PstDodecagon[linecolor=green] \hfill  
4 \PstStarFiveLines \hfill  
5 \PstStarFive
```



It is not so difficult to extend regular polygons to non regular ones, using a different value for horizontal and vertical units (nevertheless, the code is more tricky, as we must do all the trigonometry explicitly...)

```

1 \PstPentagon[xunit=0.5] \hskip5mm
2 \PstHexagon[yunit=0.5] \hskip5mm
3 \PstStarFive[xunit=0.5,yunit=1.5] \hskip5mm
4 \PstPolygon[xunit=0.8,yunit=1.5,PolyNbSides=9,PolyOffset=2,
5   PolyIntermediatePoint=0.1,PolyCurves=true]
    
```





## Text Trics

### Framed boxes

An example of a single framed box.

```
\psframebox[linewidth=1.5pt]{%  
  \parbox[c]{5cm}{\raggedright An example  
of a single framed box.}}
```

A double frame is drawn with the gap between lines equal to doublesep

```
\psdblframebox[linewidth=1.5pt]{%  
  \parbox[c]{5cm}{\raggedright A double frame  
is drawn with the gap between lines equal  
to {\tt doublesep}}}
```

## Shadowed and circled boxes



```
\psshadowbox{\bf Great Idea!!}
```



```
\pscirclebox{\begin{tabular}{c} You are \\ here \end{tabular}}
```

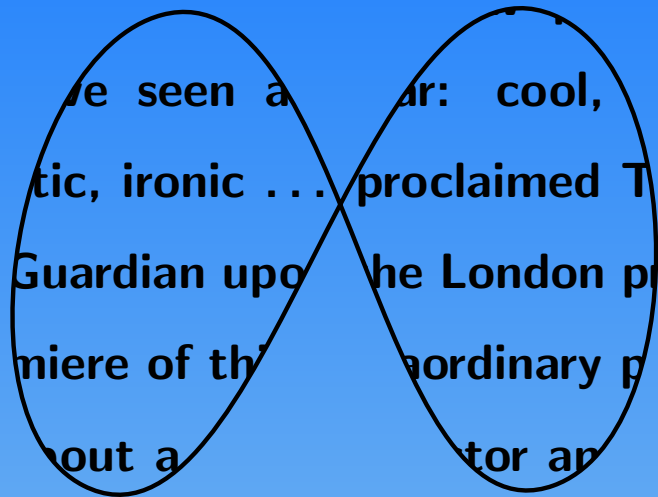
At the introductory price of **\$13.99**, it pays to act now!

At the introductory price of  
`\psovalbox[boxsep=false,linecolor=red]{\$13.99}`,  
 it pays to act now!

## Clipping

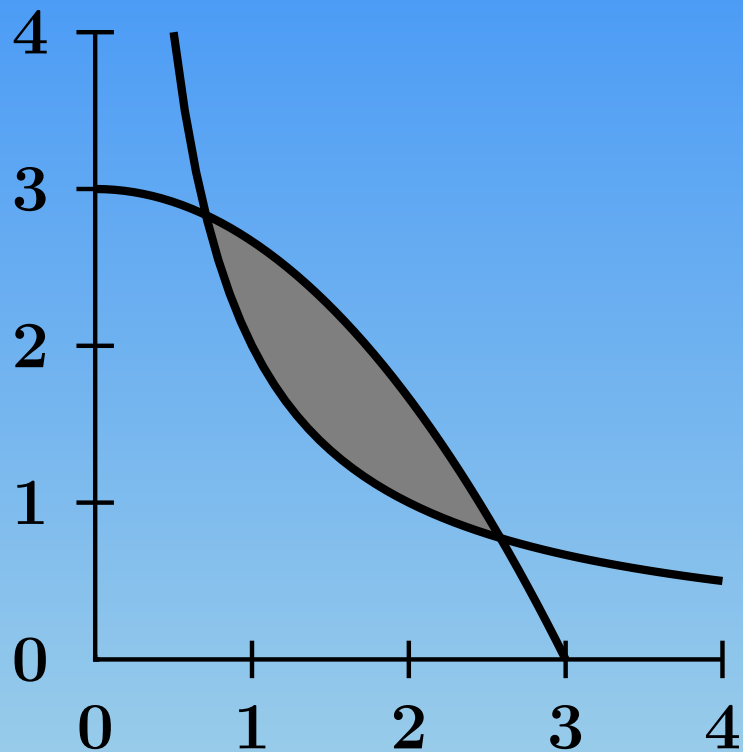
One of the best new plays I have seen all year: cool, poetic, ironic ... proclaimed *The Guardian* upon the London premiere of this extraordinary play about a Czech director and his actress wife, confronting exile in America.

```
\parbox{4.5cm}{%
  \psclip{\psccurve[linestyle=none](.5,-3)(3.5,0)
    (3.5,-3)(1,0)}
  One of the best new plays I have seen all year: cool,
  poetic, ironic \ldots proclaimed {\em The Guardian} upon
  the London premiere of this extraordinary play about a
  Czech director and his actress wife, confronting exile
  in America.
\endpsclip}
```



**The same with** `linestyle=solid`

## Clipping – shading the region between two curves:



```

\psclip{%
  \pscustom[linestyle=none]{%
    \psplot{.5}{4}{2 x div}
    \lineto(4,4)}
  \pscustom[linestyle=none]{%
    \psplot{0}{3}{3 x x mul 3 div sub}
    \lineto(0,0)}}
\psframe*[linecolor=gray](0,0)(4,4)
\endpsclip
\psplot[linewidth=1.5pt]{.5}{4}{2 x div}
\psplot[linewidth=1.5pt]{0}{3}{3 x x mul 3 div sub}
\psaxes(4,4)
    
```

## Rotation and scaling boxes

Left  
Down  
Right

```
\rotateleft{Left} \rotatedown{Down} \rotateright{Right}
```

Big and long

```
\scaleboxto(4,2){Big and long}
```

Question: How do Democrats organize a firing squad?

Answer: First they get in a circle, ...

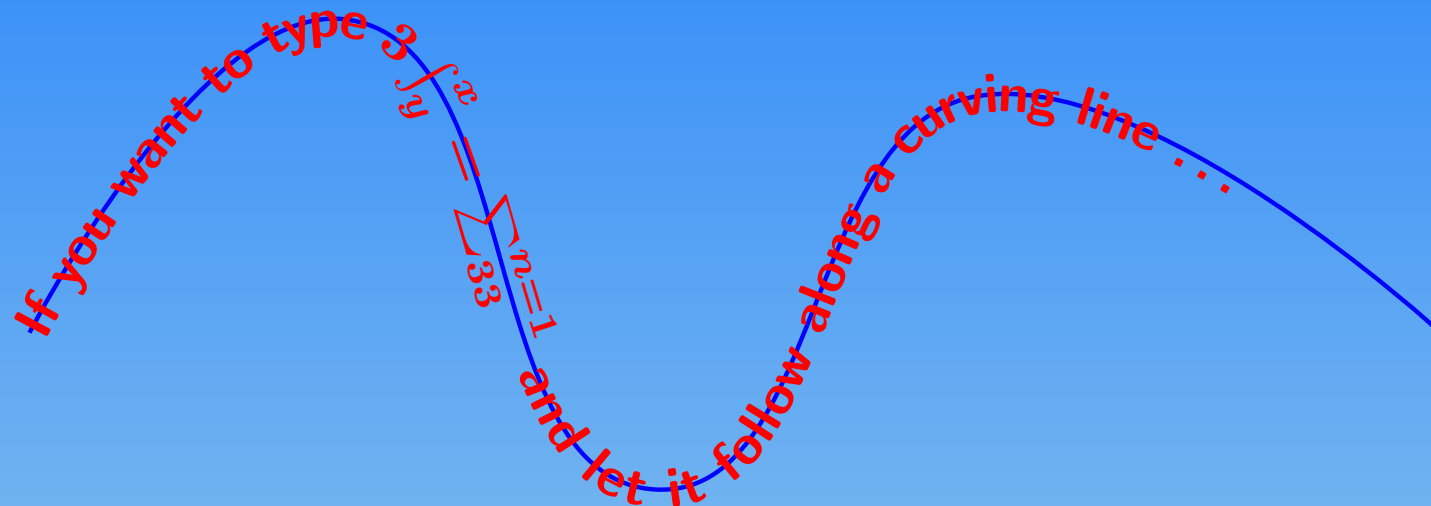
Question: How do Democrats organize a firing squad?

```
\begin{Rotatedown}
```

```
\parbox{\hsize}{Answer: First they get in a circle,  
\ldots\hss}%
```

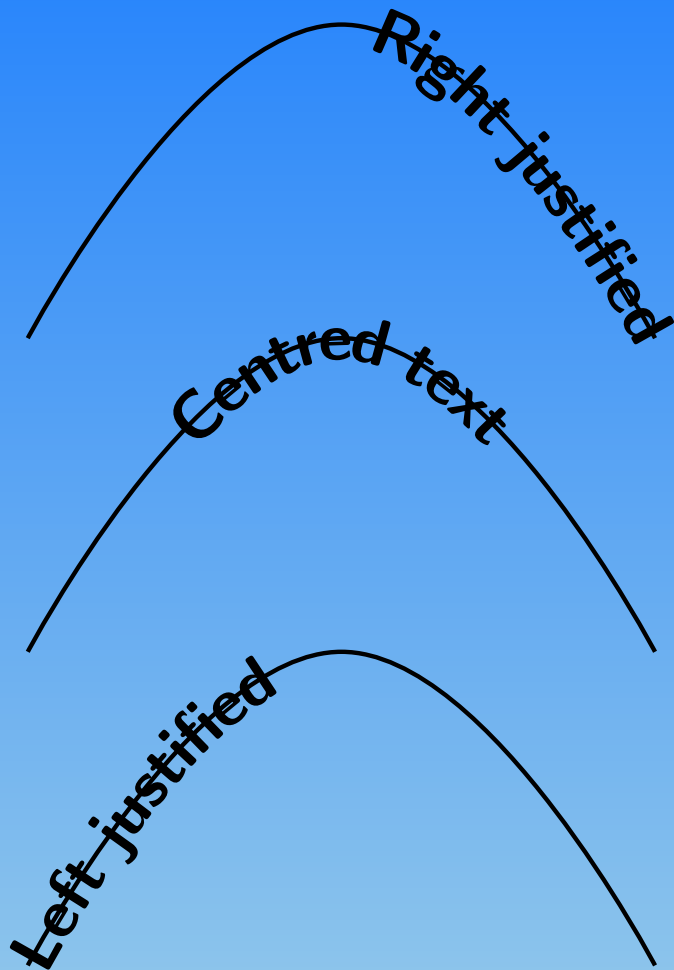
```
\end{Rotatedown}
```

## Writing Text Along a Path



```

1 \begin{pspicture}(-4,-3.2)(3,0.2)
2   \psset{linecolor=lightgray}
3   \pstextpath{\pscurve(-4,-2)(-2,0)(0,-3)(2,-1)(3,-2)}
4     {\color{red}
5       If you want to type $3 \int_x y = \sum_{n=1}^{33}$
6       and let it follow along a curving line \ldots}
7 \end{pspicture}
    
```



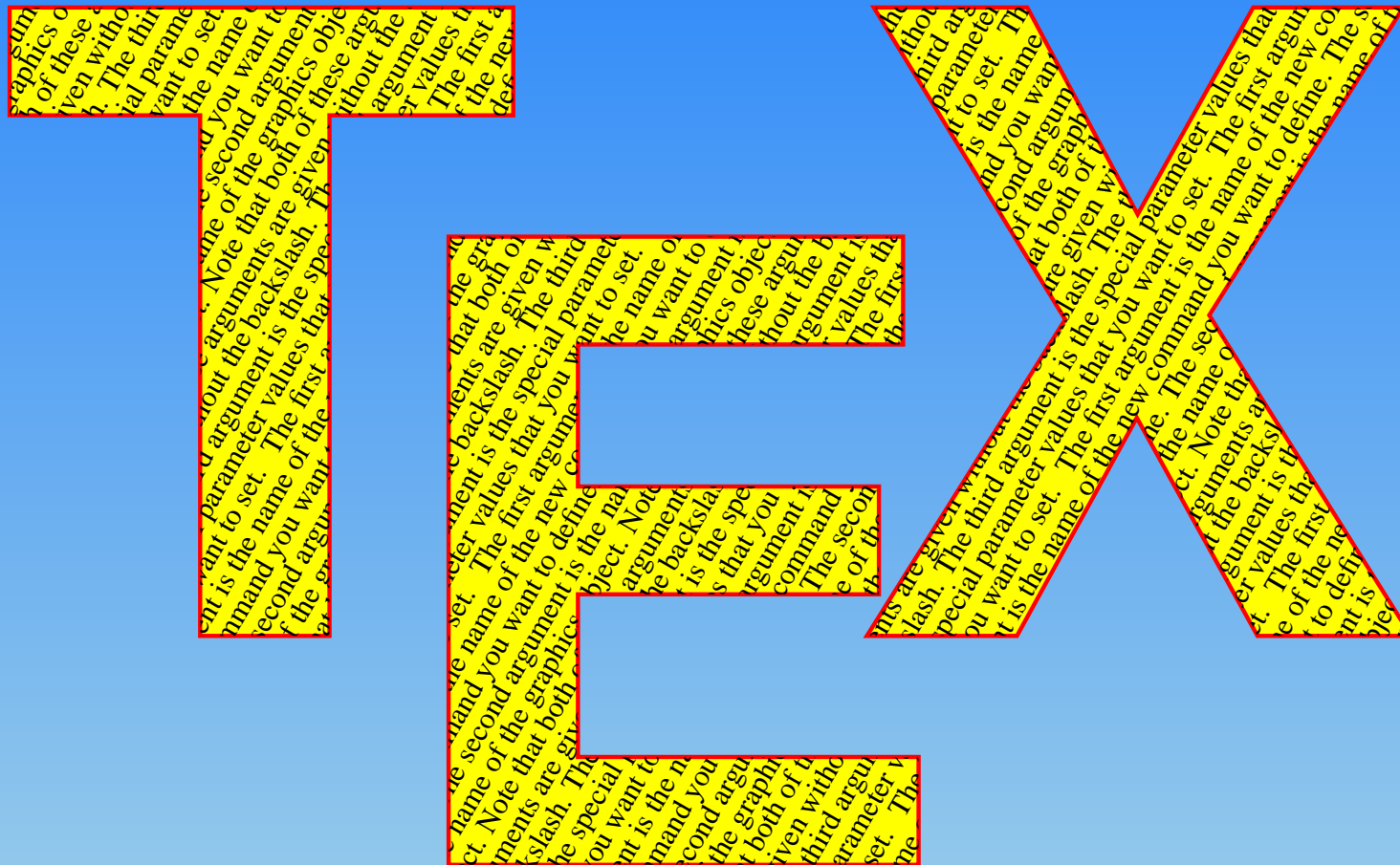
```

1  \begin{pspicture}(0,0)(4.2,6.2)
2    \pstextpath[l]{\pscurve(0,0)(2,2)(4,0)}%
3      {Left justified}
4    \pstextpath[c]{\pscurve(0,2)(2,4)(4,2)}%
5      {Centred text}
6    \pstextpath[r]{\pscurve(0,4)(2,6)(4,4)}%
7      {Right justified}
8  \end{pspicture}
    
```



## Filling Character Outline





## Nodes and Node Connections

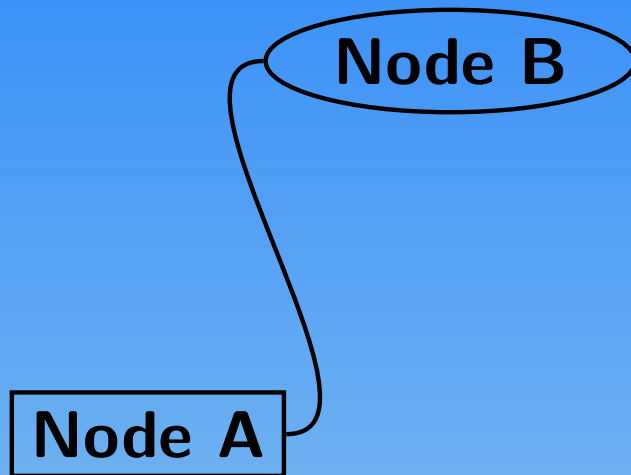
There are three components to the node macros:

**Node definitions:** The node definitions let you assign a name and shape to an object.

**Node connections:** The node connections connect two nodes, identified by their names.

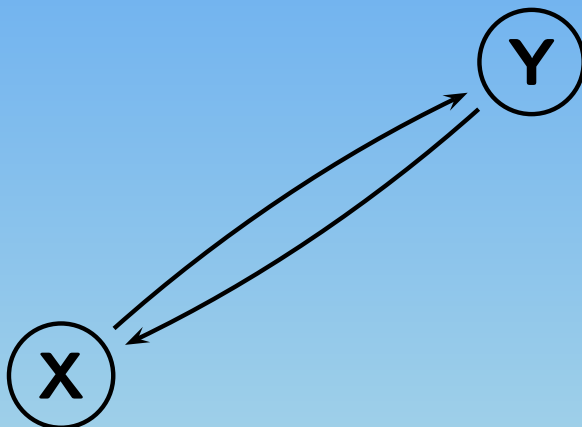
**Node labels:** The node label commands let you affix labels to the node connections.

## Node Connections

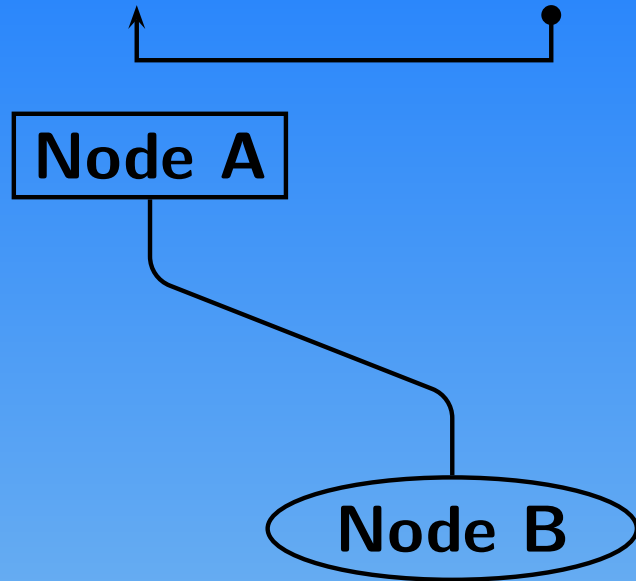


```
\rput [bl] (0,0){\rnode{A}{\psframebox{Node A}}}
\rput [tr] (4,3){\ovalnode{B}{Node B}}
\ncurve [angleB=180] {A}{B}
```

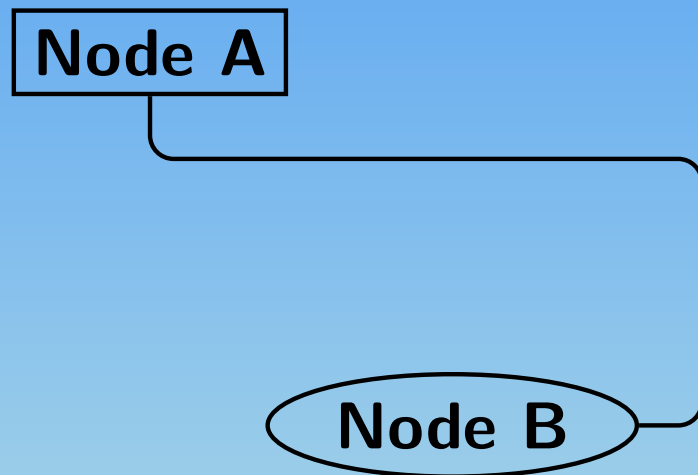
```
\cnodeput (0,0){A}{X}
\cnodeput (3,2){B}{Y}
\psset{nodesep=3pt}
\ncarc{->}{A}{B}
\ncarc{->}{B}{A}
```



Connect some words!

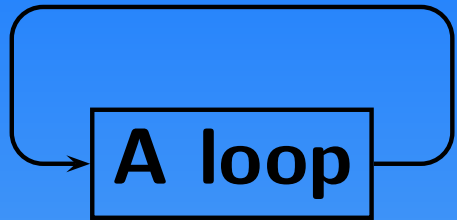


```
\rnode{A}{Connect} some \rnode{B}{words}!  
\ncbar[nodesep=3pt,angle=-90]{<-*}{A}{B}
```



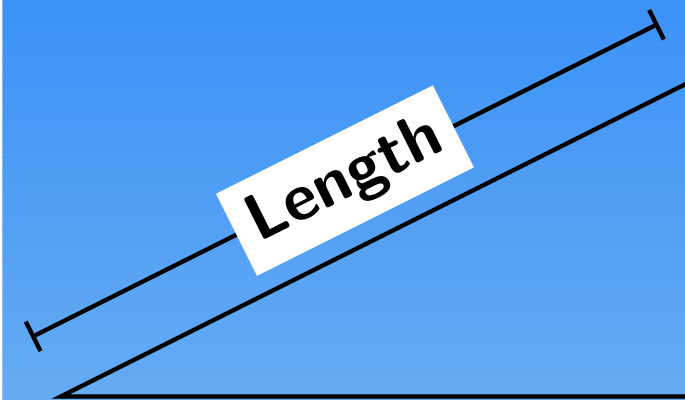
```
\rput[t1](0,3){\rnode{A}{\psframebox{Node A}}}  
\rput[br](4,0){\ovalnode{B}{Node B}}  
\ncdiag[angleA=-90,angleB=90,arm=.5,lineararc=.2]{A}{B}
```

```
\rput[t1](0,3){\rnode{A}{\psframebox{Node A}}}  
\rput[br](4,0){\ovalnode{B}{Node B}}  
\ncangles[angleA=-90,arm=.4cm,lineararc=.15]{A}{B}
```

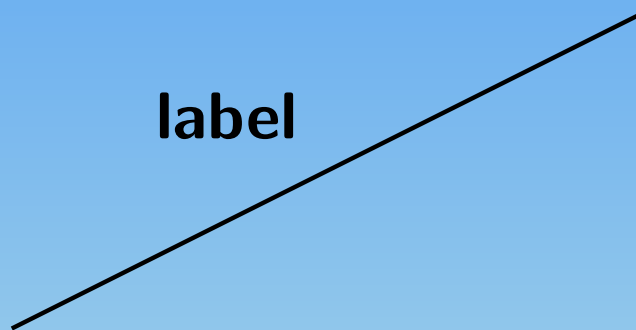


```
\rnode{a}{\psframebox{\Huge A loop}}  
\ncloop[angleB=180,loopsize=1,arm=.5,lineararc=.2]{->}{a}{a}
```

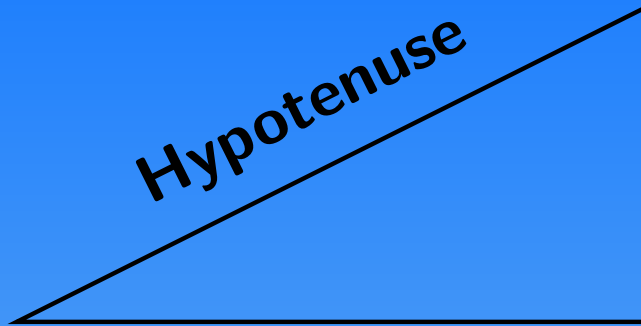
## Attaching Labels



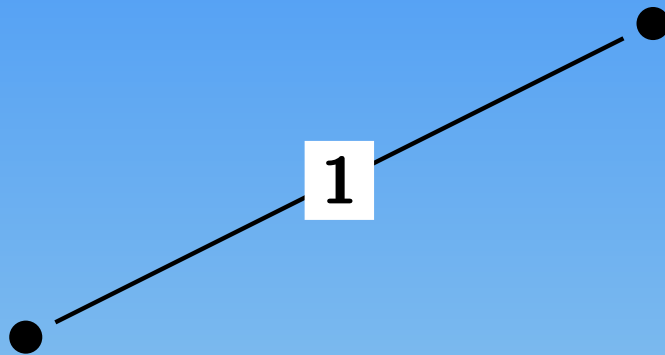
```
\pspolygon(0,0)(4,2)(4,0)
\pcline[offset=12pt]{|-|}(0,0)(4,2)
\lput*{:U}{Length}
```



```
\pcline(0,0)(4,2)
\lput{:U}{\rput[r]{N}(0,.4){label}}
```



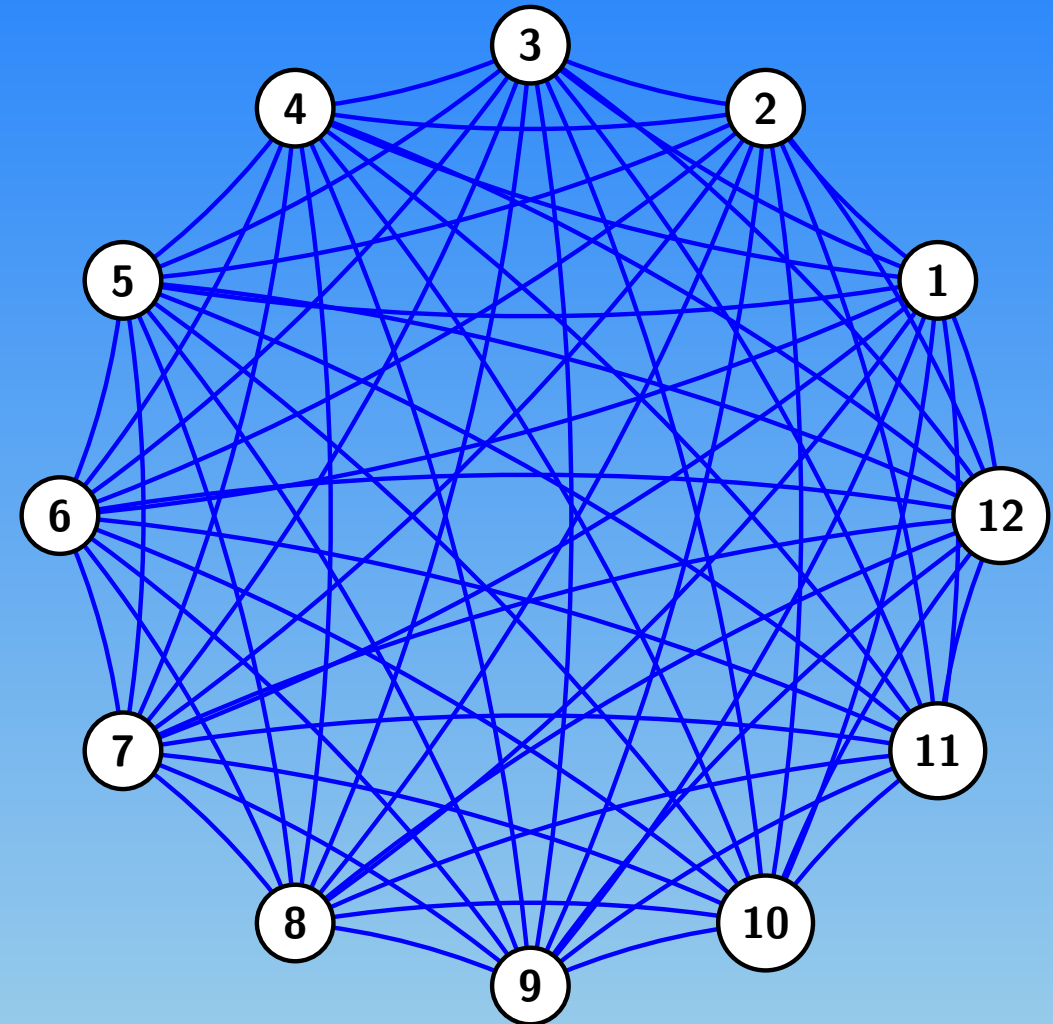
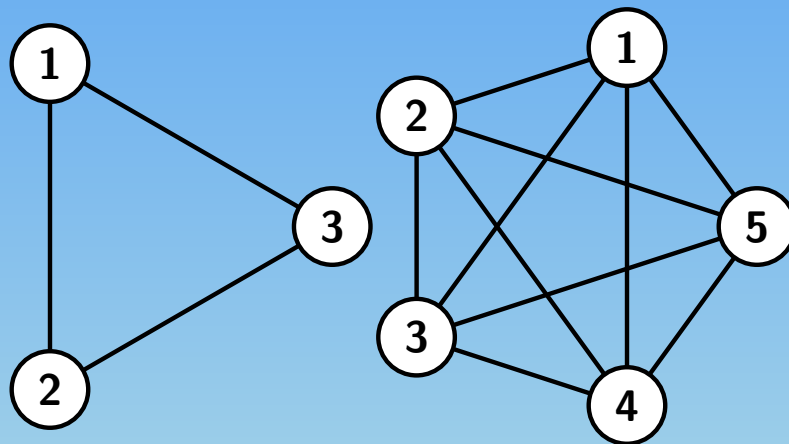
```
\pspolygon(0,0)(4,2)(4,0)
\pcline[linestyle=none](0,0)(4,2)
\aput{:U}{Hypotenuse}
```



```
\cnode*(0,0){3pt}{A}
\cnode*(4,2){3pt}{B}
\ncline[nodesep=3pt]{A}{B}
\mput*{1}
```



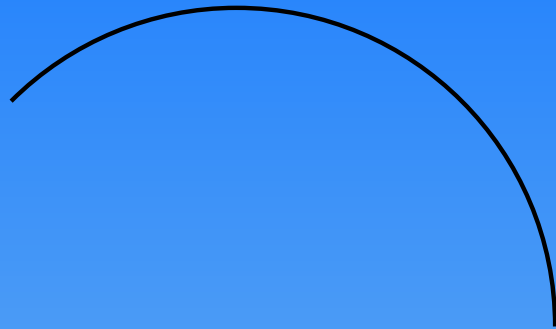
Nodes and node connections and labels are very useful in drawing graphs.



## Special Coordinates

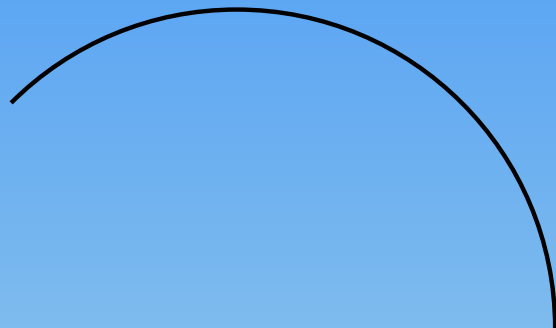
The command `\SpecialCoor` enables a special feature that lets us specify coordinates in a variety of ways, in addition to the usual **Cartesian coordinates**.

We can use **polar coordinates**, **relative coordinates** etc.



1

```
\psarc(0,0){.8in}{0}{(-1,1)}
```



1

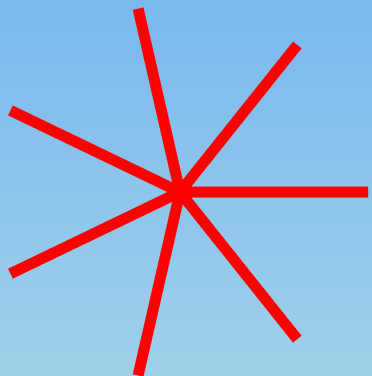
```
\SpecialCoor
```

2

```
\psarc(0,0){.8in}{0}{135}
```

Angles, in polar coordinates and other arguments, should be a number giving the angle in degrees, by default.

We can also change the units used for angles with the command `\degrees[num]`, where `num` should be the number of units in a circle.



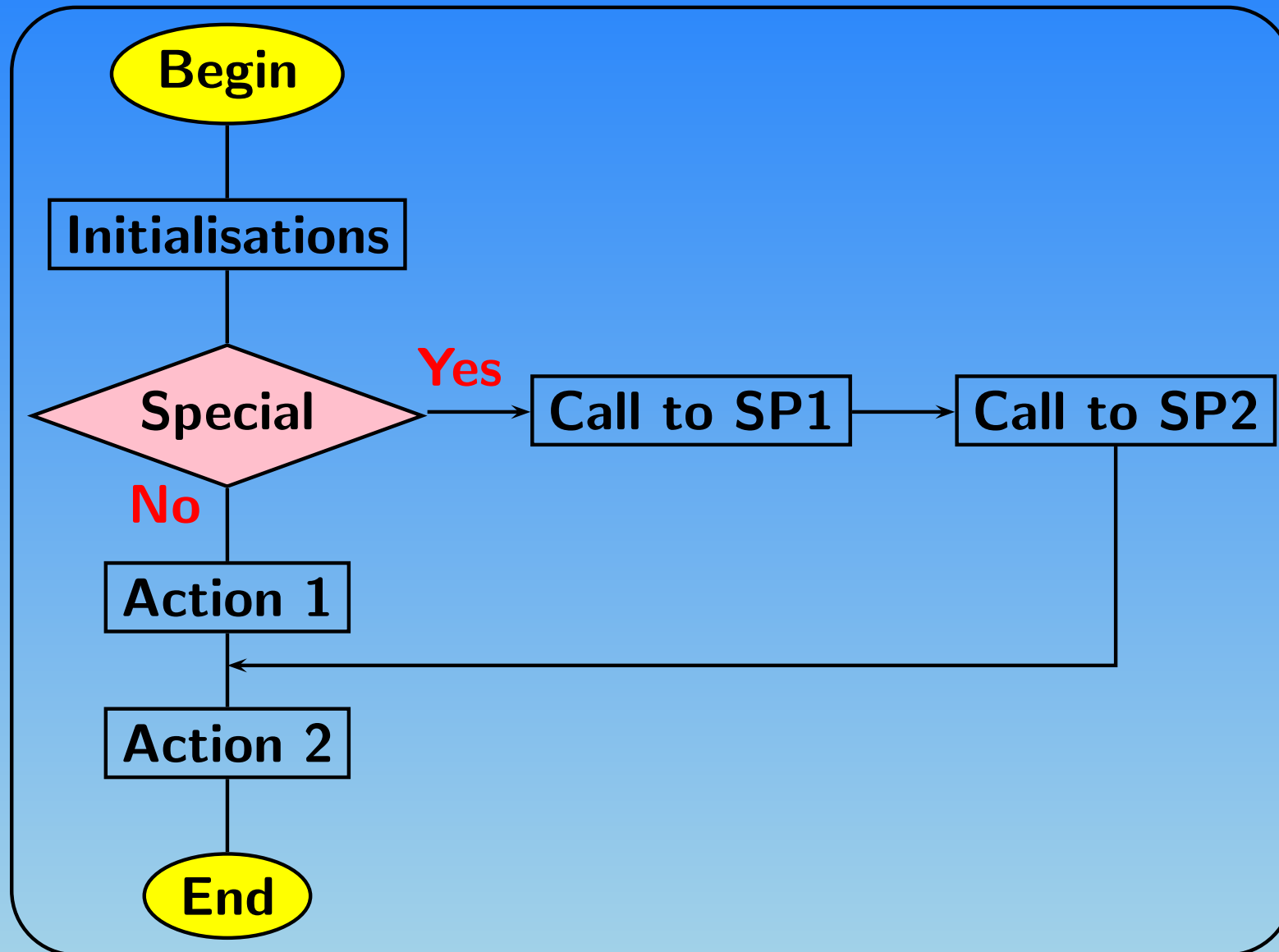
```
1 \pspicture(-1.2,-1.2)(1.2,1.2)
2 \psset{linewidth=2pt, linecolor=red}
3 \SpecialCoor
4   \degrees[70]
5   \psline(0,0)(1.2;0)
6   \psline(0,0)(1.2;10)
7   \psline(0,0)(1.2;20)
8   \psline(0,0)(1.2;30)
9   \psline(0,0)(1.2;40)
10  \psline(0,0)(1.2;50)
11  \psline(0,0)(1.2;60)
12 \NormalCoor
13 \endpspicture
```

## Overlays

- Overlays are mainly of interest for making slides, and the overlay macros described in this section are mainly of interest to T<sub>E</sub>X macro writers who want to implement overlays in a slide macro package.
- For example, the `seminar.sty` package, a L<sup>A</sup>T<sub>E</sub>X style for notes and slides, uses PStricks to implement overlays.
- Overlays are made by creating an `\hbox` and then outputting the box several times, printing different material in the box each time.

- We distinguish between two kinds of overlays:
  - ⇒ **Cumulative overlays** – with each new one added to the preceding.
  - ⇒ **Progressive overlays** – where the first slide is kept but each new one will replace the preceding.

## Flow diagram using nodes and node connections

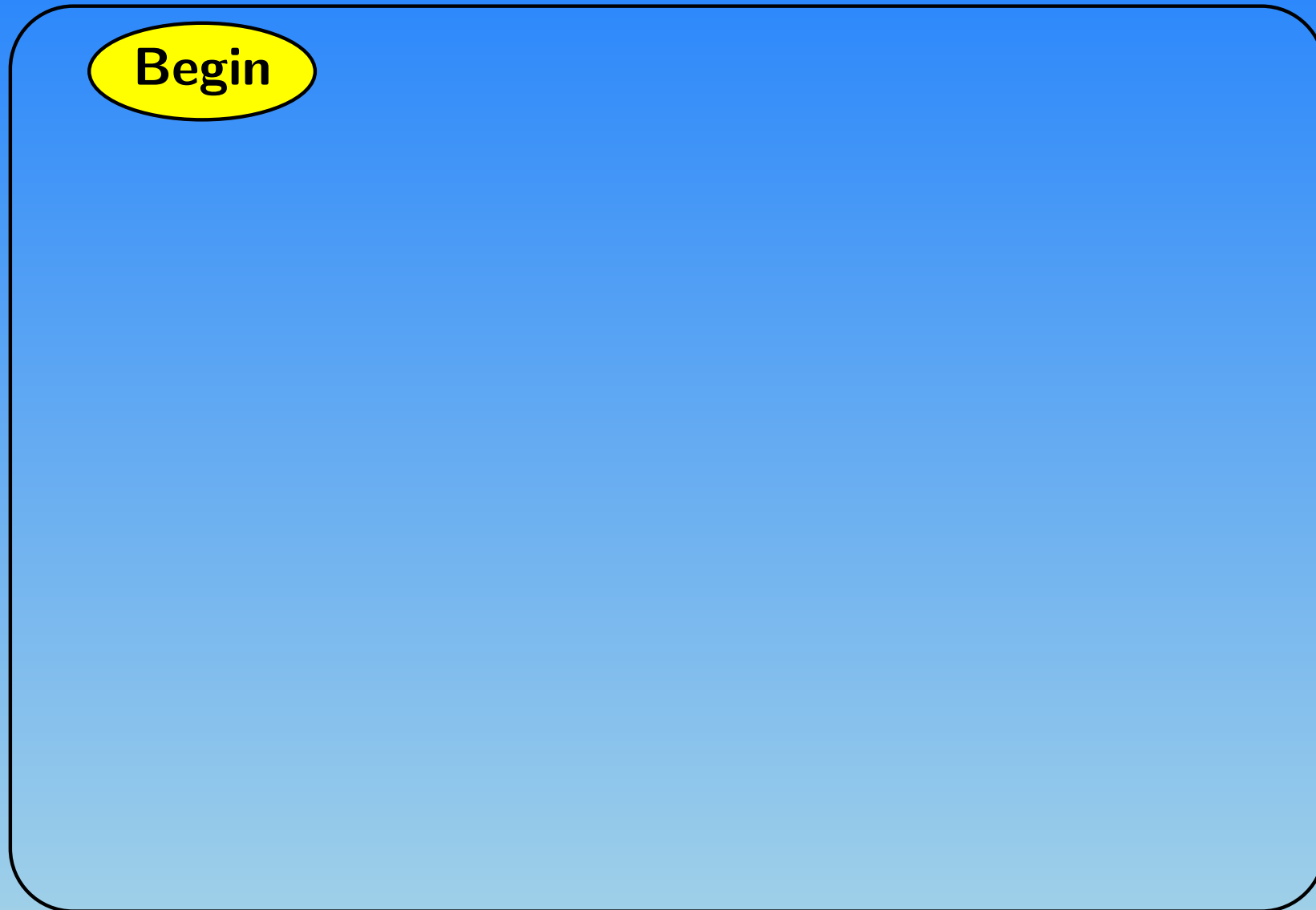


## The same diagram with overlays

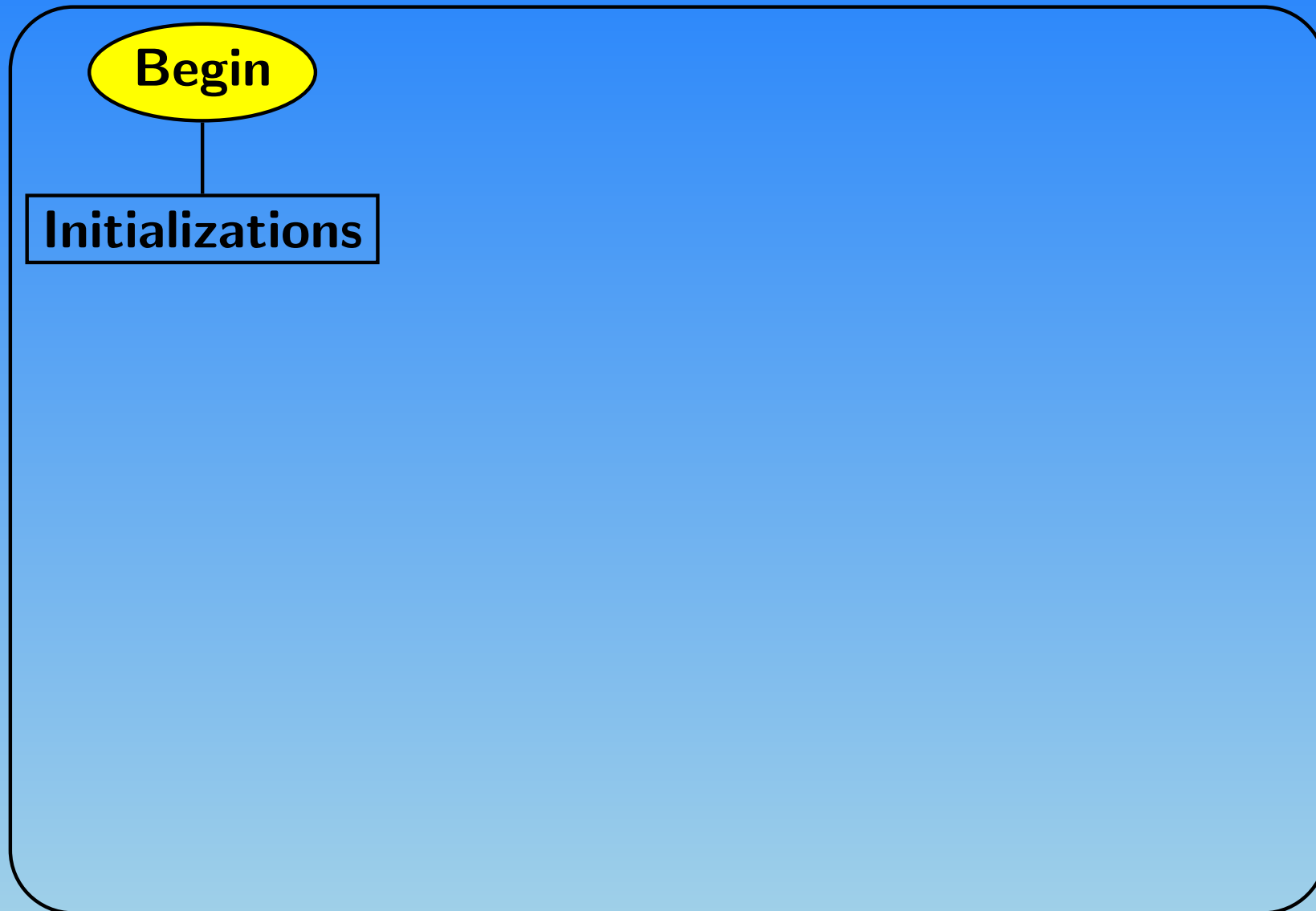




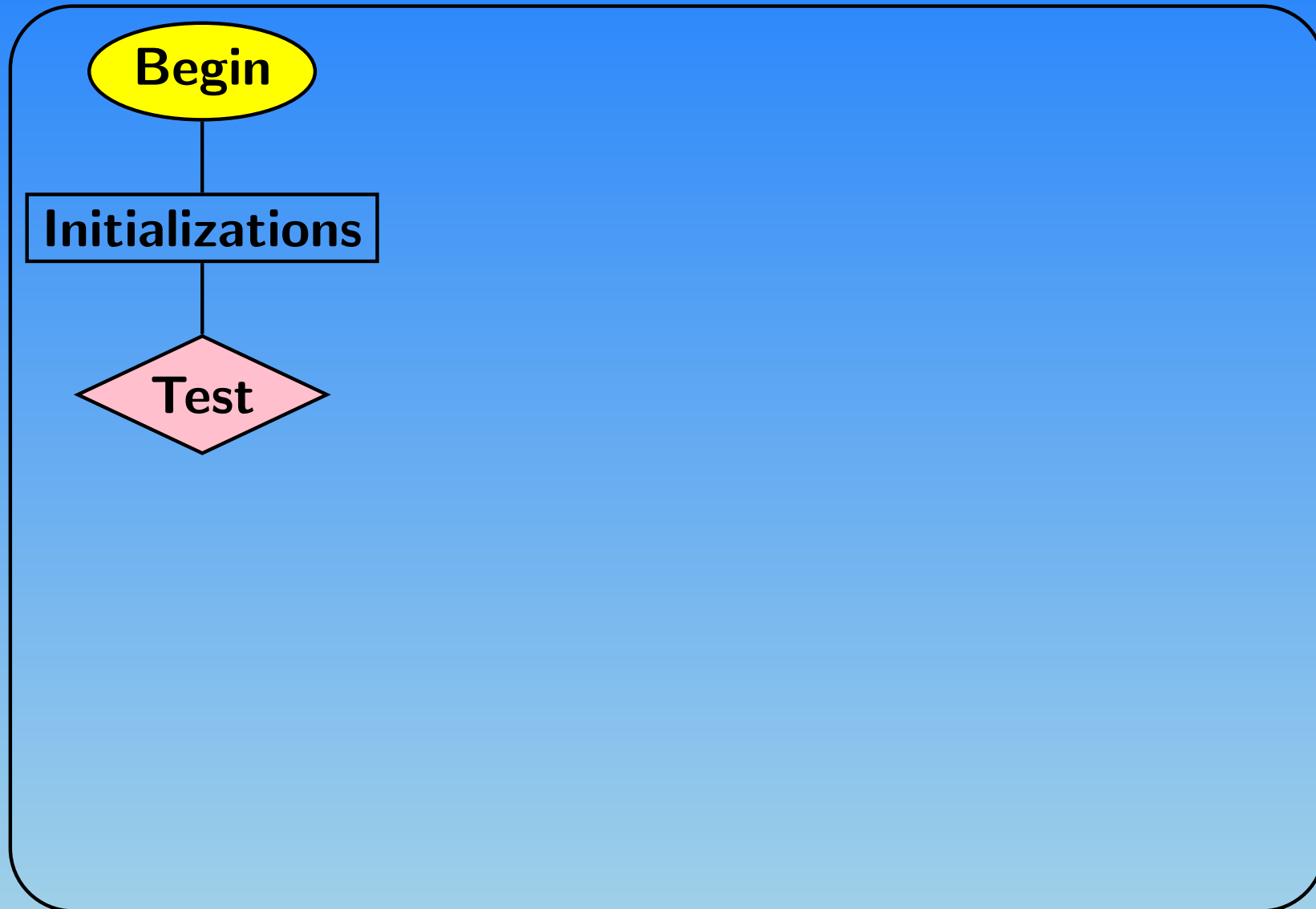
## The same diagram with overlays



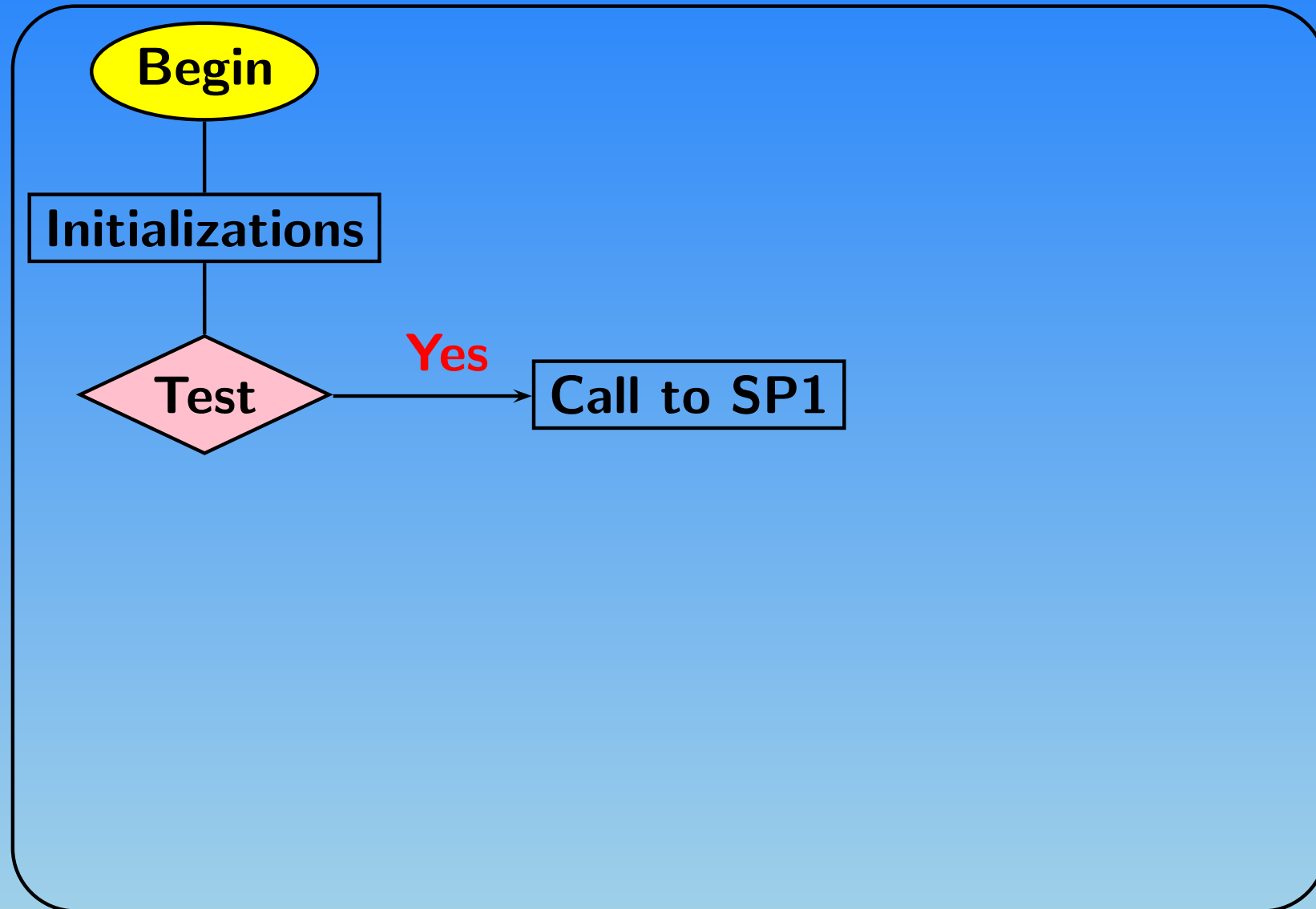
## The same diagram with overlays



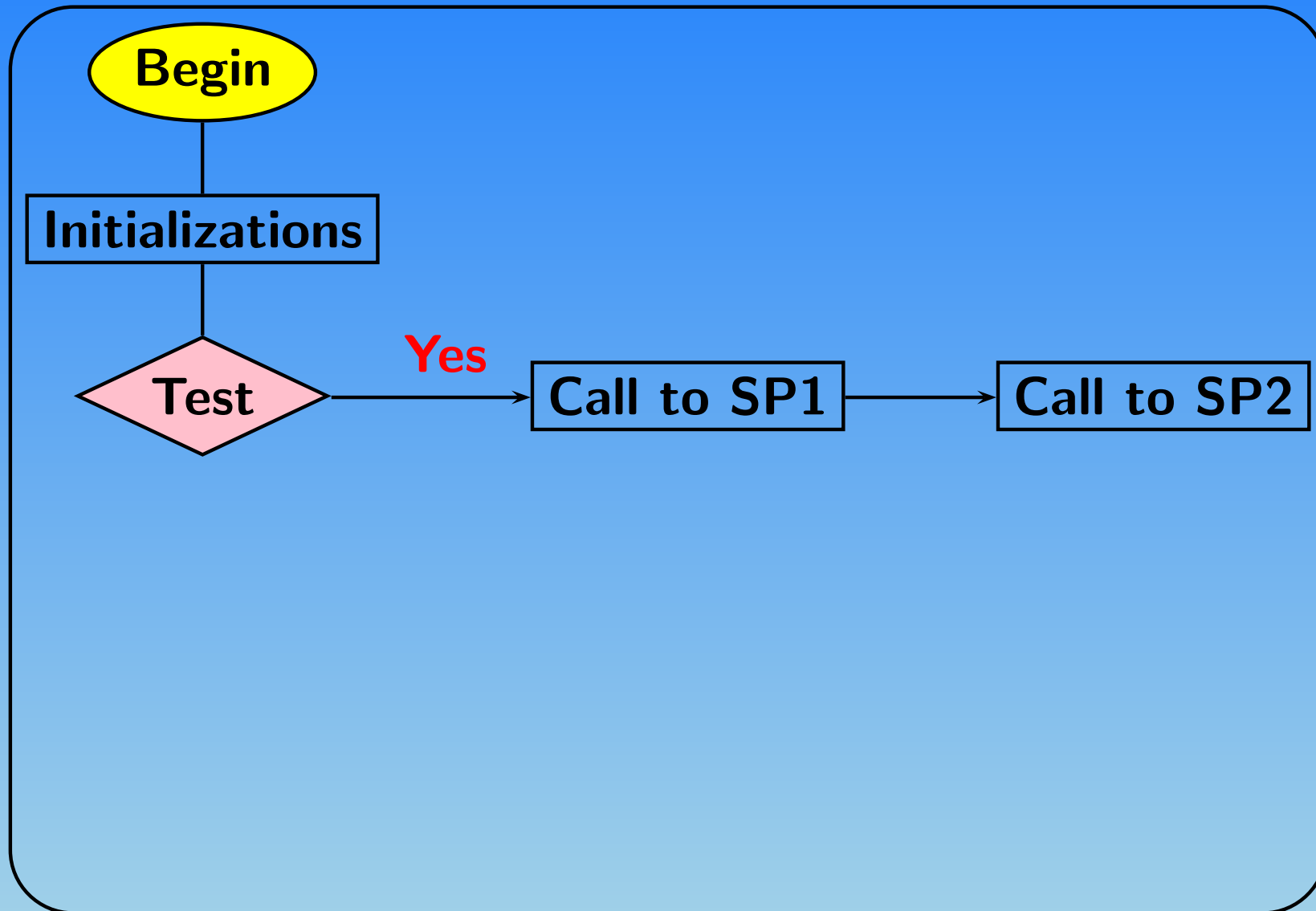
## The same diagram with overlays



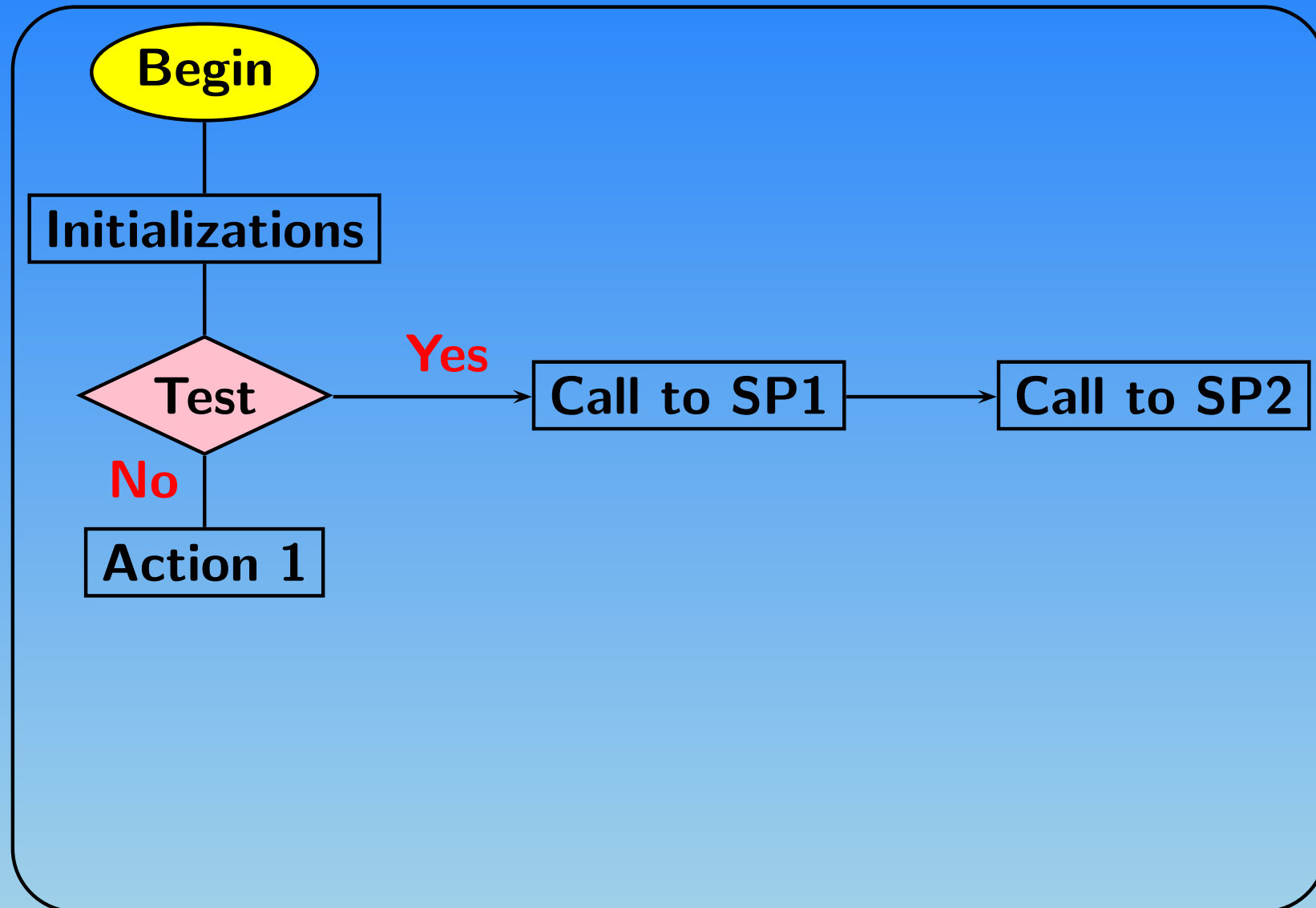
## The same diagram with overlays



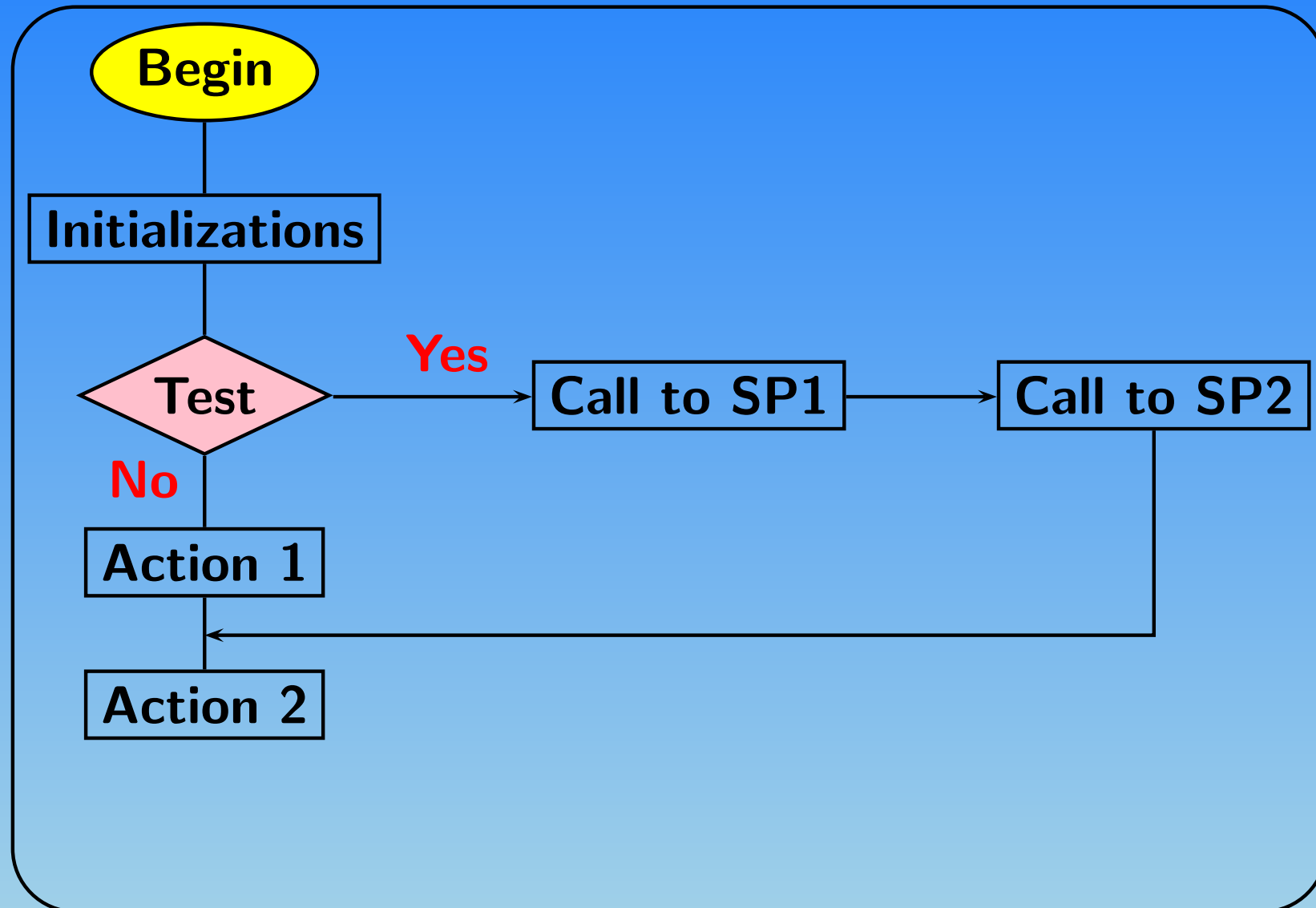
## The same diagram with overlays



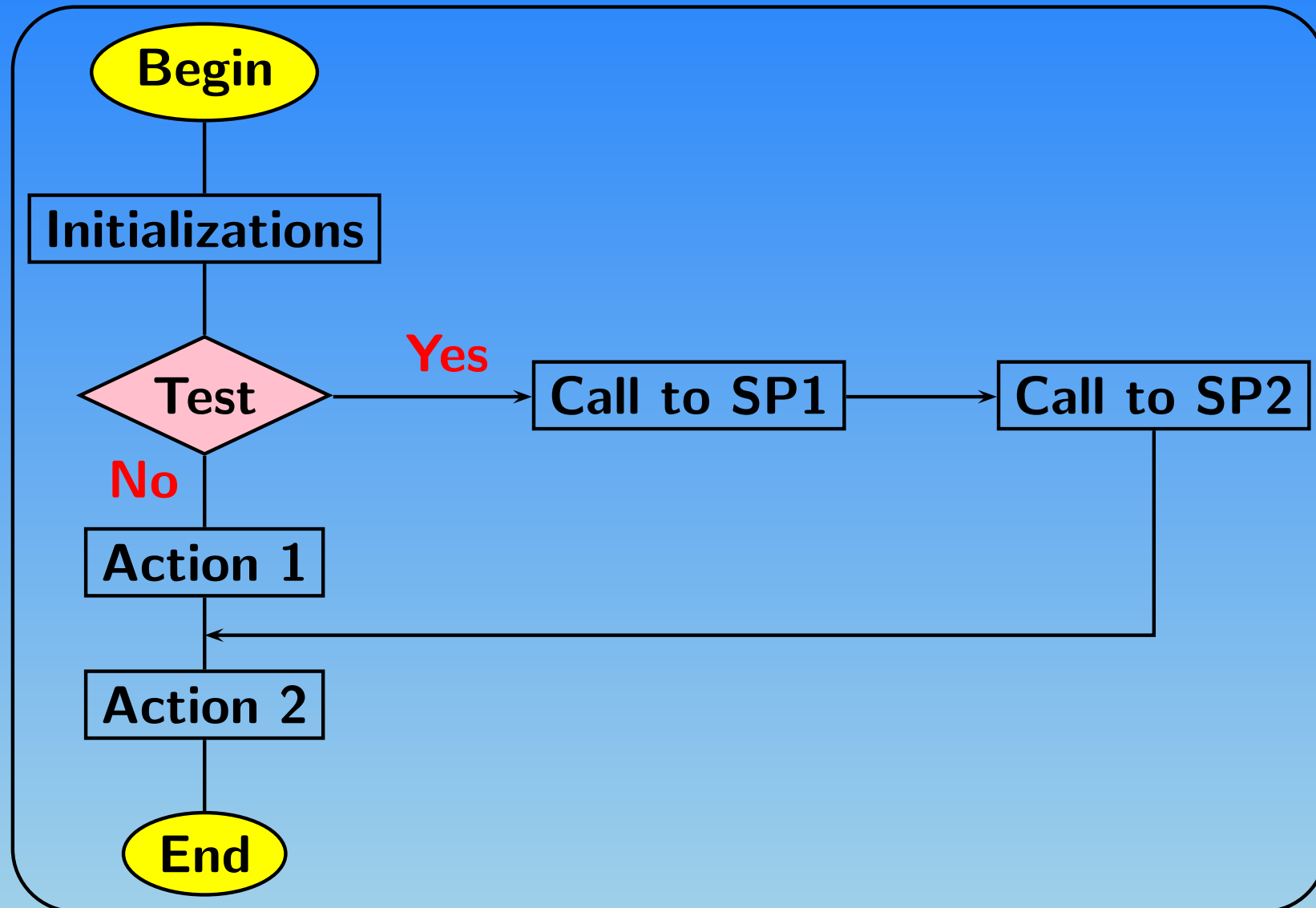
## The same diagram with overlays



## The same diagram with overlays



## The same diagram with overlays





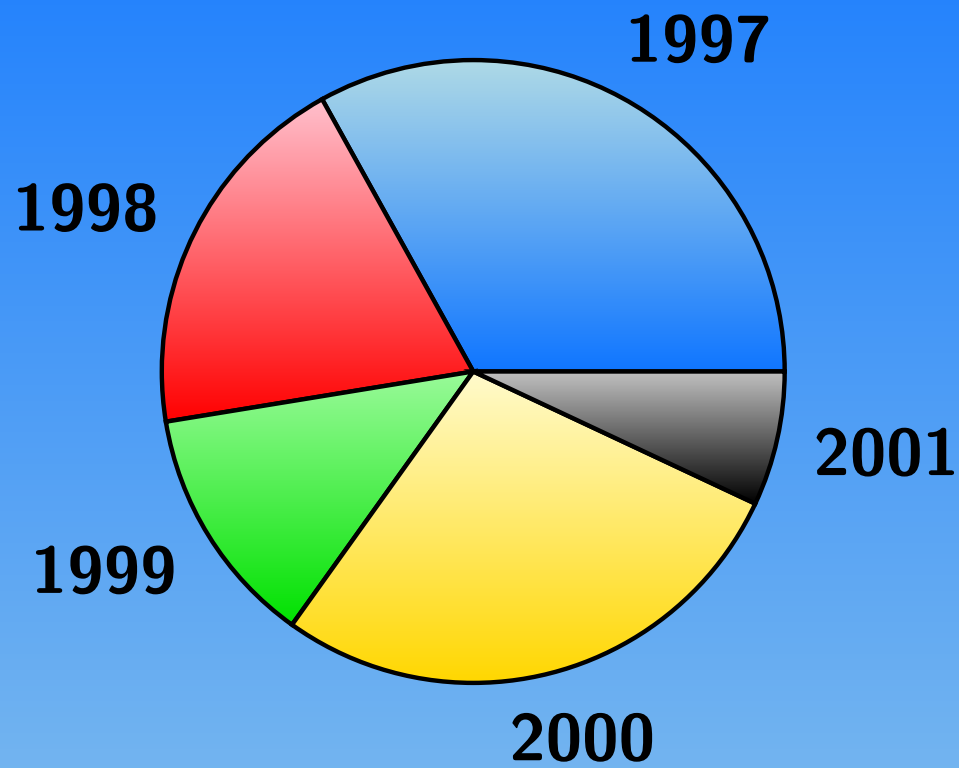


Figure 1: Results of the last five years

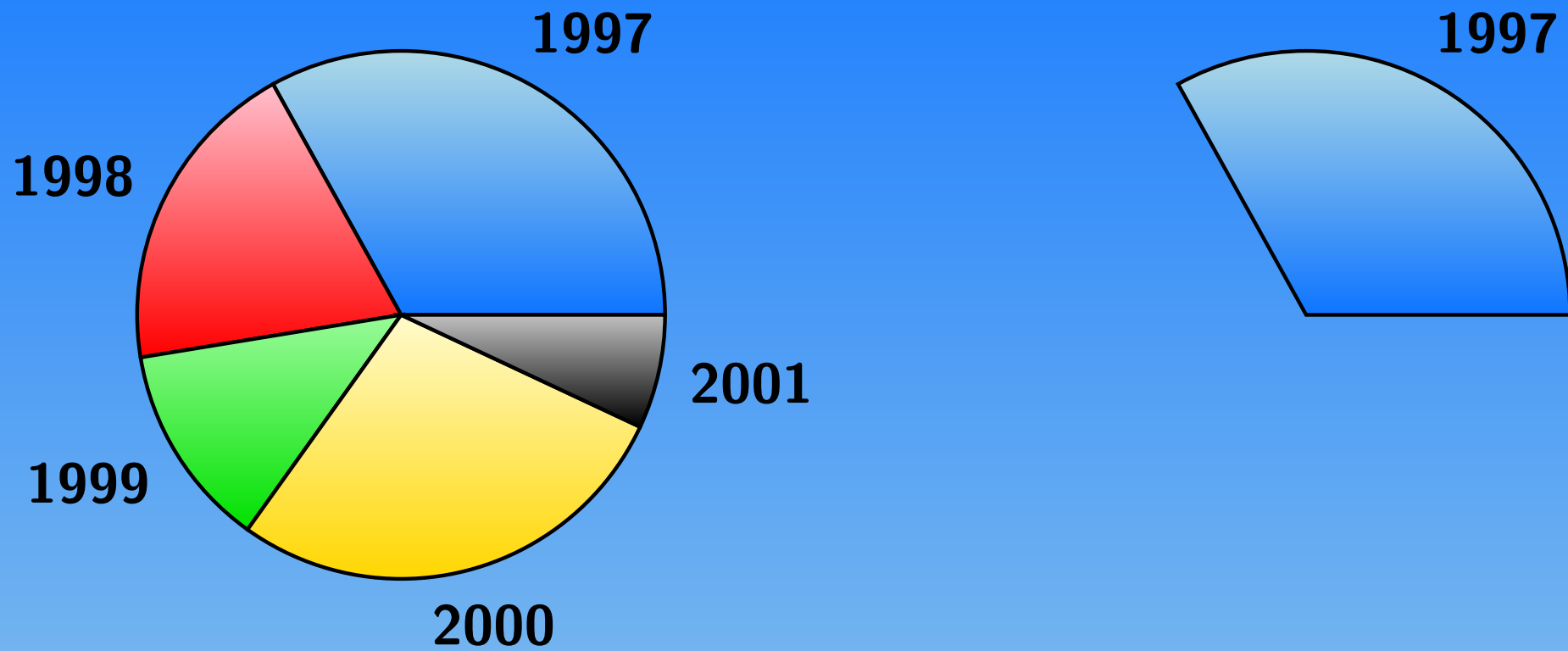


Figure 1: Results of the last five years

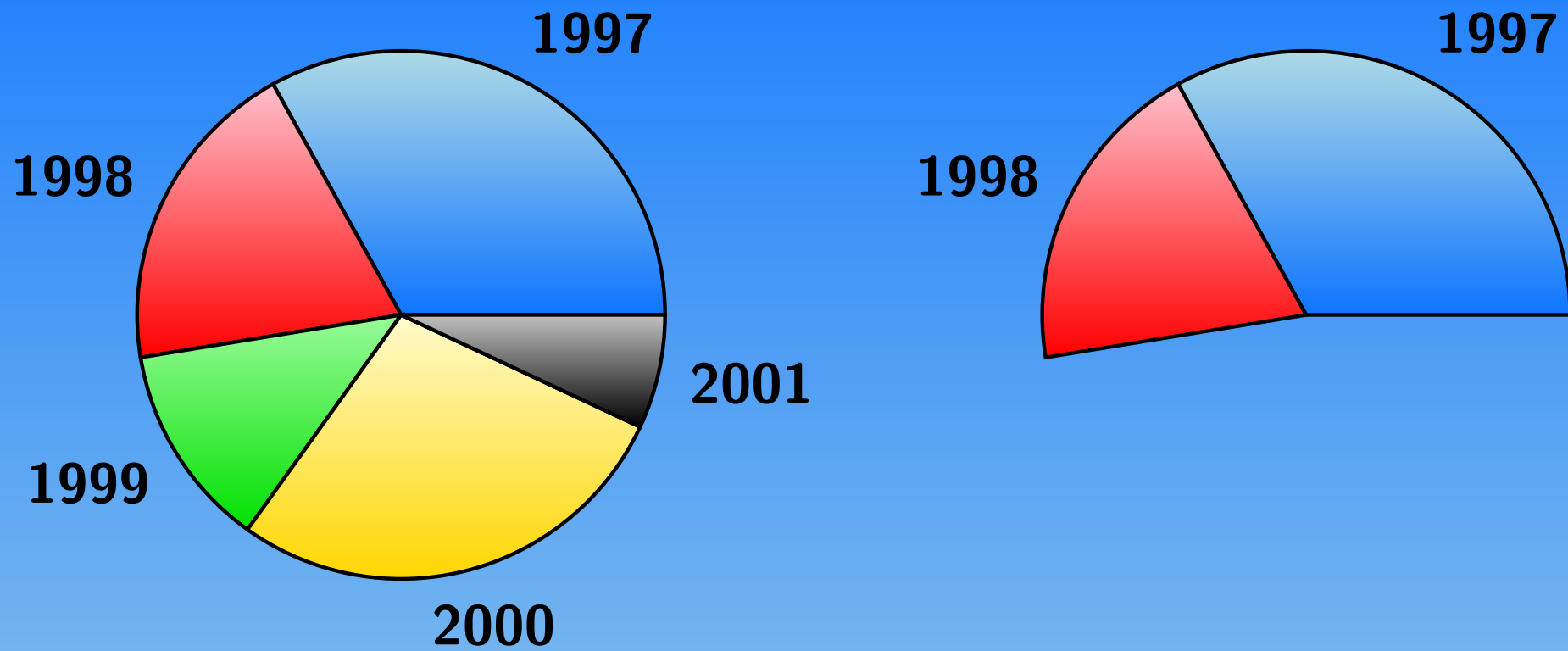


Figure 1: Results of the last five years

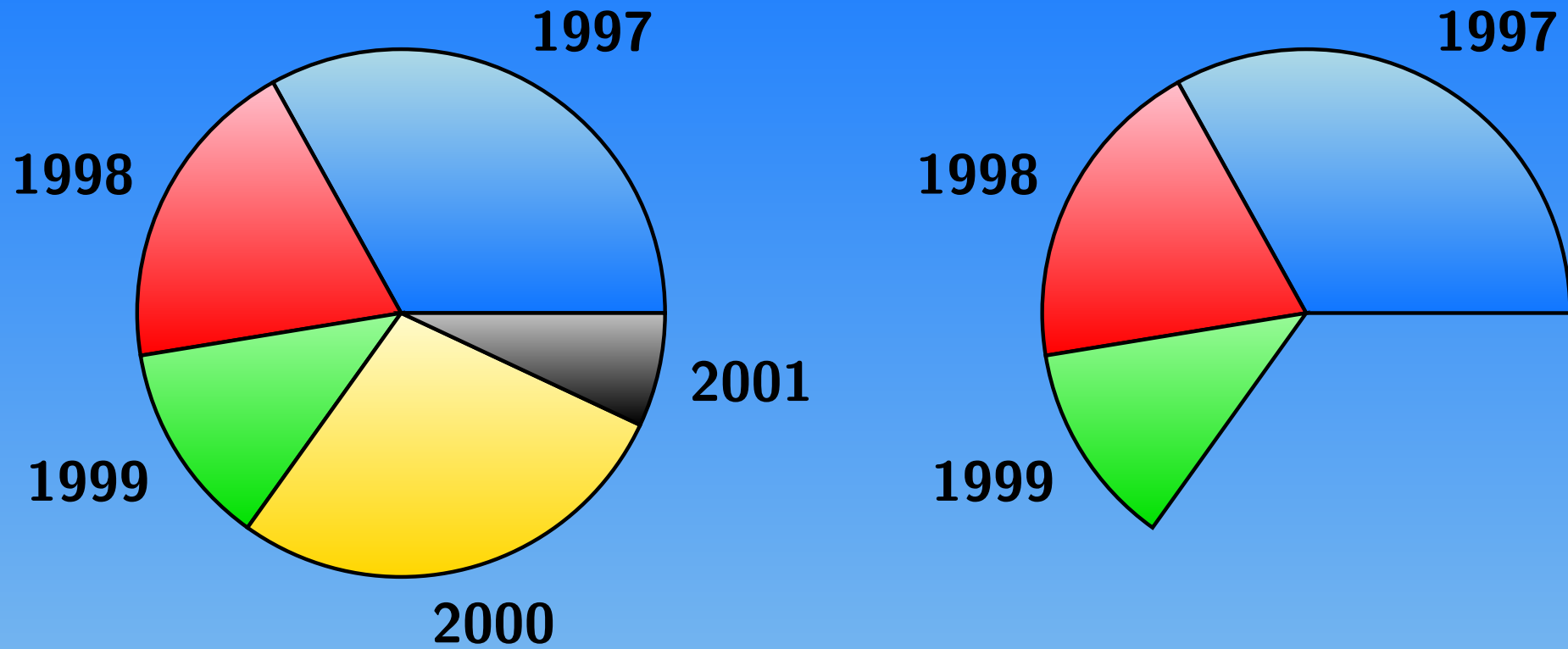


Figure 1: Results of the last five years

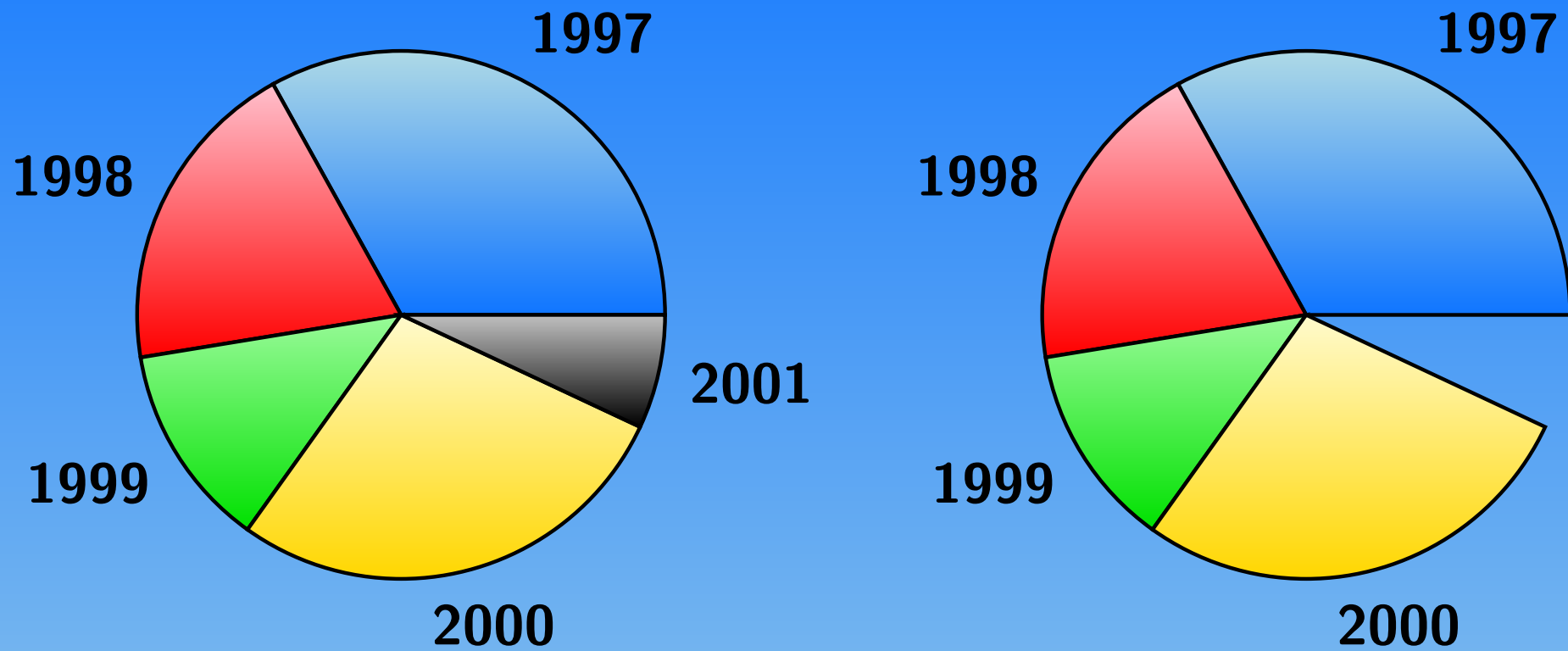


Figure 1: Results of the last five years

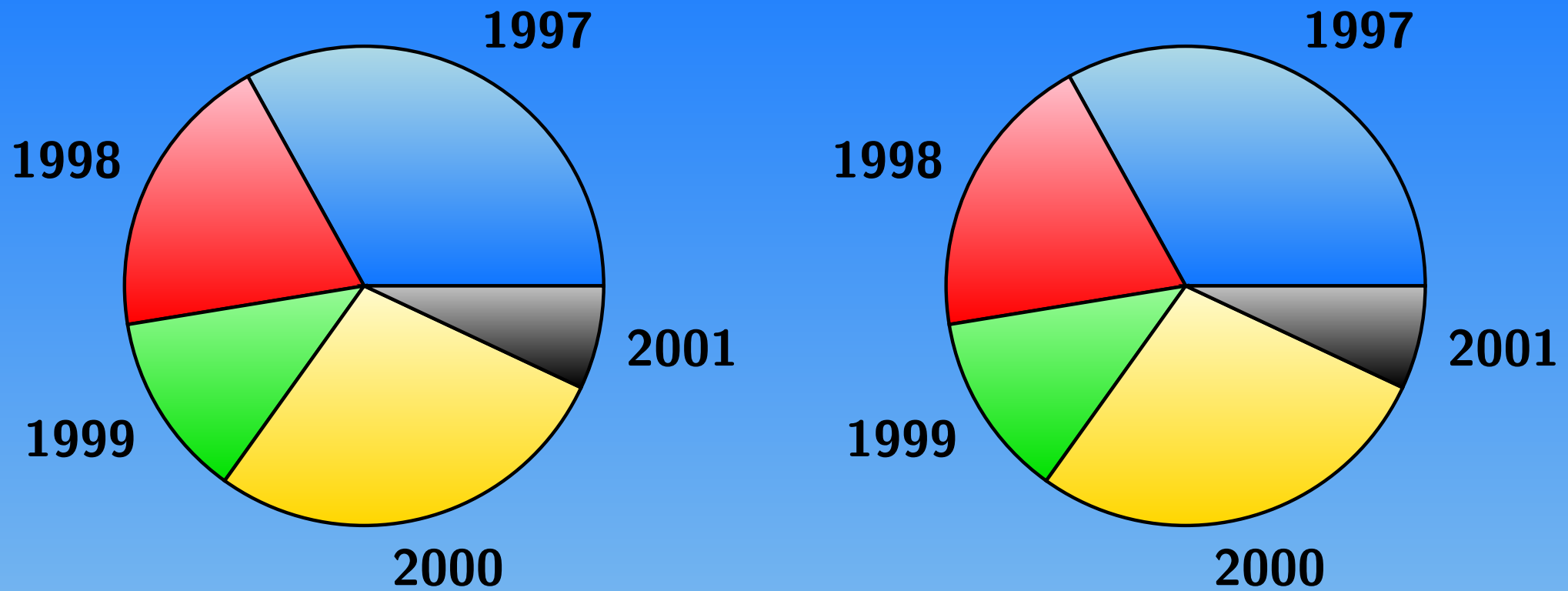


Figure 1: Results of the last five years

## Viewership Distribution of the Big Three

Age (years)



Figure 2: Main American TV channels

# Viewership Distribution of the Big Three

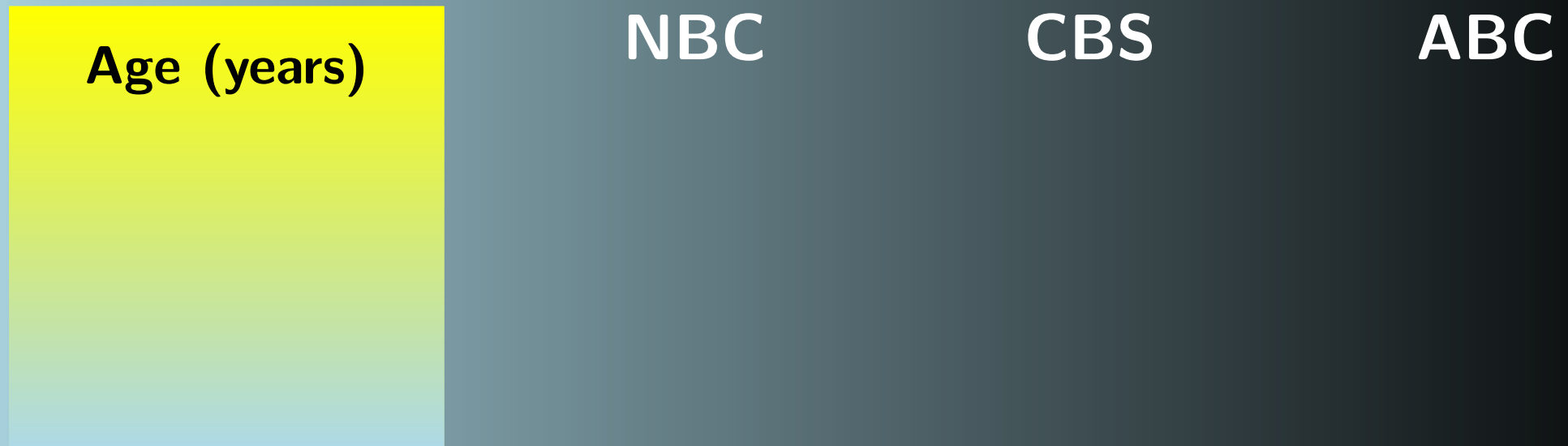


Figure 2: Main American TV channels



# Viewership Distribution of the Big Three

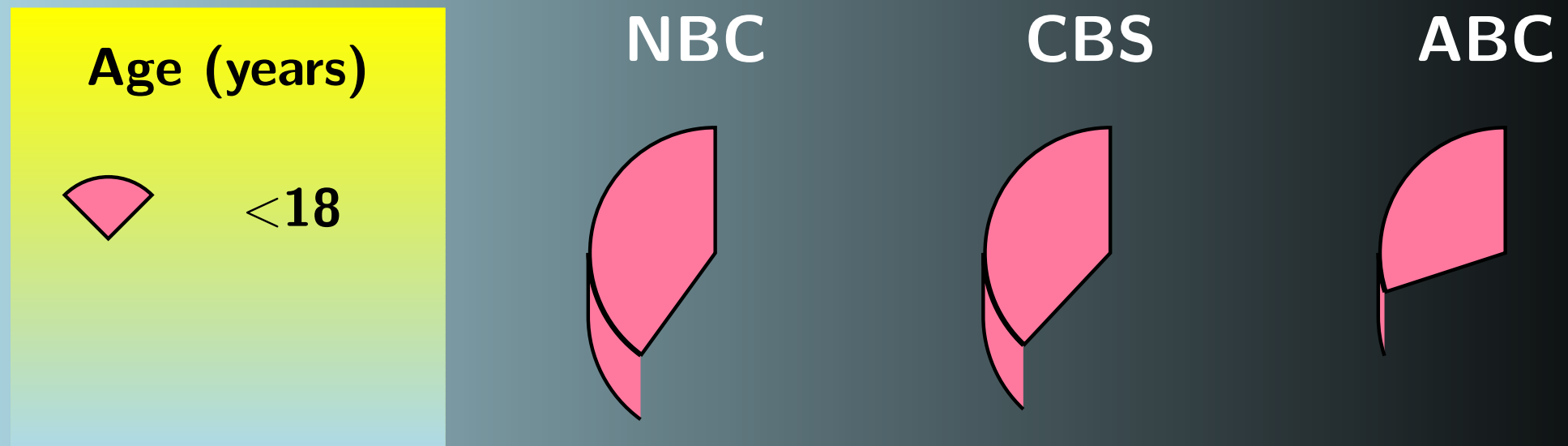


Figure 2: Main American TV channels

# Viewership Distribution of the Big Three

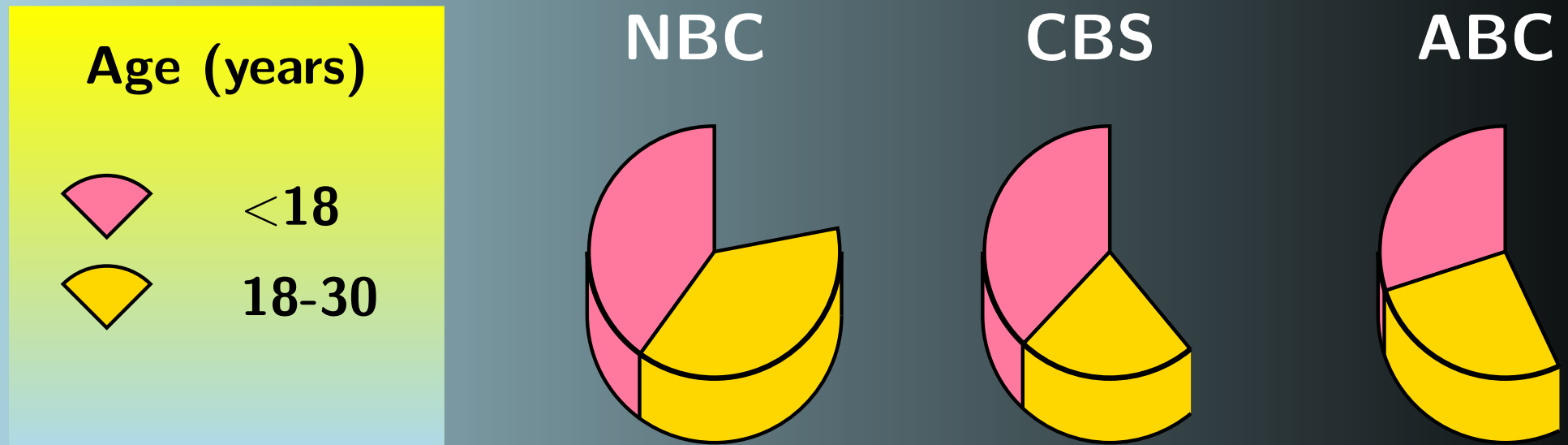


Figure 2: Main American TV channels

# Viewership Distribution of the Big Three

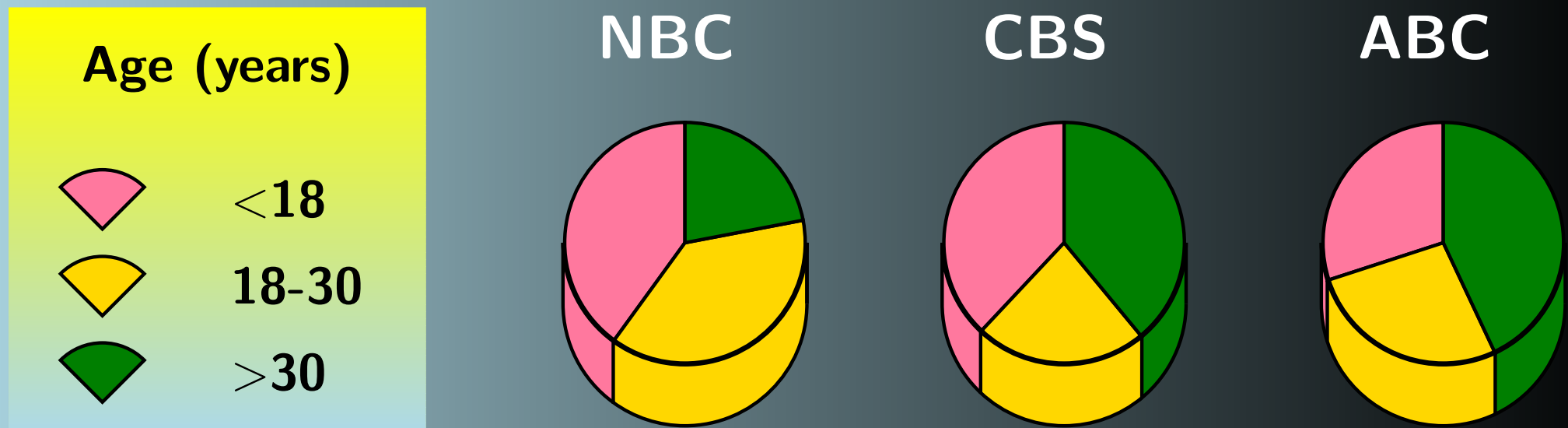


Figure 2: Main American TV channels

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$\Pi$

End of slide

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6}$$

= 2.44949


End of slide

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{\quad}$$

$= 2.44949$



## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1}$$

$= 2.44949$

$1 \implies 2.44949$

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4}}$$

**= 2.44949**

**1  $\implies$  2.44949**

**1.25  $\implies$  2.73861**

End of slide



## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9}}$$

The diagram illustrates the cumulative calculation of the formula for  $\Pi$ . It shows the formula  $\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9}}$  with arrows pointing from the terms  $1$ ,  $\frac{1}{4}$ , and  $\frac{1}{9}$  to boxes containing their cumulative values and the resulting  $\Pi$  value.

Cumulative Value	Resulting $\Pi$
1	2.44949
1.25	2.73861
1.36111	2.85774

End of slide

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16}}$$

The diagram illustrates the cumulative calculation of the formula for  $\Pi$ . It shows the formula  $\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16}}$  with arrows pointing from the terms to boxes showing intermediate values and their corresponding  $\Pi$  values:

- 1  $\implies$  2.44949
- 1.25  $\implies$  2.73861
- 1.36111  $\implies$  2.85774
- 1.42361  $\implies$  2.92261

The final result of the formula is shown as  $= 2.44949$ .

End of slide

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots}$$

The diagram illustrates the cumulative values of the series for  $\Pi$ . Arrows point from the terms  $1$ ,  $\frac{1}{4}$ ,  $\frac{1}{9}$ , and  $\frac{1}{16}$  to boxes containing cumulative sums and their corresponding  $\Pi$  values:

- $1 \implies 2.44949$
- $1.25 \implies 2.73861$
- $1.36111 \implies 2.85774$
- $1.42361 \implies 2.92261$

The final value of  $\Pi$  is shown as  $= 2.44949$ .

End of slide

## 2 – Equations with (cumulative) annotations

A formula for  $\Pi$  from Leonhard Euler

$$\Pi = \sqrt{6} \times \sqrt{1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots}$$

The diagram illustrates the cumulative calculation of the series for  $\Pi$ . It shows the terms  $1$ ,  $\frac{1}{4}$ ,  $\frac{1}{9}$ , and  $\frac{1}{16}$  being added to the sum. The cumulative sum and the resulting value of  $\Pi$  are shown in boxes:

- $1 \implies 2.44949$
- $1.25 \implies 2.73861$
- $1.36111 \implies 2.85774$
- $1.42361 \implies 2.92261$

The final value of  $\Pi$  is  $2.44949$ .

$$= \left( 6 \sum_{n=1}^{\infty} \frac{1}{n^2} \right)^{\frac{1}{2}}$$

End of slide

## 3 – Listing with (progressive) annotations

- ➡ From a manual to introduce to parallel programming with the MPI library
- ➡ First with overlays but without annotations, just using the features of the 'fancyvrb' package

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6
7
8
9
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13
14 end program WhoAmI
```

End of slide

## 3 – Listing with (progressive) annotations

- ➡ From a manual to introduce to parallel programming with the MPI library
- ➡ First with overlays but without annotations, just using the features of the 'fancyvrb' package

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8
9
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13
14 end program WhoAmI
```

End of slide

## 3 – Listing with (progressive) annotations

- ➡ From a manual to introduce to parallel programming with the MPI library
- ➡ First with overlays but without annotations, just using the features of the 'fancyvrb' package

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8
9
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13   call MPI_FINALIZE(code)
14 end program WhoAmI
```

End of slide

## 3 – Listing with (progressive) annotations

- ➡ From a manual to introduce to parallel programming with the MPI library
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```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8   call MPI_COMM_SIZE(MPI_COMM_WORLD,nb_procs,code)
9
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE(code)
14 end program WhoAmI
```

End of slide



## 3 – Listing with (progressive) annotations

- ➡ From a manual to introduce to parallel programming with the MPI library
- ➡ First with overlays but without annotations, just using the features of the 'fancyvrb' package

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8   call MPI_COMM_SIZE(MPI_COMM_WORLD,nb_procs,code)
9   call MPI_COMM_RANK(MPI_COMM_WORLD,rank,code)
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE(code)
14 end program WhoAmI
```

End of slide

➡ Then the same code, but using both the features of the 'fancyvrb' and 'listings' packages, with an automatic *pretty printing* of the code, after definition of a new language to emphasize the MPI-1 constants and subroutines (see the file `lstlang0.sty`)

➡ We could also use the 'listings' package alone

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6
7
8
9
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13
14 end program WhoAmI
```

End of slide

➡ Then the same code, but using both the features of the 'fancyvrb' and 'listings' packages, with an automatic *pretty printing* of the code, after definition of a new language to emphasize the MPI-1 constants and subroutines (see the file `lstlang0.sty`)

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1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8
9
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13
14 end program WhoAmI
```

End of slide

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1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8
9
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

End of slide

☞ Then the same code, but using both the features of the 'fancyvrb' and 'listings' packages, with an automatic *pretty printing* of the code, after definition of a new language to emphasize the MPI-1 constants and subroutines (see the file `lstlang0.sty`)

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```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9
10
11  print *, 'I am process ',rank, ' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

End of slide

☞ Then the same code, but using both the features of the 'fancyvrb' and 'listings' packages, with an automatic *pretty printing* of the code, after definition of a new language to emphasize the MPI-1 constants and subroutines (see the file `lstlang0.sty`)

☞ We could also use the 'listings' package alone

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE (MPI_COMM_WORLD ,nb_procs ,code )
9   call MPI_COMM_RANK (MPI_COMM_WORLD ,rank ,code )
10
11  print *, 'I am process ',rank, ' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

End of slide

➡ And now always the same code, but adding external annotations, using PStricks nodes. This time, all annotations are shown together, without using overlays.

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD , rank , code )
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

The diagram shows four annotations with arrows pointing to specific lines of code:

- Initialization of MPI environment** (blue text in a white box) points to line 6: `call MPI_INIT (code)`.
- Number of processes for the current execution** (yellow text in a yellow box) points to the `nb_procs` argument in line 8: `MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )`.
- Rank of the process among all of them** (blue text in a white box) points to the `rank` argument in line 9: `MPI_COMM_RANK ( MPI_COMM_WORLD , rank , code )`.
- Exit of MPI environment** (blue text in a white box) points to line 13: `call MPI_FINALIZE (code)`.

- ➔ Then finally the same code again, with the same annotations, but shown in a progressive way, using overlays

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD ,rank ,code )
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```



- ➔ Then finally the same code again, with the same annotations, but shown in a progressive way, using overlays

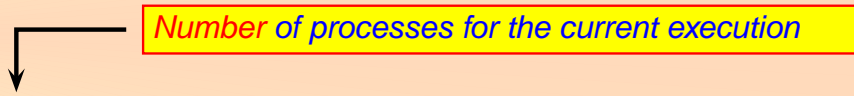
```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD ,rank ,code )
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

Initialization of MPI environment

End of slide

- ➔ Then finally the same code again, with the same annotations, but shown in a progressive way, using overlays

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD , rank , code )
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```



- ➔ Then finally the same code again, with the same annotations, but shown in a progressive way, using overlays

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD ,rank ,code )
10
11   print *, 'I am process ',rank,' among ',nb_procs
12
13   call MPI_FINALIZE (code)
14 end program WhoAmI
```

↑ Rank of the process among all of them

- ➔ Then finally the same code again, with the same annotations, but shown in a progressive way, using overlays

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD ,rank ,code )
10
11  print *, 'I am process ',rank,' among ',nb_procs
12
13  call MPI_FINALIZE (code) ← Exit of MPI environment
14 end program WhoAmI
```

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6
7
8
9
10
11   print *, 'I am process ',      , ' among ',
12
13
14 end program WhoAmI
```

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8
9
10
11   print *, 'I am process ', rank, ' among ', nb_procs
12
13
14 end program WhoAmI
```

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8
9
10
11  print *, 'I am process ', rank, ' among ', nb_procs
12
13
14 end program WhoAmI
```

*Initialization of MPI environment*



End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT(code)
7
8
9
10
11  print *, 'I am process ', rank, ' among ', nb_procs
12
13  call MPI_FINALIZE(code)
14 end program WhoAmI
```

*Initialization of MPI environment*



End of slide



## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8
9
10
11  print *, 'I am process ', rank, ' among ', nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

*Initialization of MPI environment*

*Exit of MPI environment*

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD ,nb_procs ,code )
9
10
11  print *, 'I am process ', rank , ' among ', nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

*Initialization of MPI environment*

*Exit of MPI environment*

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )
9
10
11  print *, 'I am process ', rank , ' among ', nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

*Initialization of MPI environment*

*Number of processes for the current execution*

*Exit of MPI environment*

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD , rank , code )
10
11  print *, 'I am process ', rank , ' among ', nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

Initialization of MPI environment

Number of processes for the current execution

Exit of MPI environment

End of slide

## 4 – (Cumulative) listing with (cumulative) annotations (I)

```
1 program WhoAmI
2   implicit none
3   include 'mpif.h'
4   integer :: nb_procs,rank,code
5
6   call MPI_INIT (code)
7
8   call MPI_COMM_SIZE ( MPI_COMM_WORLD , nb_procs , code )
9   call MPI_COMM_RANK ( MPI_COMM_WORLD , rank , code )
10
11  print *, 'I am process ', rank , ' among ', nb_procs
12
13  call MPI_FINALIZE (code)
14 end program WhoAmI
```

Initialization of MPI environment

Number of processes for the current execution

Rank of the process among all of them

Exit of MPI environment

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
3
4 #include <OB/CORBA.h>
5 #include <export_skel.h>
6
7 class ClassMatrix : virtual public POA_Exporte {
8
9     private :
10         TypeMatrix A;
11
12     public :
13         ClassMatrix(double init);
14         ~ClassMatrix();
15
16         virtual void MultiplyVector(CORBA::Double alpha,
17                                     TypeVector_slice *vector)
18             throw(CORBA::SystemException);
19 };
```

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
3
4 #include <OB/CORBA.h>
5 #include <export_skel.h>
6
7 class ClassMatrix : virtual public POA_Exporte {
8
9     private :
10         TypeMatrix A;
11
12     public :
13         ClassMatrix(double init);
14         ~ClassMatrix( );
15
16         virtual void MultiplyVector(CORBA::Double    alpha,
17                                     TypeVector_slice *vector)
18             throw(CORBA::SystemException);
19 };
```

*File of CORBA required headers*

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
3
4 #include <OB/CORBA.h>
5 #include <export_skel.h>
6
7 class ClassMatrix : virtual public POA_Exporte {
8
9     private :
10         TypeMatrix A;
11
12     public :
13         ClassMatrix(double init);
14         ~ClassMatrix( );
15
16         virtual void MultiplyVector(CORBA::Double    alpha,
17                                     TypeVector_slice *vector)
18             throw(CORBA::SystemException);
19 };
```

*File of CORBA required headers*

*File of headers relative to the skeleton generated from the IDL interface by the IDL compiler*

End of slide



## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
3
4 #include <OB/CORBA.h>
5 #include <export_skel.h>
6
7 class ClassMatrix : virtual public POA_Exporte {
8
9     private :
10         TypeMatrix A;
11
12     public :
13         ClassMatrix(double init);
14         ~ClassMatrix( );
15
16         virtual void MultiplyVector(CORBA::Double    alpha,
17                                     TypeVector_slice *vector)
18             throw(CORBA::SystemException);
19 };
```

*File of CORBA required headers*

*File of headers relative to the **skeleton** generated from the IDL interface by the IDL compiler*

*The class **ClassMatrix** must now be known inside the CORBA POA*

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
3
4 #include <OB/CORBA.h>
5 #include <export_skel.h>
6
7 class ClassMatrix : virtual public POA_Exporte {
8
9     private :
10         TypeMatrix A;
11
12     public :
13         ClassMatrix(double init);
14         ~ClassMatrix();
15
16         virtual void MultiplyVector(CORBA::Double alpha,
17                                     TypeVector_slice *vector)
18             throw(CORBA::SystemException);
19 };
```

*File of CORBA required headers*

*File of headers relative to the skeleton generated from the IDL interface by the IDL compiler*

*The class ClassMatrix must now be known inside the CORBA POA*

*Constructor*

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
```

```
3
4 #include <OB/CORBA.h>
```

```
5 #include <export_skel.h>
```

```
6
7 class ClassMatrix : virtual public POA_Exporte {
```

```
8
9 private :
10     TypeMatrix A;
```

```
11
12 public :
```

```
13     ClassMatrix(double init);
```

```
14     ~ClassMatrix();
```

```
15
16     virtual void MultiplyVector(CORBA::Double    alpha,
17                                 TypeVector_slice *vector)
18         throw(CORBA::SystemException);
```

```
19 };
```

*File of CORBA required headers*

*File of headers relative to the skeleton generated from the IDL interface by the IDL compiler*

*The class ClassMatrix must now be known inside the CORBA POA*

*Constructor*

*Destructor*

End of slide

## 5 – Listing with (cumulative) annotations (II)

➔ From a manual to introduce to distributed programming with CORBA

```
1 #include <iostream.h>
2 #include <fstream.h>
```

```
3
4 #include <OB/CORBA.h>
```

```
5 #include <export_skel.h>
```

```
6
7 class ClassMatrix : virtual public POA_Exporte {
```

```
8
9 private :
10     TypeMatrix A;
```

```
11
12 public :
13     ClassMatrix(double init);
```

```
14     ~ClassMatrix();
```

```
15
16     virtual void MultiplyVector(CORBA::Double    alpha,
17                                 TypeVector_slice *vector)
18         throw(CORBA::SystemException);
```

```
19 };
```

*File of CORBA required headers*

*File of headers relative to the skeleton generated from the IDL interface by the IDL compiler*

*The class ClassMatrix must now be known inside the CORBA POA*

*Constructor*

*Destructor*

*Definition of a service to multiply a matrix by a scalar and a vector, with a management of the exceptions done by CORBA*

End of slide

```
20 // Implementation of the methods
21
22 ClassMatrix::ClassMatrix(double cste) {
23     long long i, j;
24
25     for (i = 0; i < N; i++) {
26         for (j = 0; j < N; j++) {
27             A[i][j] = 0.0;}}
28     for (i = 0; i < N; i++) {
29         A[i][i] = cste;}
30 }
31
32 ClassMatrix::~ClassMatrix() {
33     cout << "Destruction of the object" << endl;
34 }
35
36 void ClassMatrix::MultiplyVector(CORBA::Double alpha,
37     TypeVector_slice *vector)
38     throw(CORBA::SystemException) {
39
40     long long i, j;
41     TypeVector tmp;
42
43     for (i = 0; i < N; i++) {
44         tmp[i] = 0.0;
45         for (j = 0; j < N; j++) {
46             tmp[i] = tmp[i] + alpha * A[i][j] * vector[j];
47         }
48     }
49     for (i = 0; i < N; i++) vector[i] = tmp[i];
50 }
```

End of slide

```
20 // Implementation of the methods
```

```
21 ClassMatrix: :ClassMatrix(double cste) {
```

```
22     long long i, j;
```

```
23     for (i = 0; i < N; i++) {
```

```
24         for (j = 0; j < N; j++) {
```

```
25             A[i][j] = 0.0;}}
```

```
26     for (i = 0; i < N; i++) {
```

```
27         A[i][i] = cste;}
```

```
28     }
```

```
29 }
```

```
30 ClassMatrix: :~ClassMatrix() {
```

```
31     cout << "Destruction of the object" << endl;
```

```
32 }
```

```
33 void ClassMatrix: :MultiplyVector(CORBA: :Double alpha,
```

```
34     TypeVector_slice *vector)
```

```
35     throw(CORBA: :SystemException) {
```

```
36     long long i, j;
```

```
37     TypeVector tmp;
```

```
38     for (i = 0; i < N; i++) {
```

```
39         tmp[i] = 0.0;
```

```
40         for (j = 0; j < N; j++) {
```

```
41             tmp[i] = tmp[i] + alpha * A[i][j] * vector[j];
```

```
42         }
```

```
43     }
```

```
44     for (i = 0; i < N; i++) vector[i] = tmp[i];
```

```
45 }
```

Implementation of the constructor:  
initialization of the matrix to the identity matrix

```
20 // Implementation of the methods
```

```
21 ClassMatrix::ClassMatrix(double cste) {
```

```
22     long long i, j;
```

```
23     for (i = 0; i < N; i++) {
```

```
24         for (j = 0; j < N; j++) {
```

```
25             A[i][j] = 0.0;}}
```

```
26     for (i = 0; i < N; i++) {
```

```
27         A[i][i] = cste;}
```

```
28     }
```

```
29 }
```

```
30 }
```

```
31
```

```
32 ClassMatrix::~ClassMatrix() {
```

```
33     cout << "Destruction of the object" << endl;
```

```
34 }
```

```
35
```

```
36 void ClassMatrix::MultiplyVector(CORBA::Double alpha,
```

```
37     TypeVector_slice *vector)
```

```
38     throw(CORBA::SystemException) {
```

```
39     long long i, j;
```

```
40     TypeVector tmp;
```

```
41     for (i = 0; i < N; i++) {
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42         tmp[i] = 0.0;
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```
43         for (j = 0; j < N; j++) {
```

```
44             tmp[i] = tmp[i] + alpha * A[i][j] * vector[j];
```

```
45         }
```

```
46     }
```

```
47     for (i = 0; i < N; i++) vector[i] = tmp[i];
```

```
48 }
```

```
49 }
```

Implementation of the **constructor**:  
initialization of the matrix to the identity matrix

Implementation of the **destructor**:  
generally memory deallocation

End of slide

```
20 // Implementation of the methods
```

```
21 ClassMatrix: :ClassMatrix(double cste) {
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22     long long i, j;
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23     for (i = 0; i < N; i++) {
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24         for (j = 0; j < N; j++) {
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25             A[i][j] = 0.0;}}
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26     for (i = 0; i < N; i++) {
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27         A[i][i] = cste;}
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```
28     }
```

```
29 }
```

Implementation of the **constructor**:  
initialization of the matrix to the identity matrix

```
30 ClassMatrix: :~ClassMatrix() {
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31     cout << "Destruction of the object" << endl;
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Implementation of the **destructor**:  
generally memory deallocation

```
33 void ClassMatrix: :MultiplyVector(CORBA: :Double alpha,
```

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34     TypeVector_slice *vector) {
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35     throw(CORBA: :SystemException) {
```

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36         long long i, j;
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37         TypeVector tmp;
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38         for (i = 0; i < N; i++) {
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39             tmp[i] = 0.0;
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40             for (j = 0; j < N; j++) {
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```
41                 tmp[i] = tmp[i] + alpha * A[i][j] * vector[j];
```

```
42             }
```

```
43         }
```

```
44         for (i = 0; i < N; i++) vector[i] = tmp[i];
```

```
45     }
```

Service to compute the product of a matrix  
(multiplied by a constant) with a vector, with  
a management of the exceptions done by  
CORBA

End of slide



```
51 // Main program
52
53 int main(int argc, char* argv[])
54 {
55     // Initialization of the CORBA ORB and POA
56     CORBA::ORB_var orb = CORBA::ORB_init(argc, argv);
57     CORBA::Object_var poaObj = orb -> resolve_initial_references("RootPOA");
58     PortableServer::POA_var RootPOA = PortableServer::POA::_narrow(poaObj);
59
60     ClassMatrix Matrix( (double) (1.0));
61
62     // Writing of the "universal pointer" IOR in the file "reference"
63     CORBA::String_var str = orb -> object_to_string( Matrix._this() );
64     ofstream out("reference");
65     out << str << endl;
66     out.close();
67
68     RootPOA -> the_POAManager() -> activate();
69     orb -> run();
70
71     orb -> destroy();
72 }
```

End of slide

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End of slide

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End of slide

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End of slide

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End of slide

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61
62     // Writing of the "universal pointer" IOR in the file "reference"
63     CORBA::String_var str = orb -> object_to_string( Matrix._this() ); ← Local characters string, used to
64     ofstream out( "reference" ); } store the generated reference
65     out << str << endl; } ← Writing of this server reference in the file
66     out.close(); } reference
67
68     RootPOA -> the_POAManager() -> activate();
69     orb -> run();
70
71     orb -> destroy();
72 }
```

End of slide

```
51 // Main program
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64     ofstream out( "reference" ); } store the generated reference
65     out << str << endl;
66     out.close(); } ← Writing of this server reference in the file
67                                     reference
68     RootPOA -> the_POAManager() -> activate(); } ← Activation of the ORB (which will "listen")
69     orb -> run();
70
71     orb -> destroy();
72 }
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End of slide

```
51 // Main program
52
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64     ofstream out( "reference" ); } store the generated reference
65     out << str << endl;
66     out.close(); } ← Writing of this server reference in the file
67                                     reference
68     RootPOA -> the_POAManager() -> activate(); } ← Activation of the ORB (which will "listen")
69     orb -> run();
70
71     orb -> destroy(); ← Destruction of the ORB (it will never occur
72 } here)
```

End of slide



## 2 – Communication ring

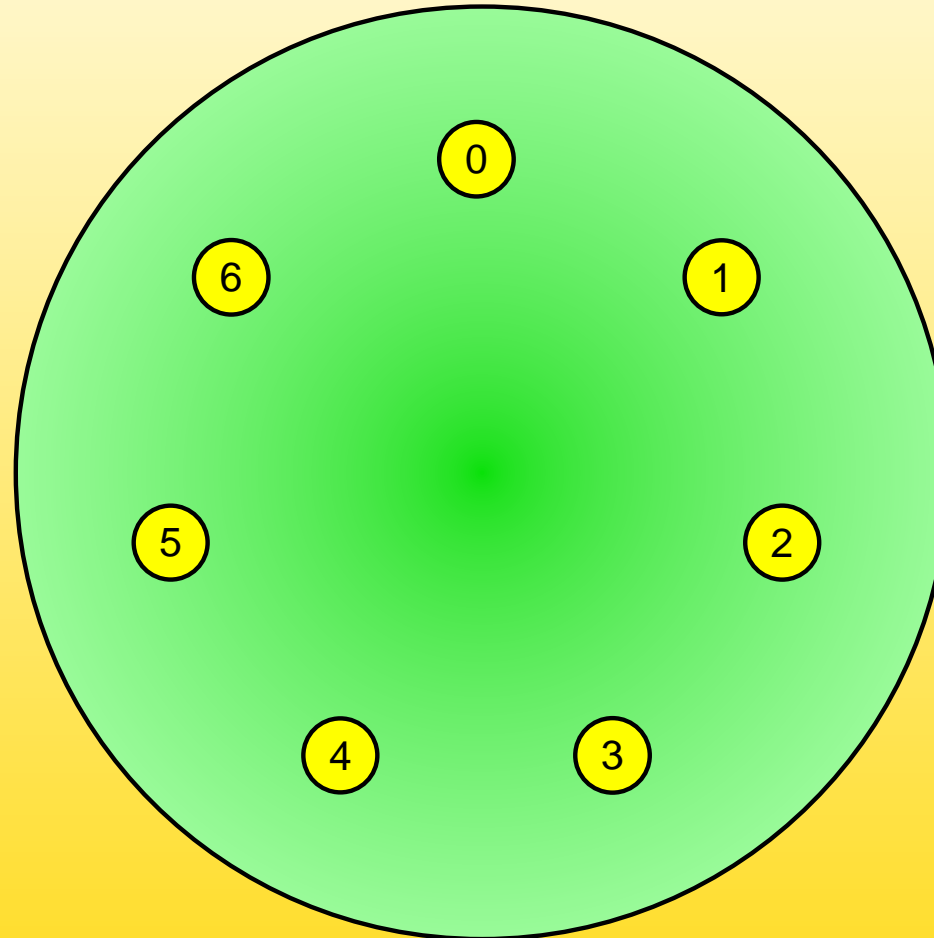


Figure 1: Communication ring

End of animation

## 2 – Communication ring

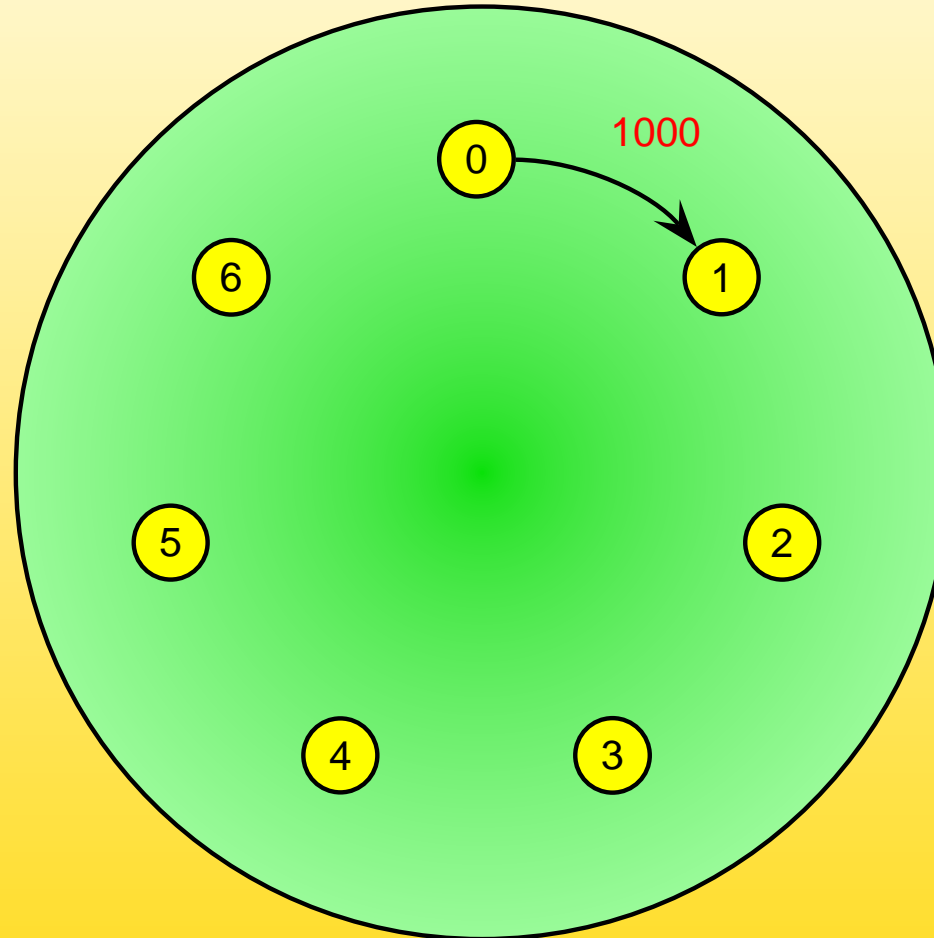


Figure 1: Communication ring

End of animation

## 2 – Communication ring

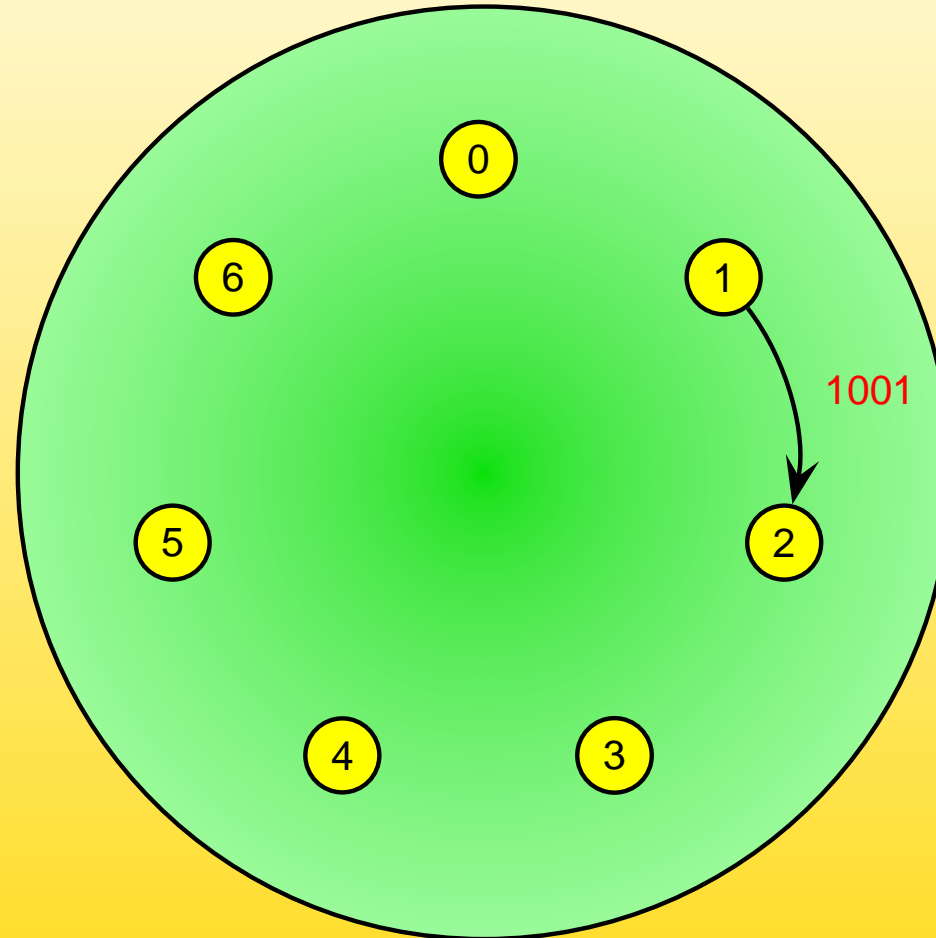


Figure 1: Communication ring

End of animation

## 2 – Communication ring

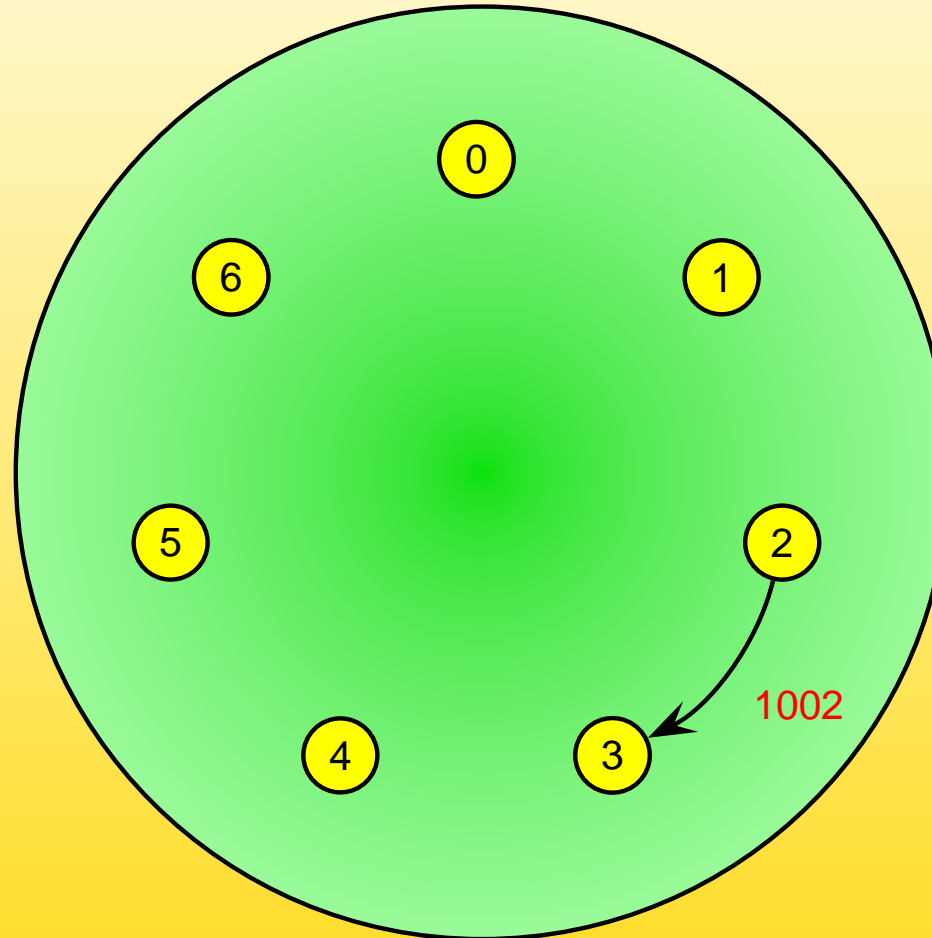


Figure 1: Communication ring

End of animation

## 2 – Communication ring

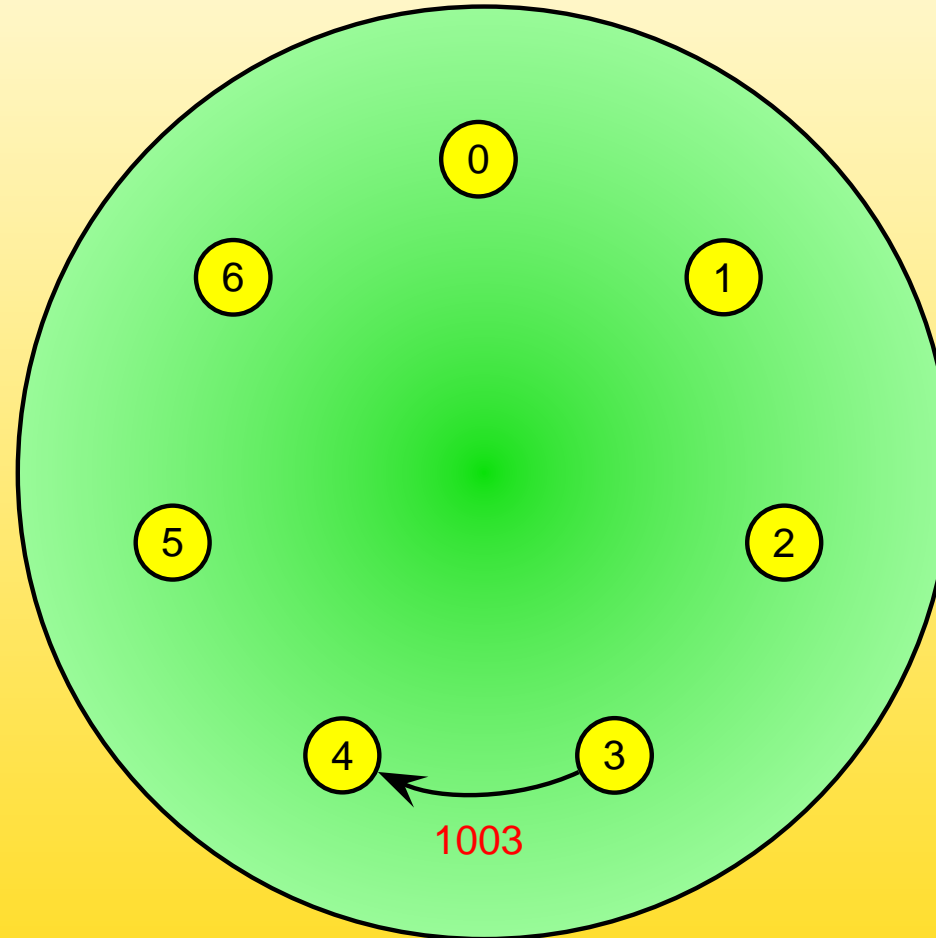


Figure 1: Communication ring

End of animation

## 2 – Communication ring

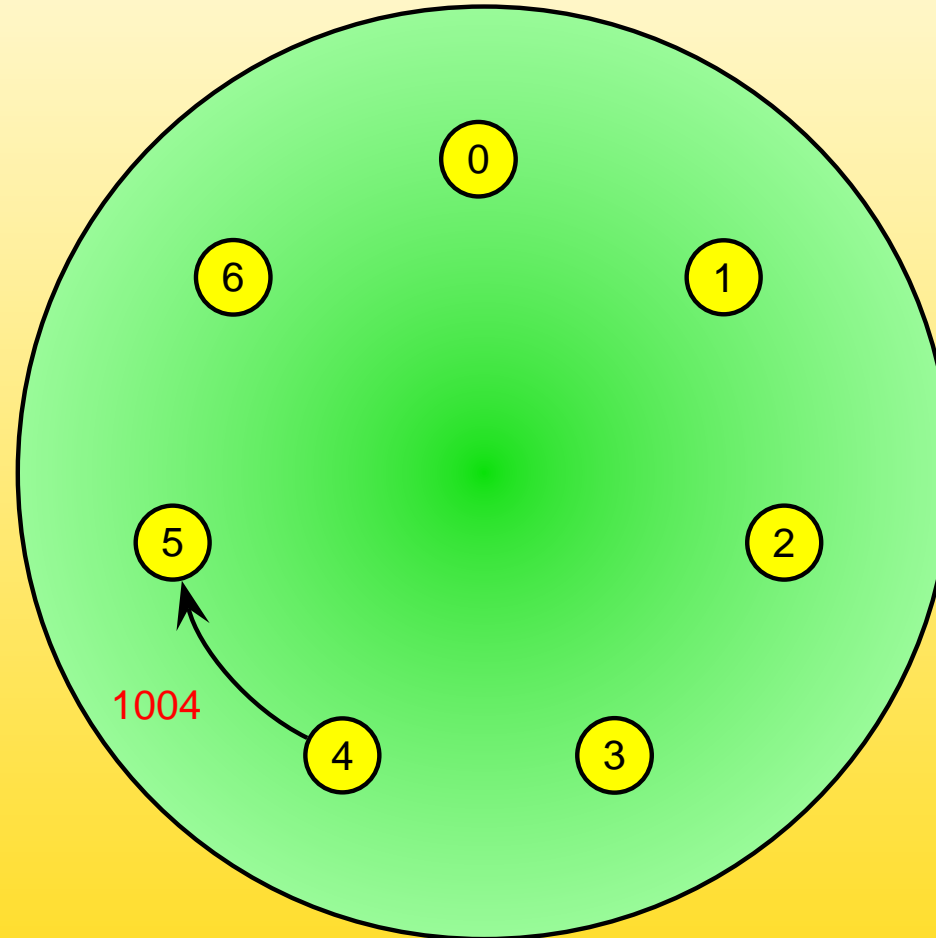


Figure 1: Communication ring

End of animation

## 2 – Communication ring

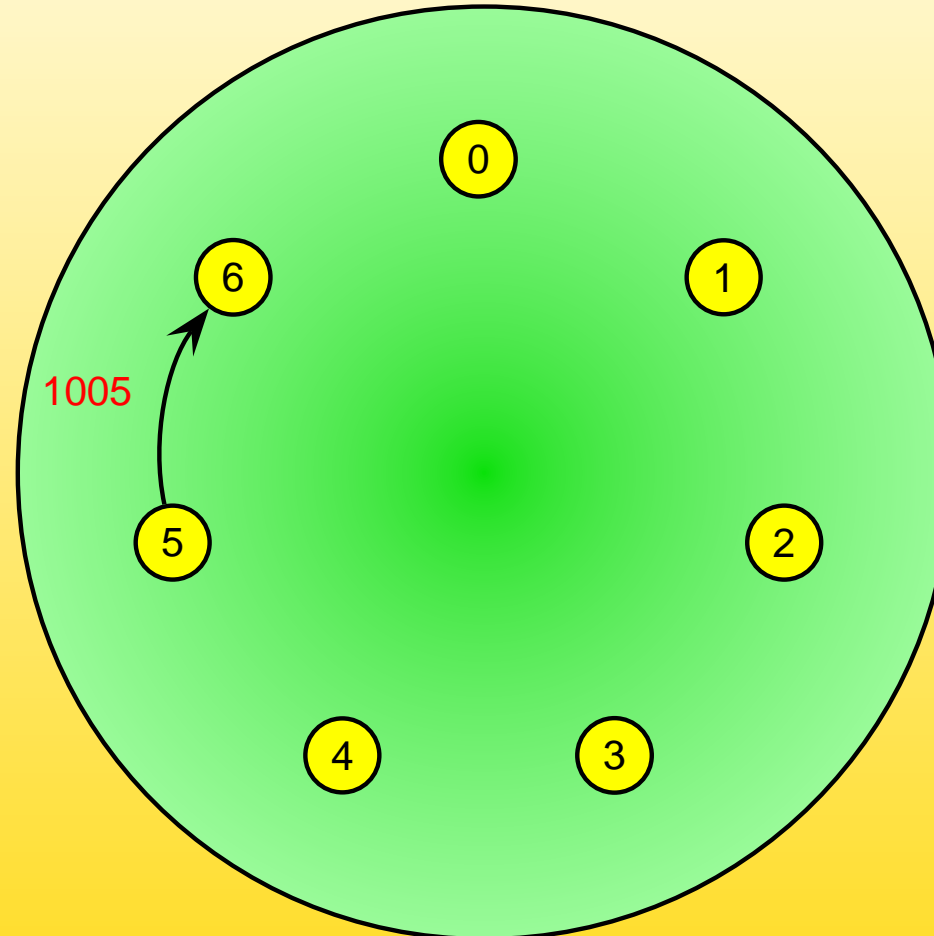


Figure 1: Communication ring

End of animation

## 2 – Communication ring

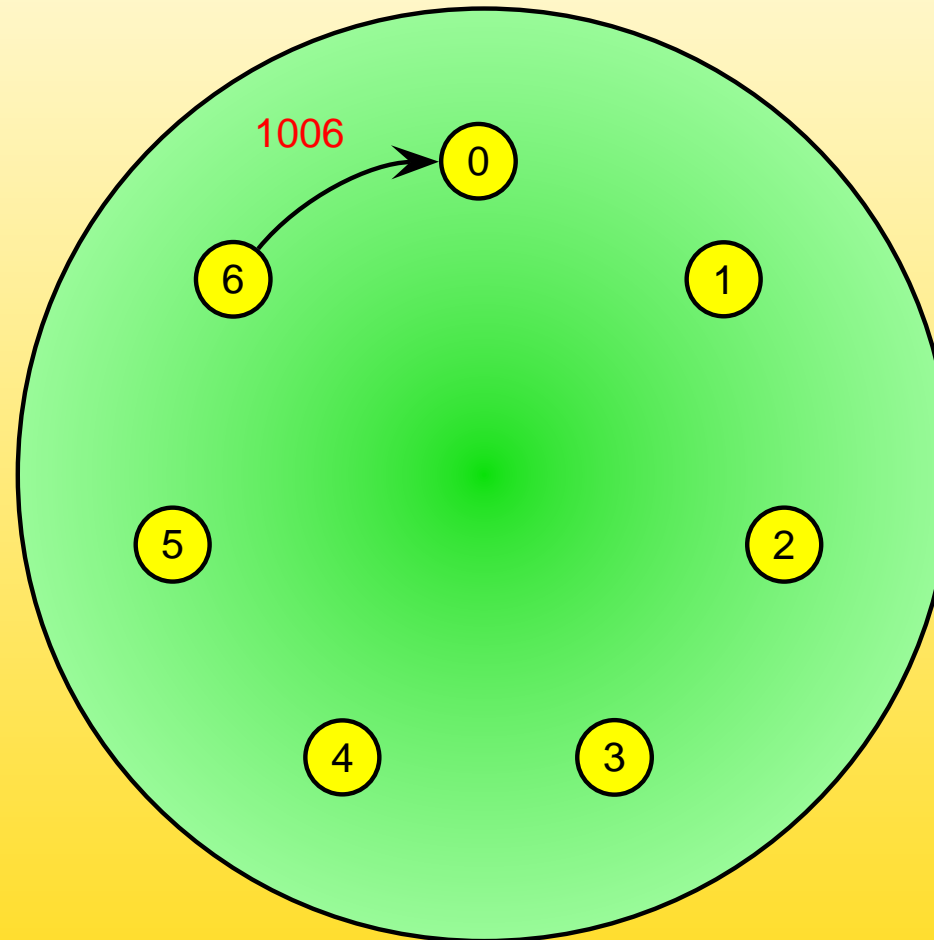


Figure 1: Communication ring

End of animation



## 3 – Commutative diagram

Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

$L$

Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

$$L \xleftarrow{i_1} L_r$$

Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

$$L \xleftarrow{i_1} L_r \xrightarrow{r} R$$

Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

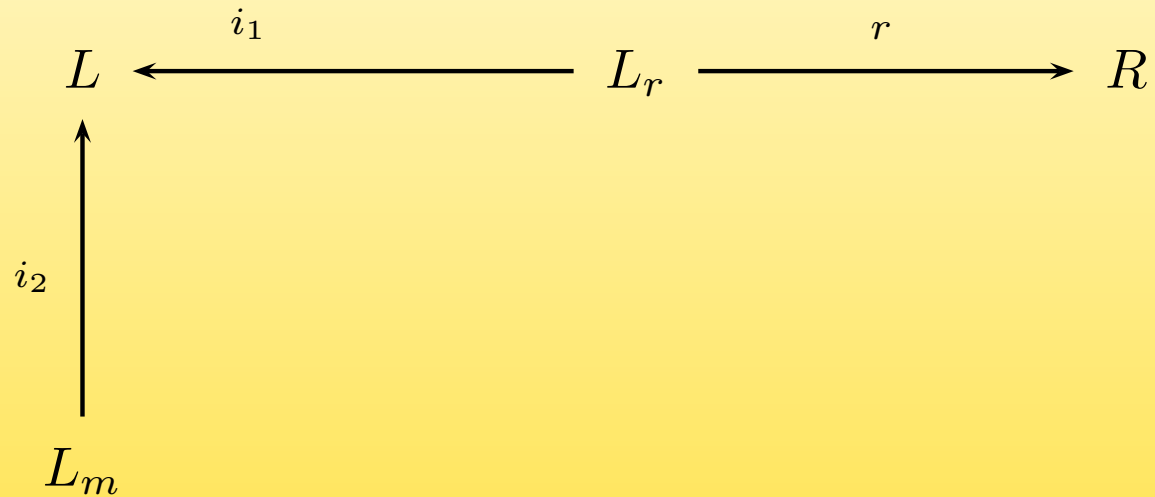


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

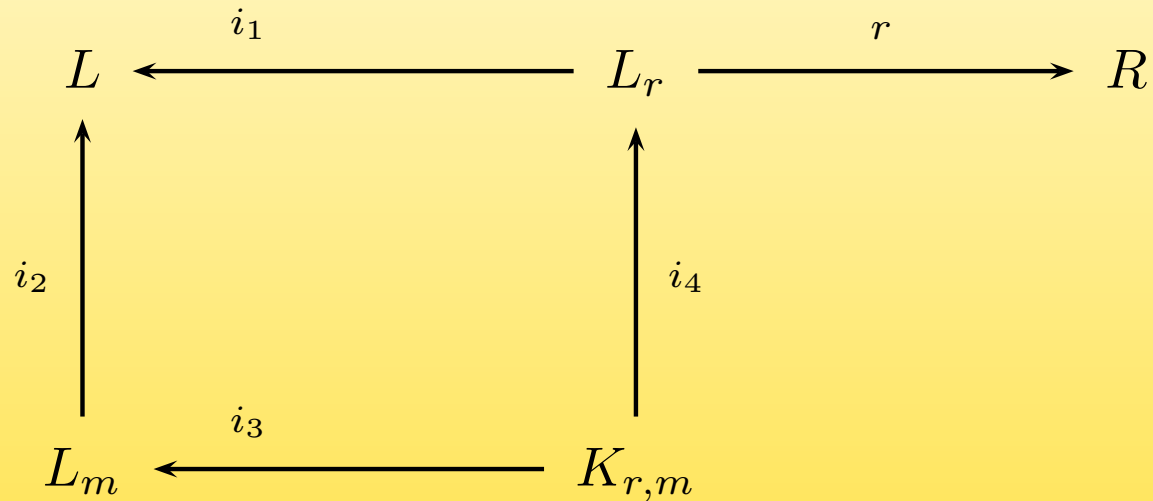


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

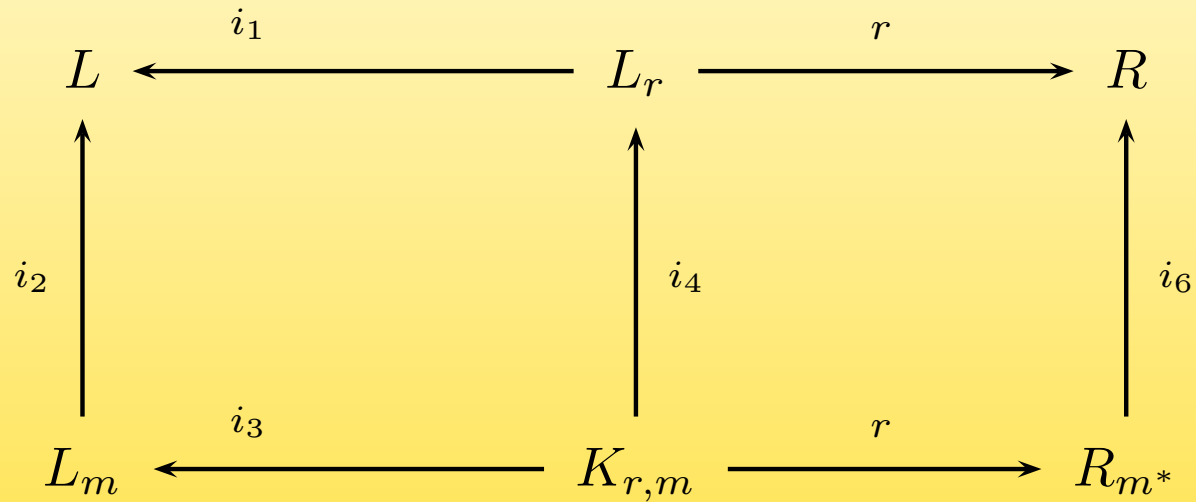


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

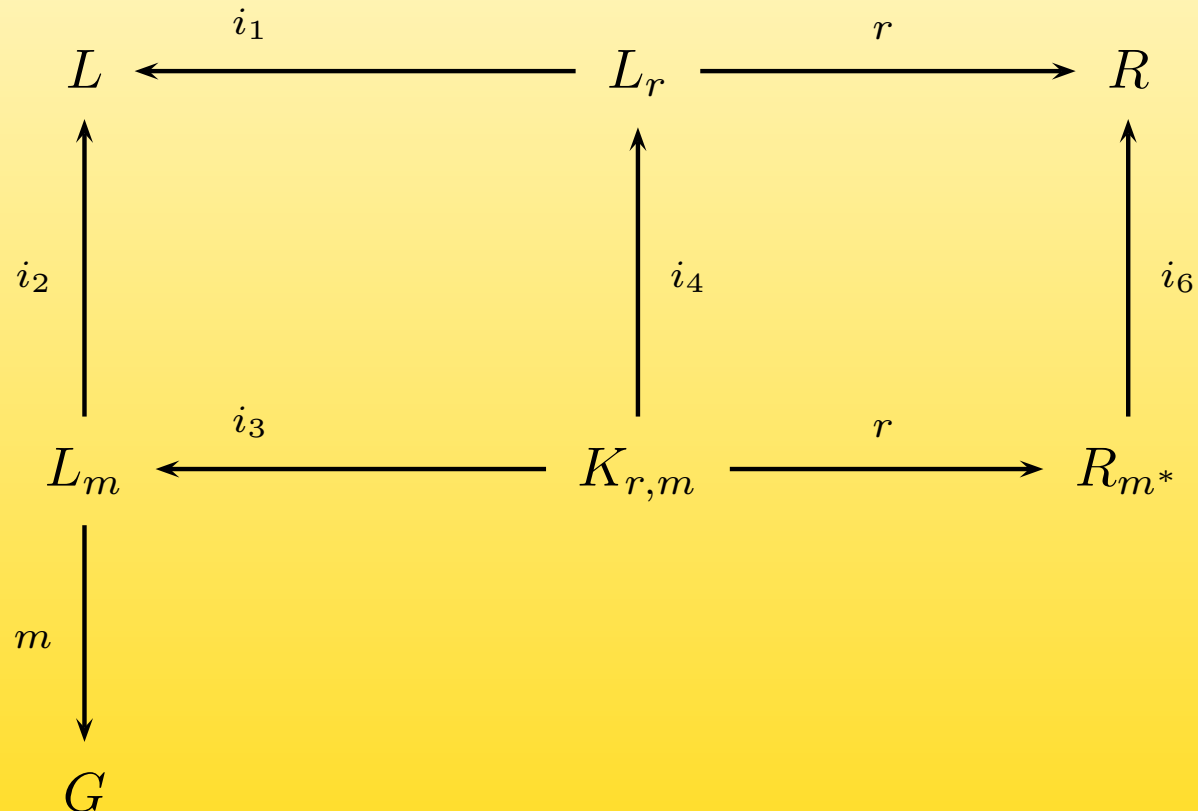


Figure 2: Commutative diagram

End of animation



## 3 – Commutative diagram

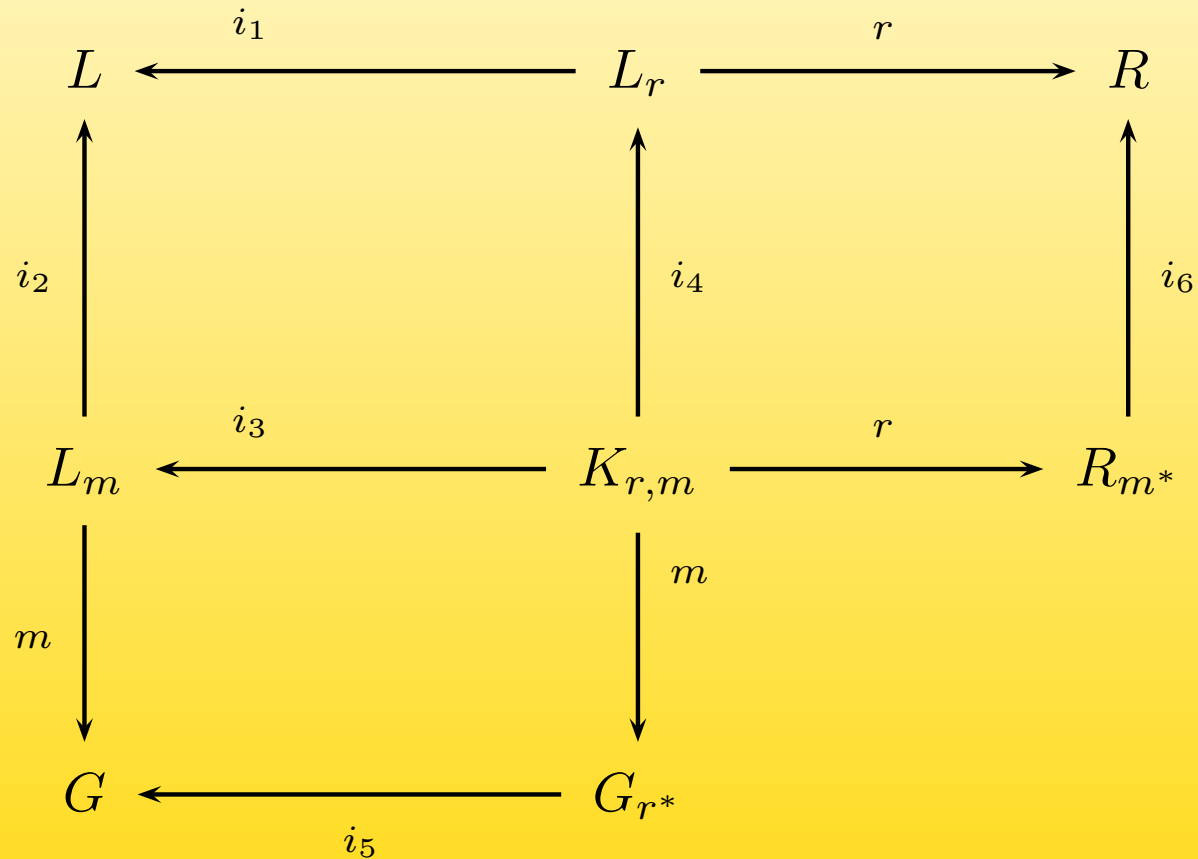


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

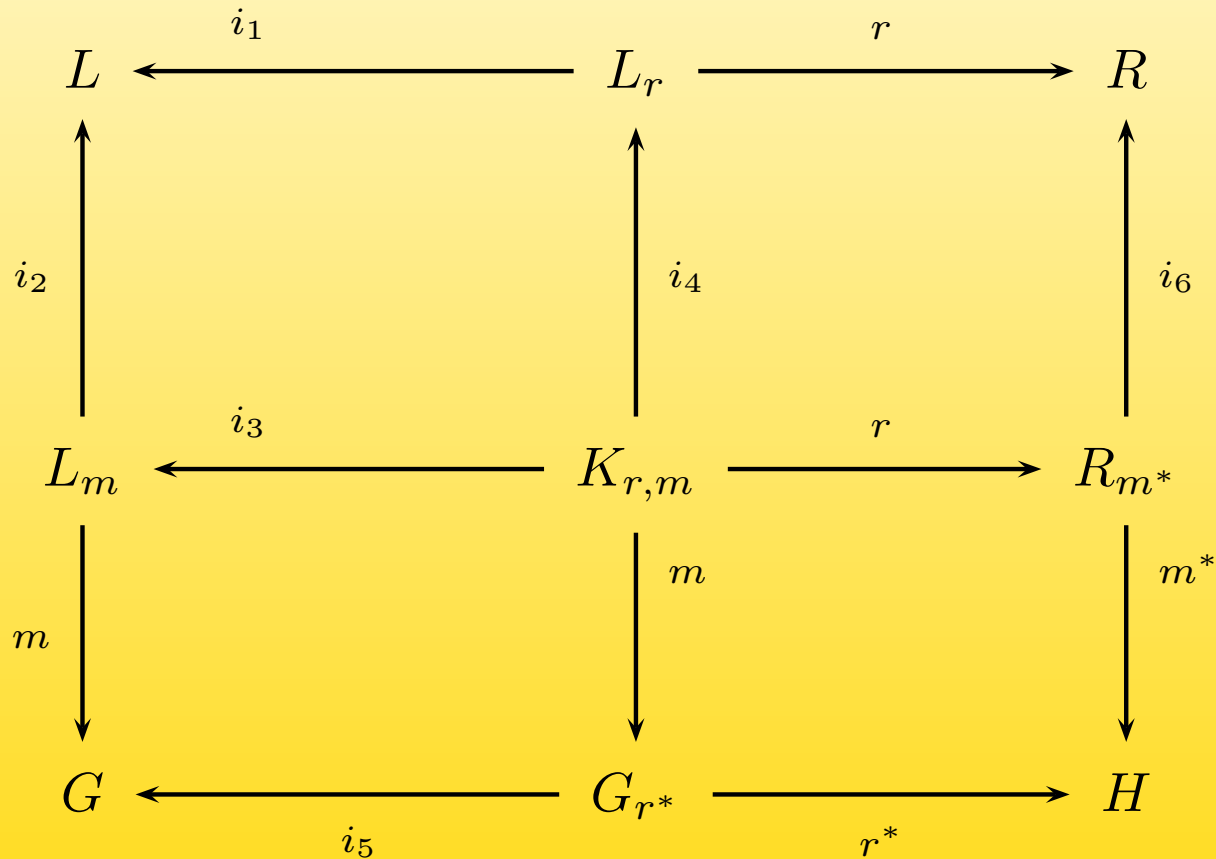


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

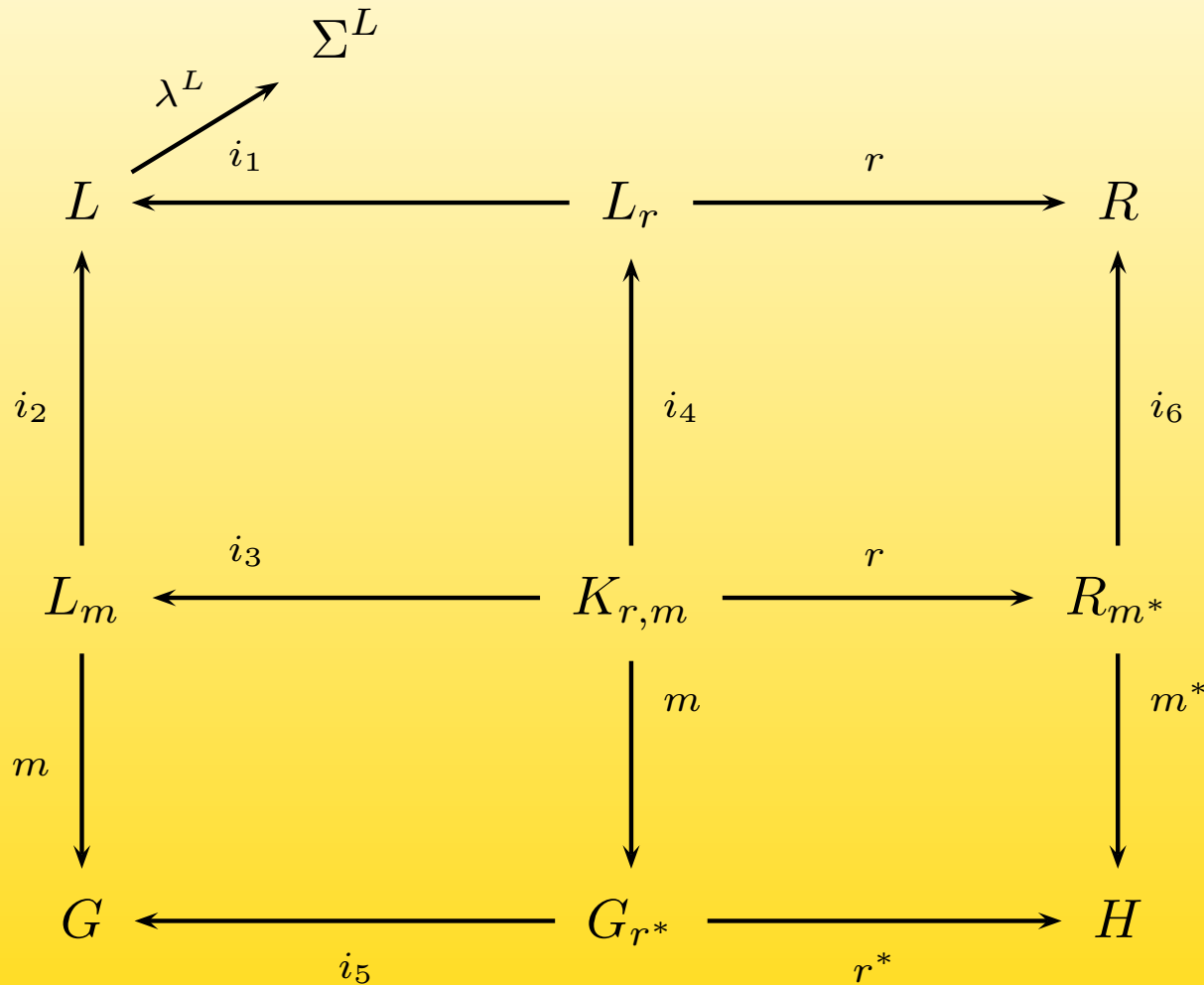


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

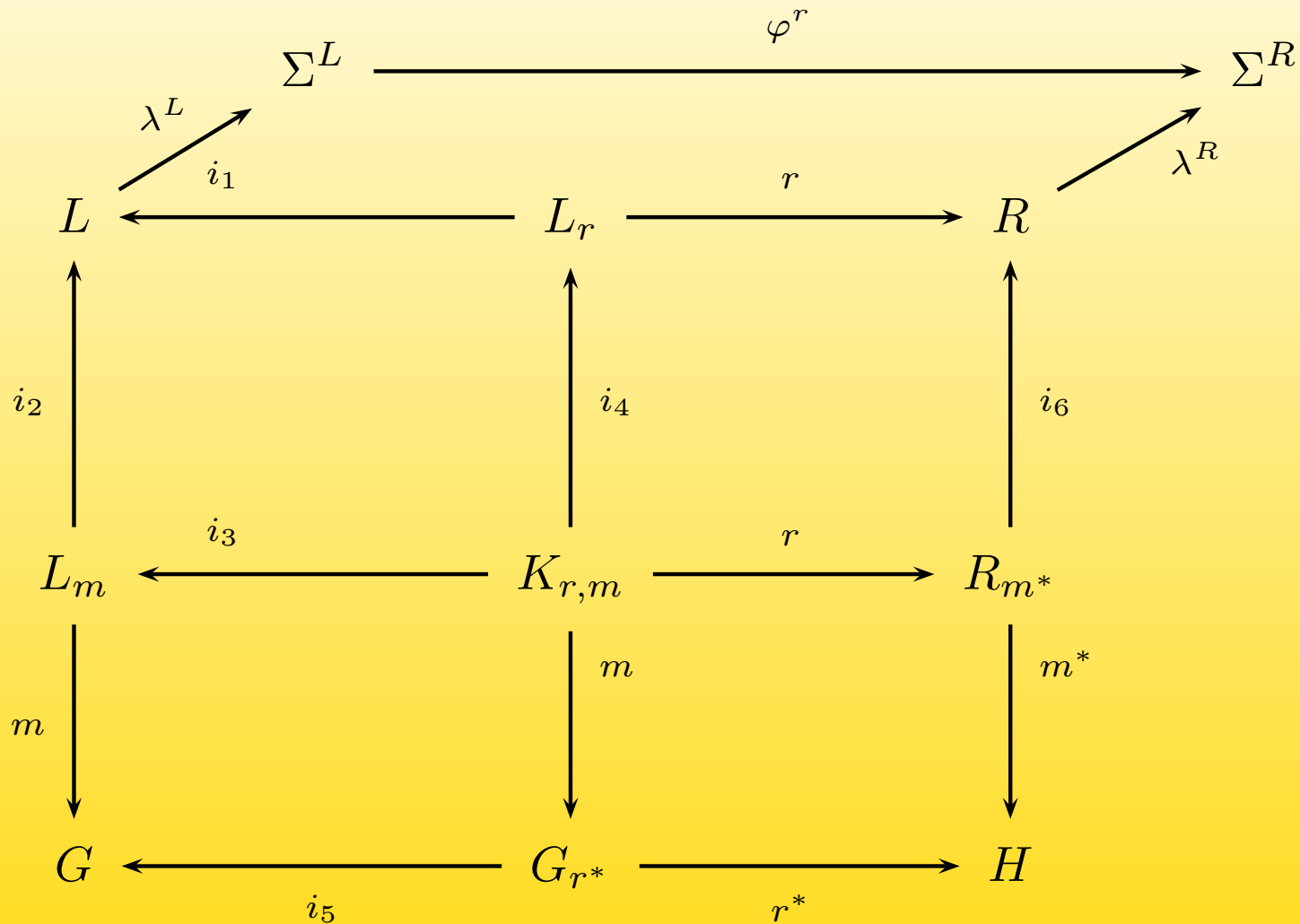


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

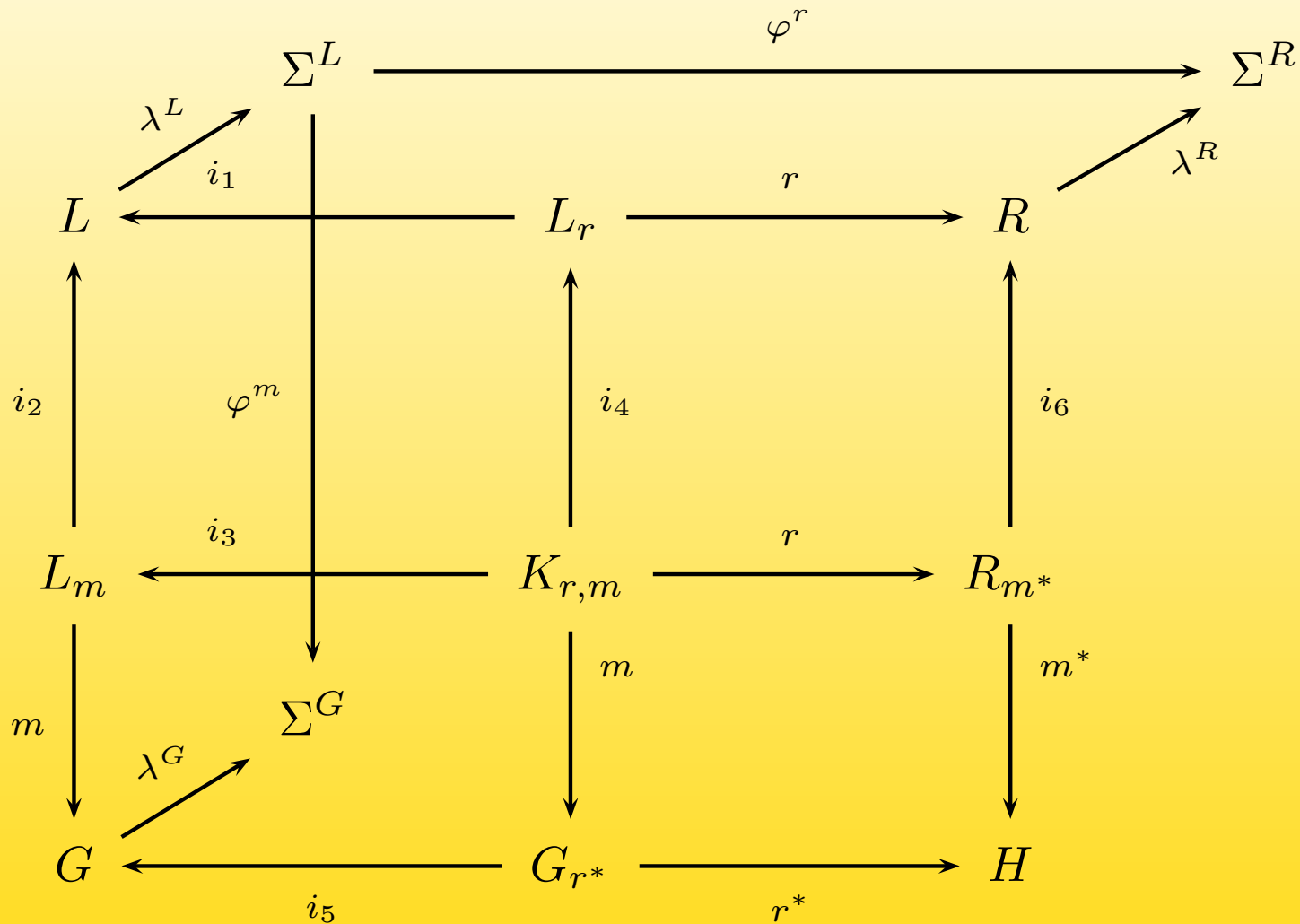


Figure 2: Commutative diagram

End of animation

## 3 – Commutative diagram

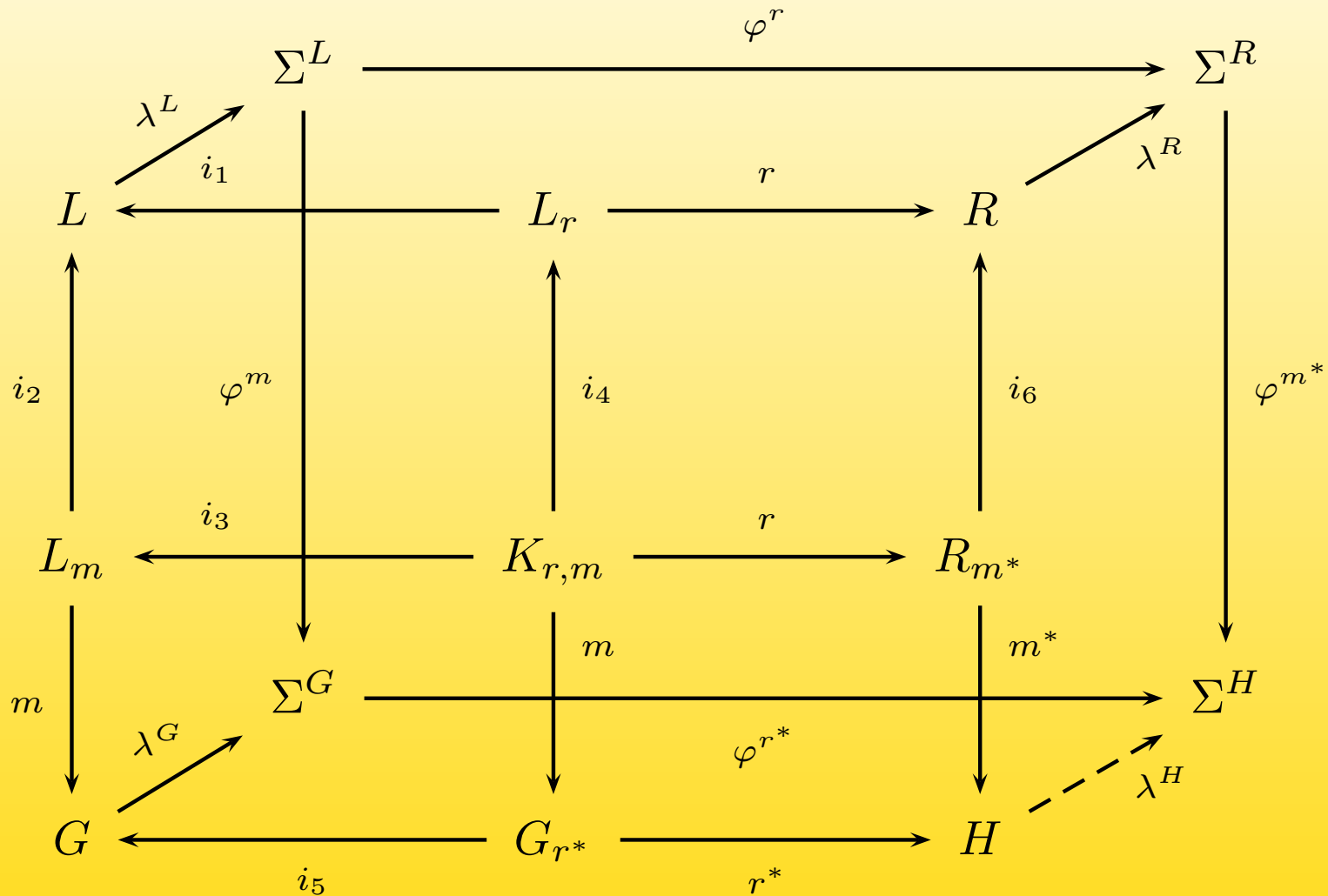
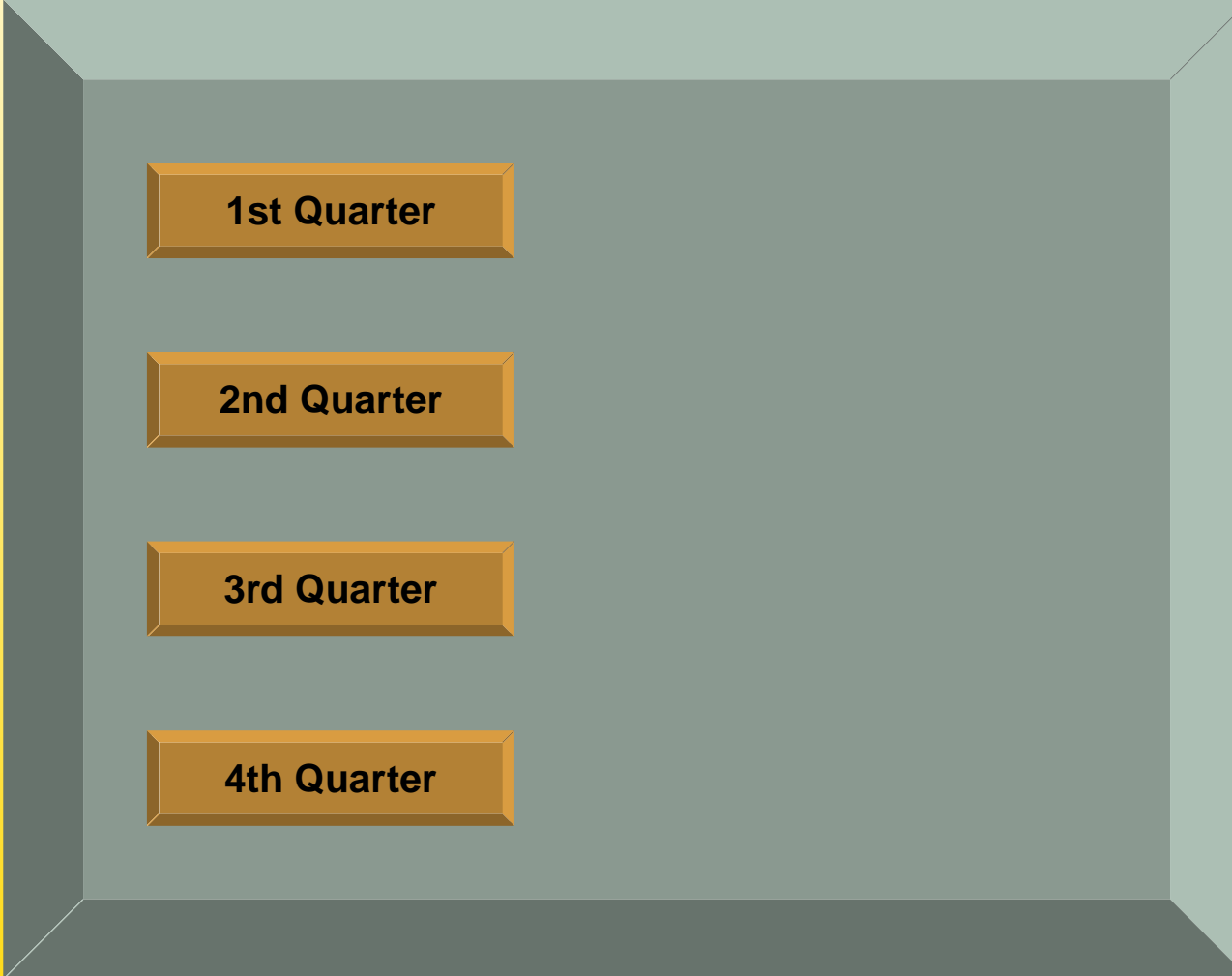


Figure 2: Commutative diagram

End of animation

## 4 – Results of the year

Table 1: Results of the year

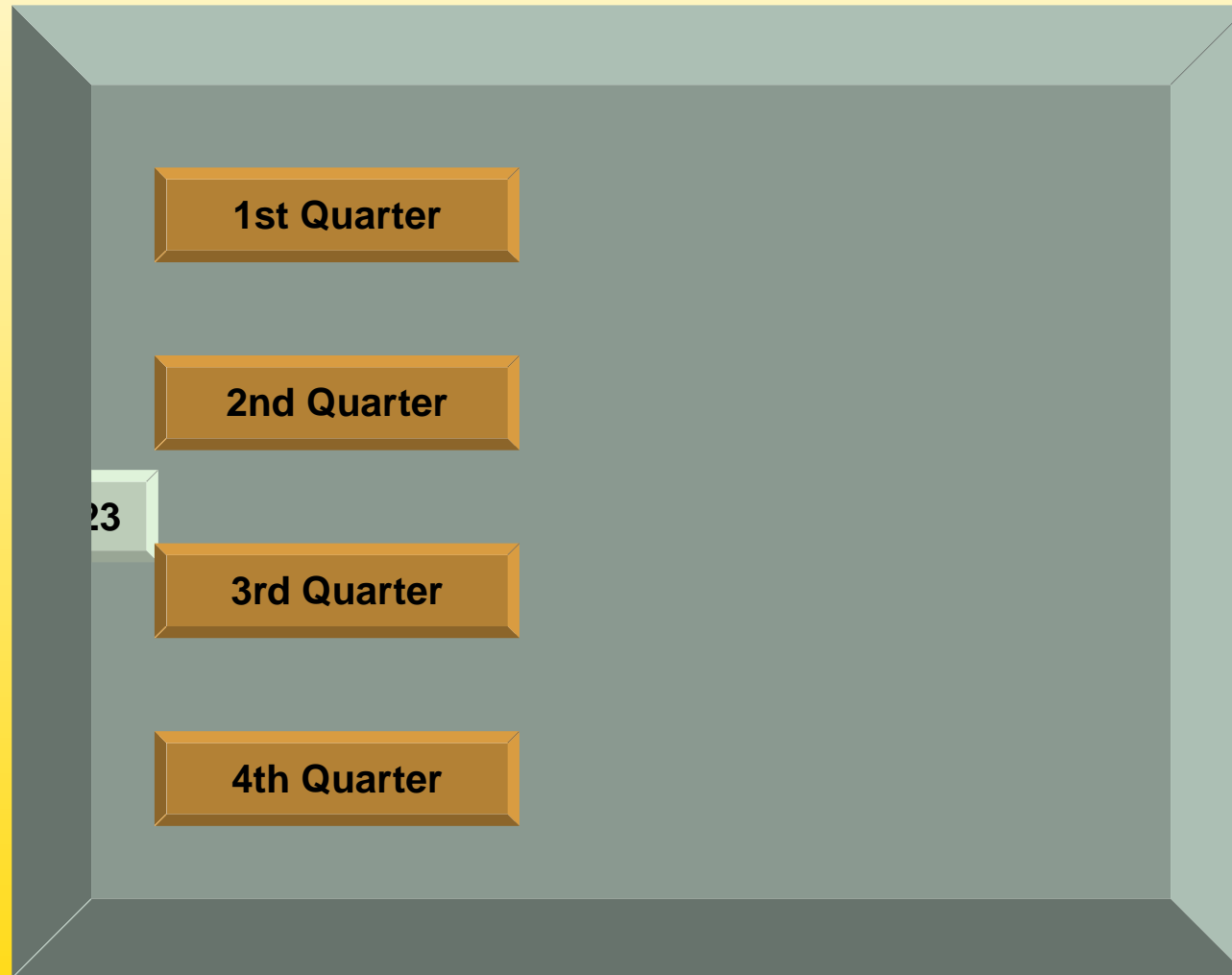


1st Quarter
2nd Quarter
3rd Quarter
4th Quarter

End of animation

## 4 – Results of the year

Table 1: Results of the year

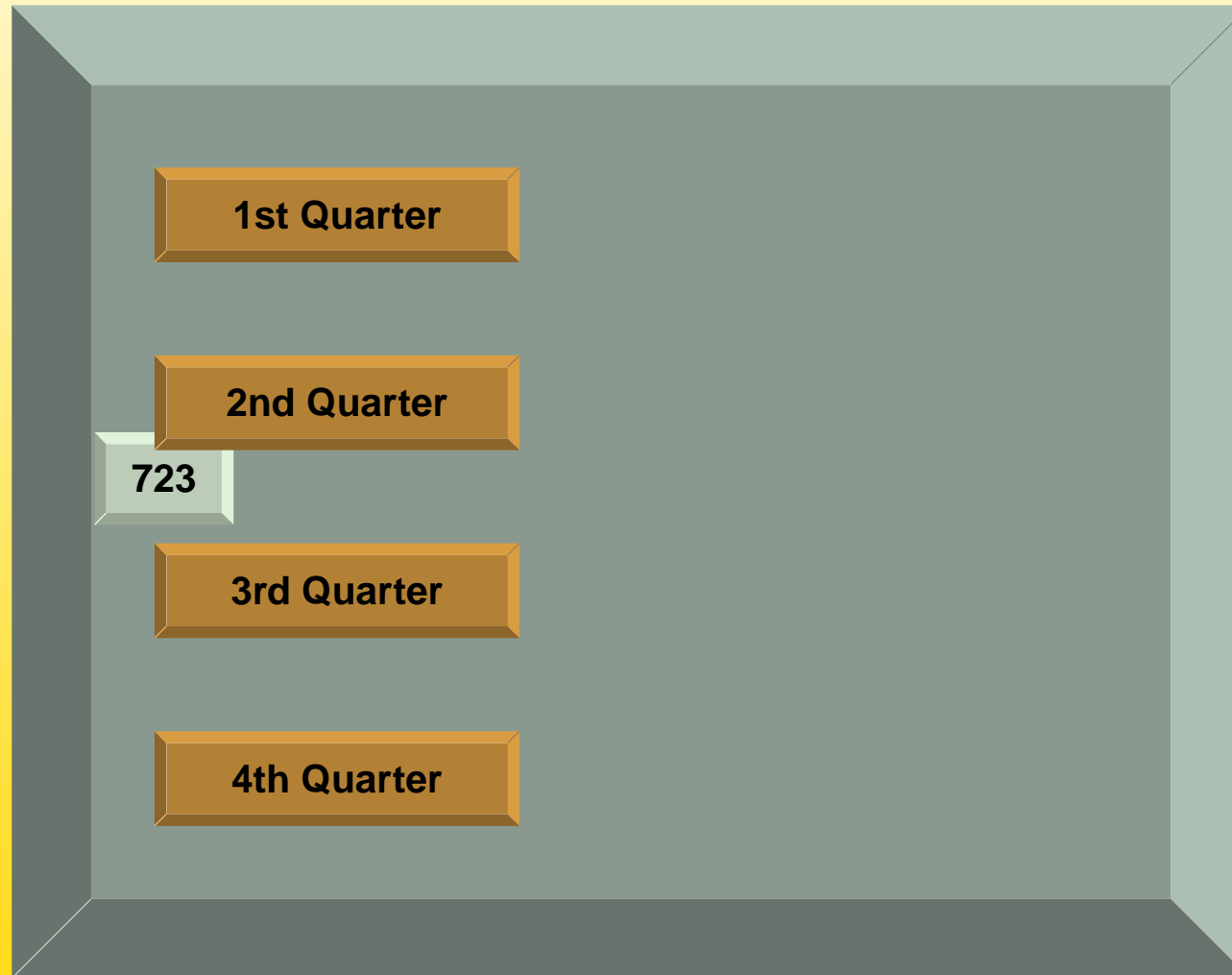


End of animation



## 4 – Results of the year

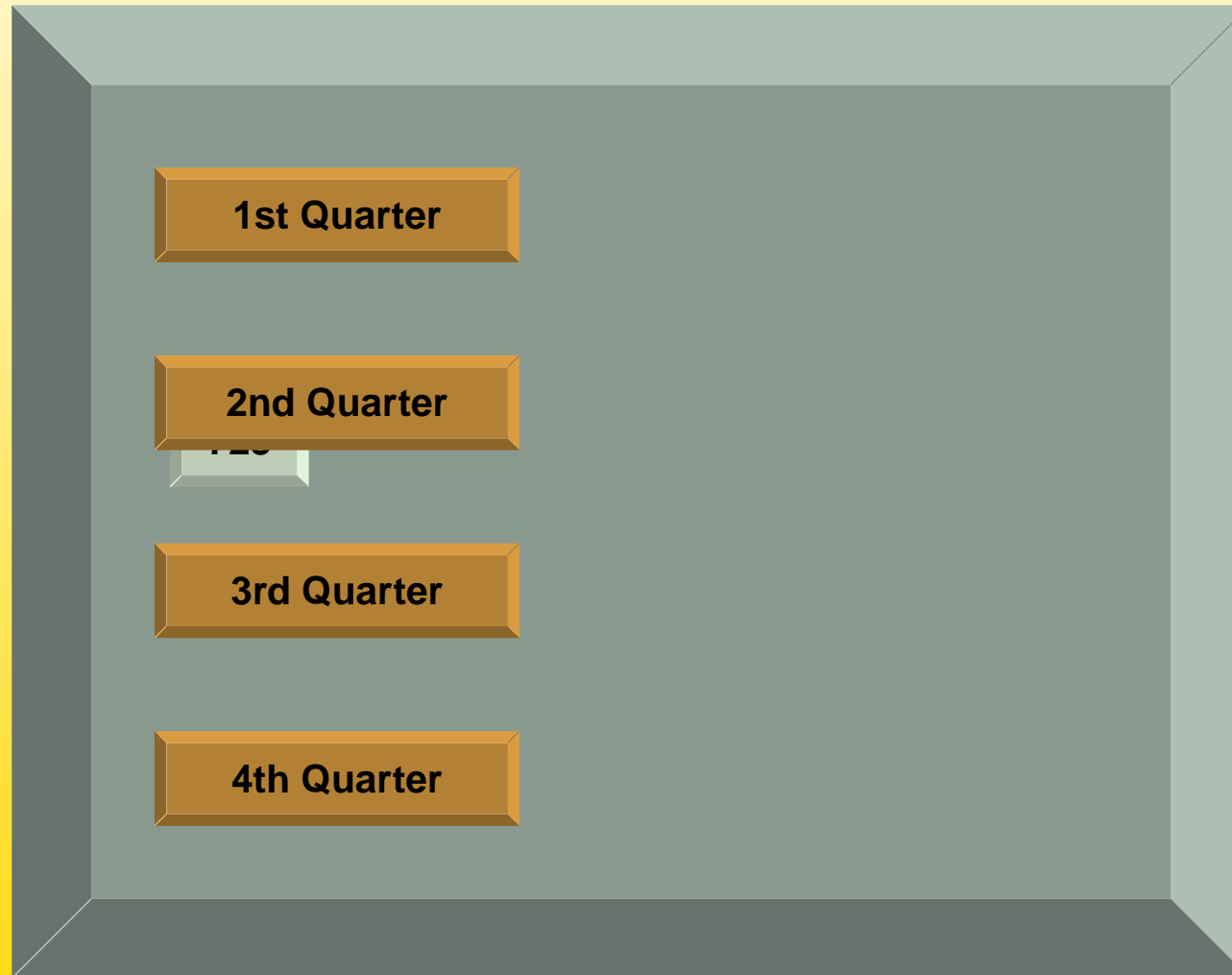
Table 1: Results of the year



End of animation

## 4 – Results of the year

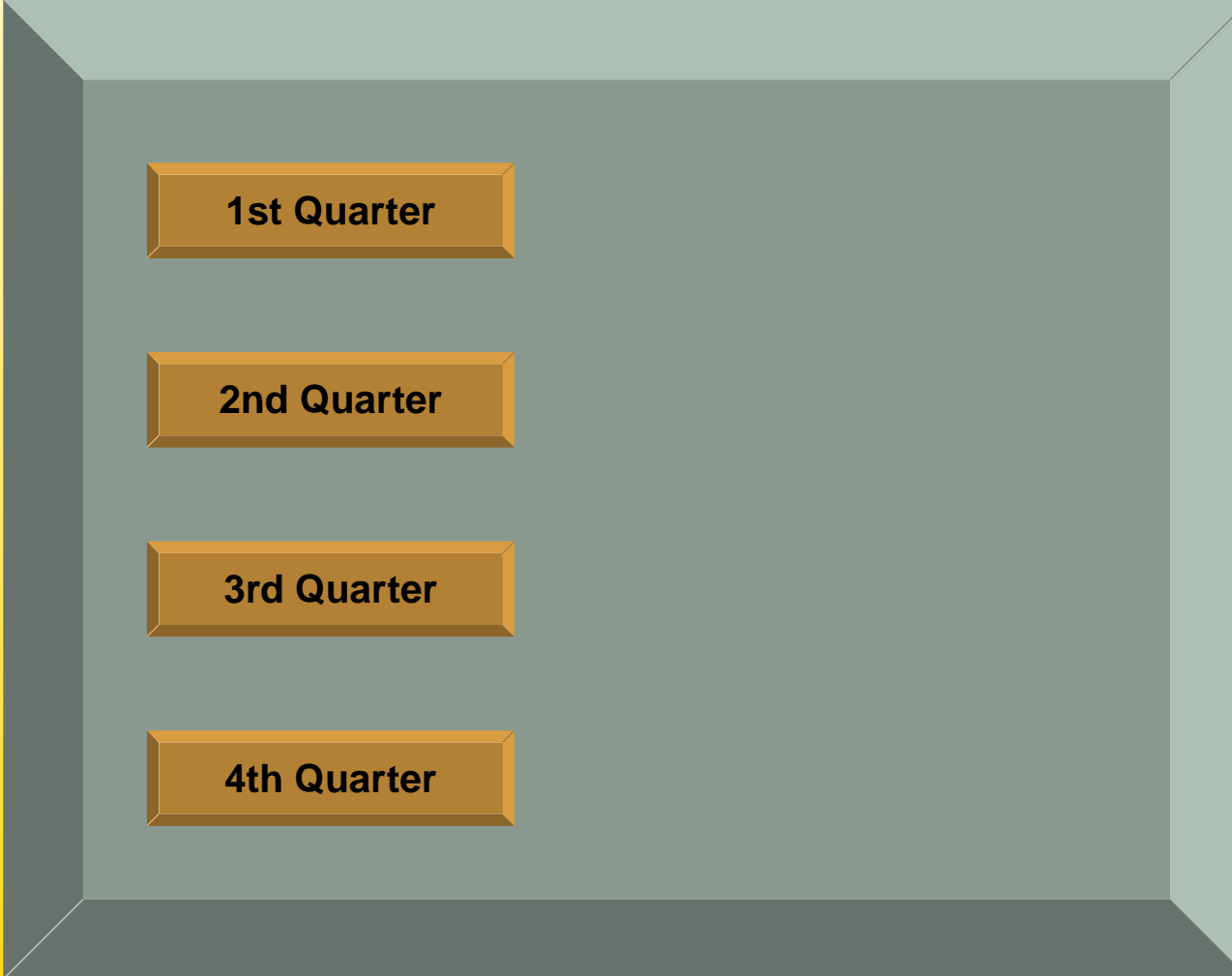
Table 1: Results of the year



End of animation

## 4 – Results of the year

Table 1: Results of the year

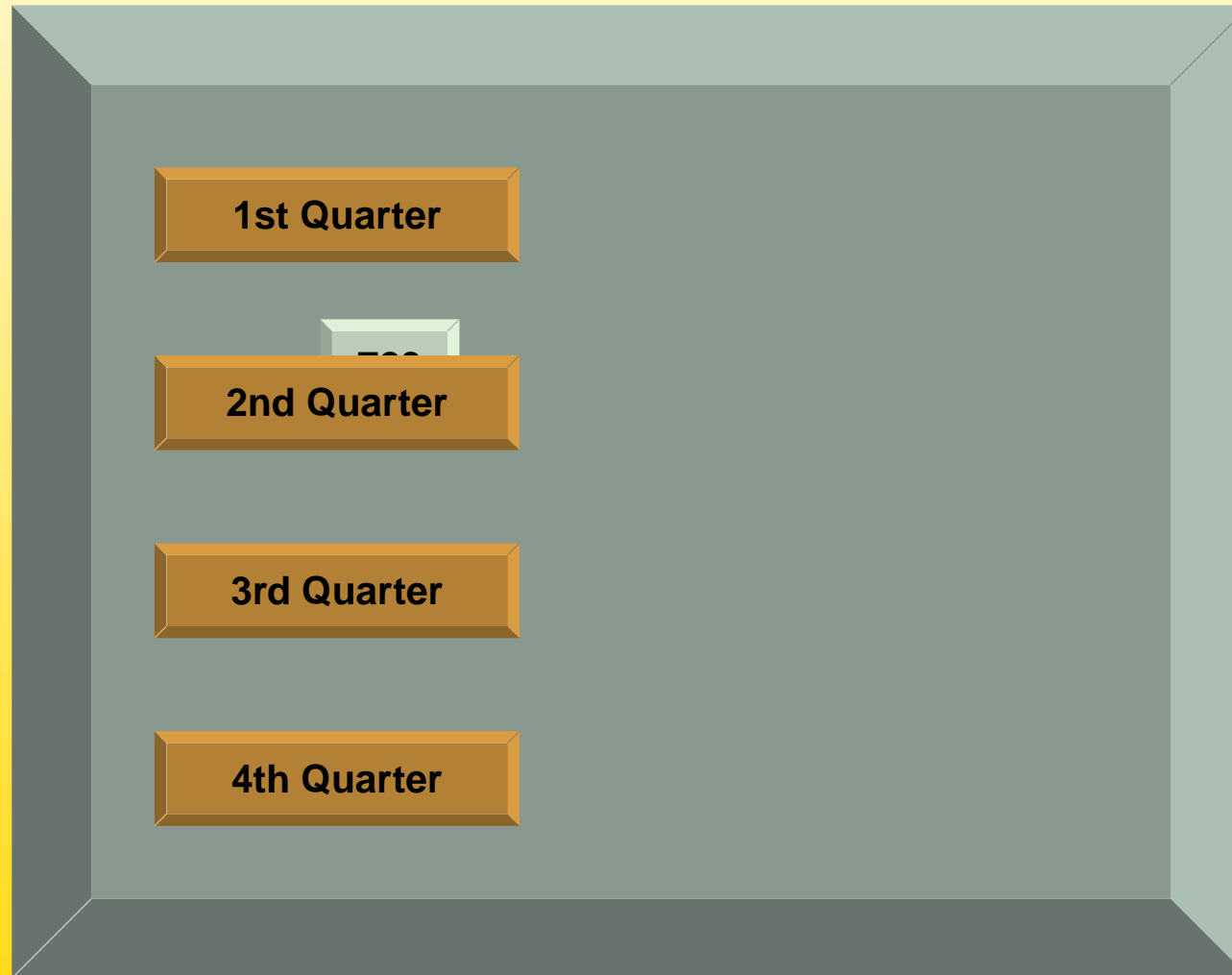


1st Quarter
2nd Quarter
3rd Quarter
4th Quarter

End of animation

## 4 – Results of the year

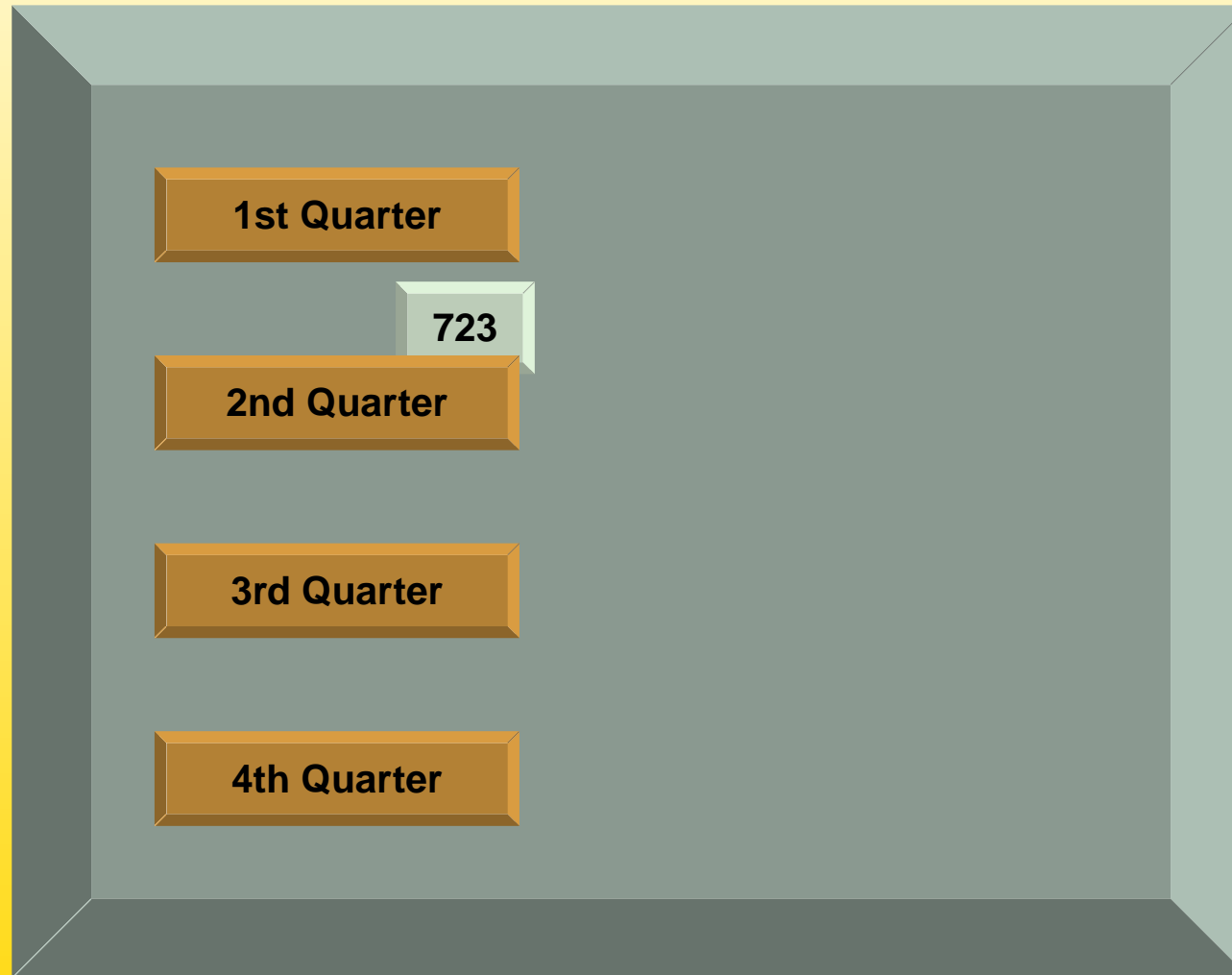
Table 1: Results of the year



End of animation

## 4 – Results of the year

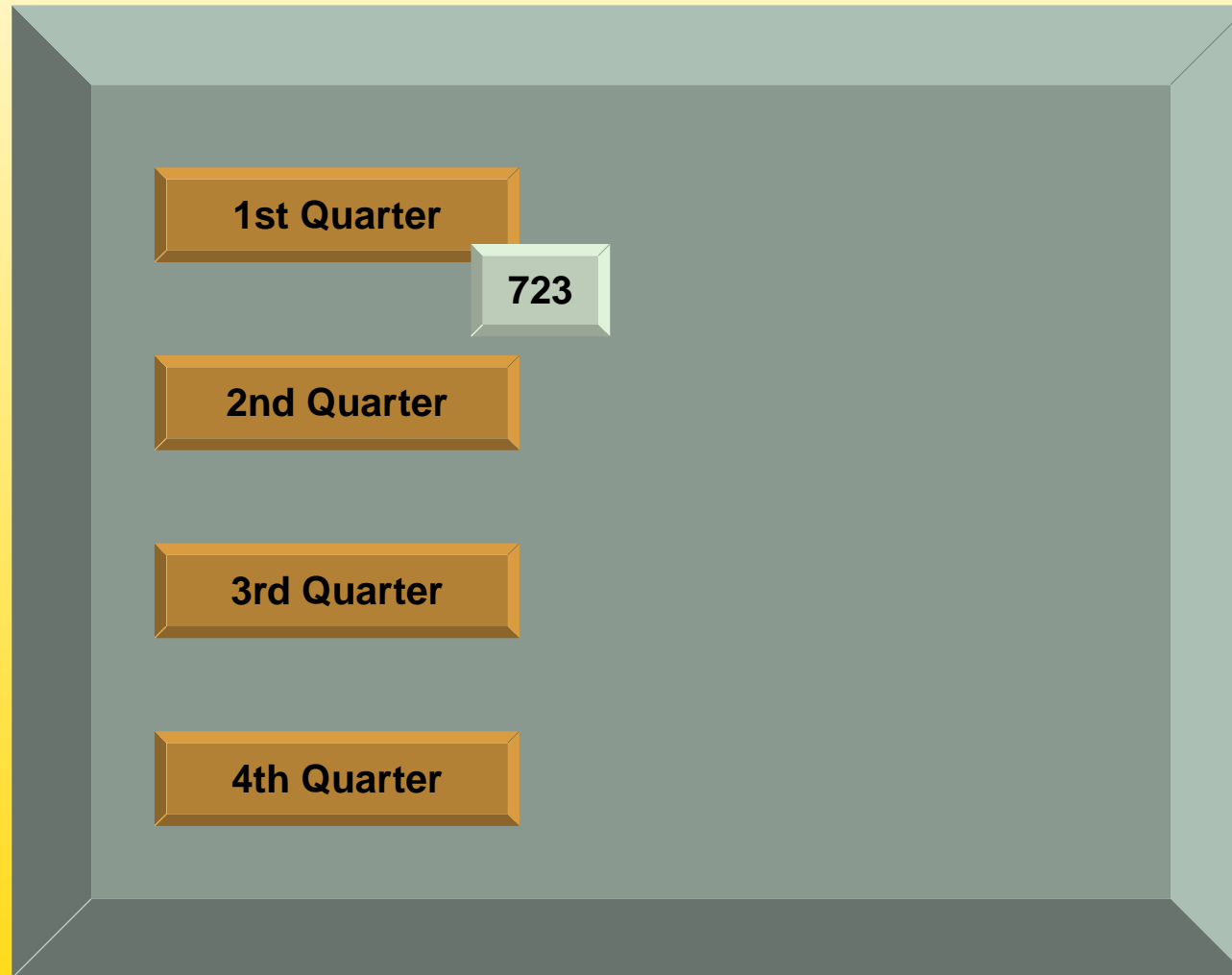
Table 1: Results of the year



End of animation

## 4 – Results of the year

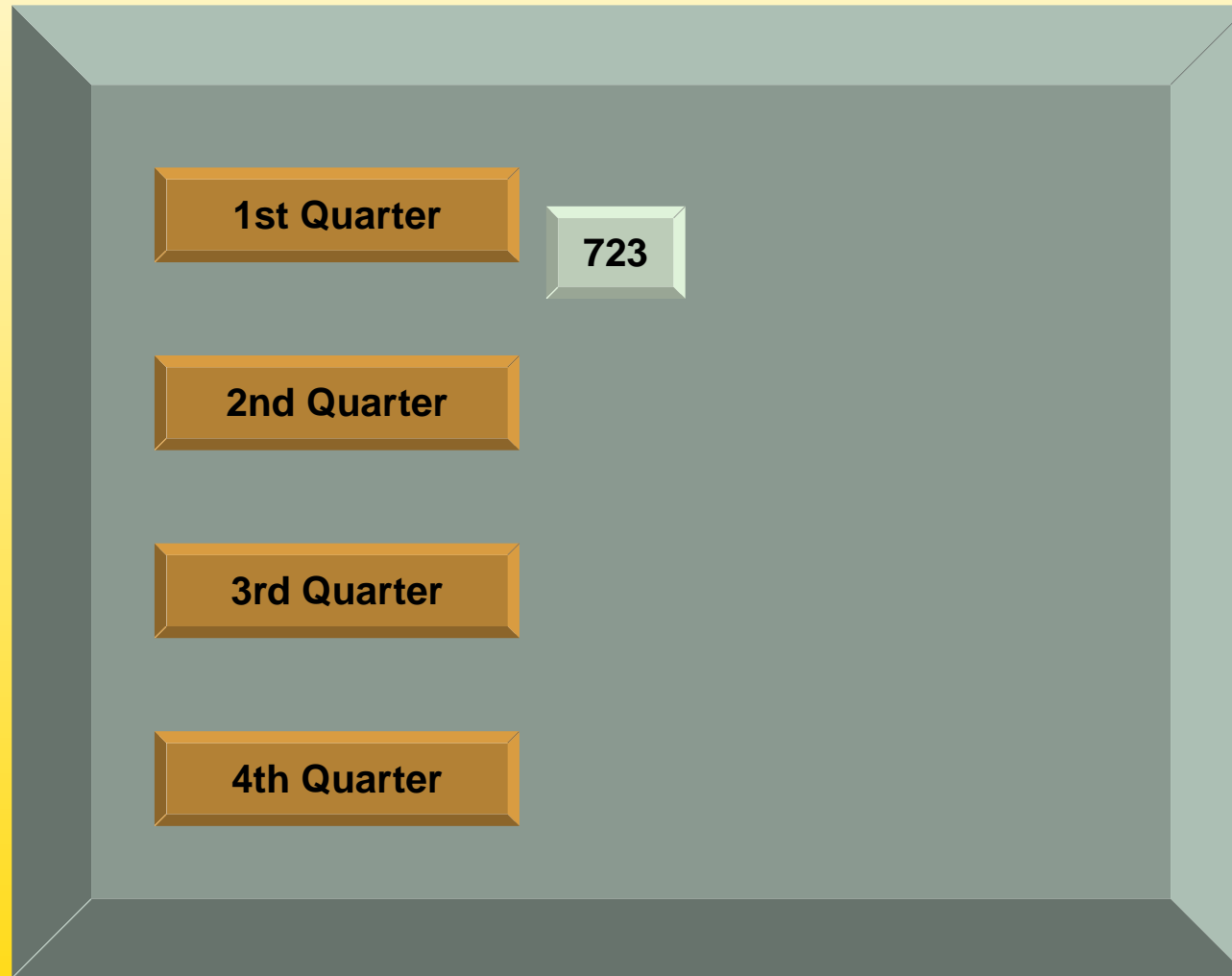
Table 1: Results of the year



End of animation

## 4 – Results of the year

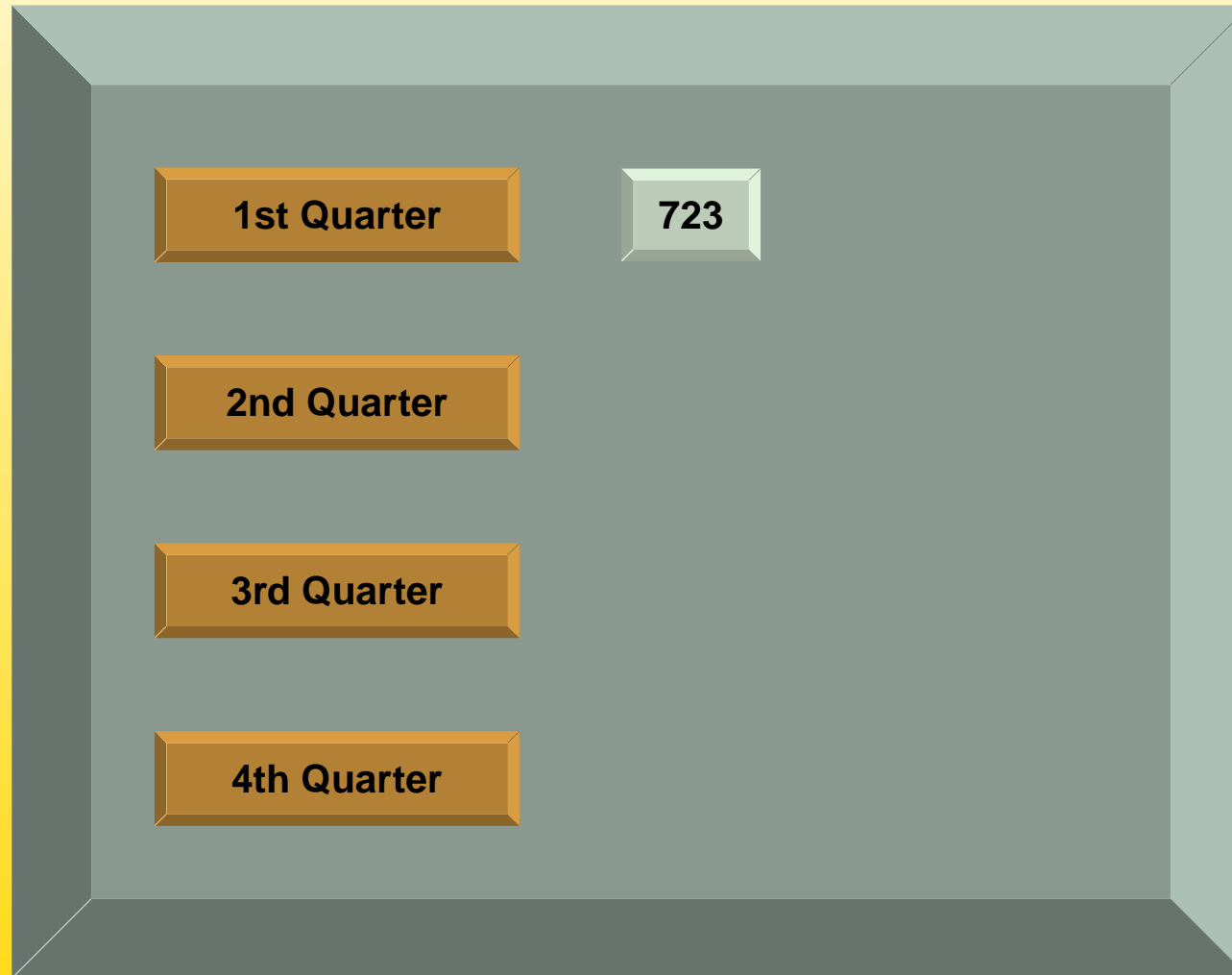
Table 1: Results of the year



End of animation

## 4 – Results of the year

Table 1: Results of the year

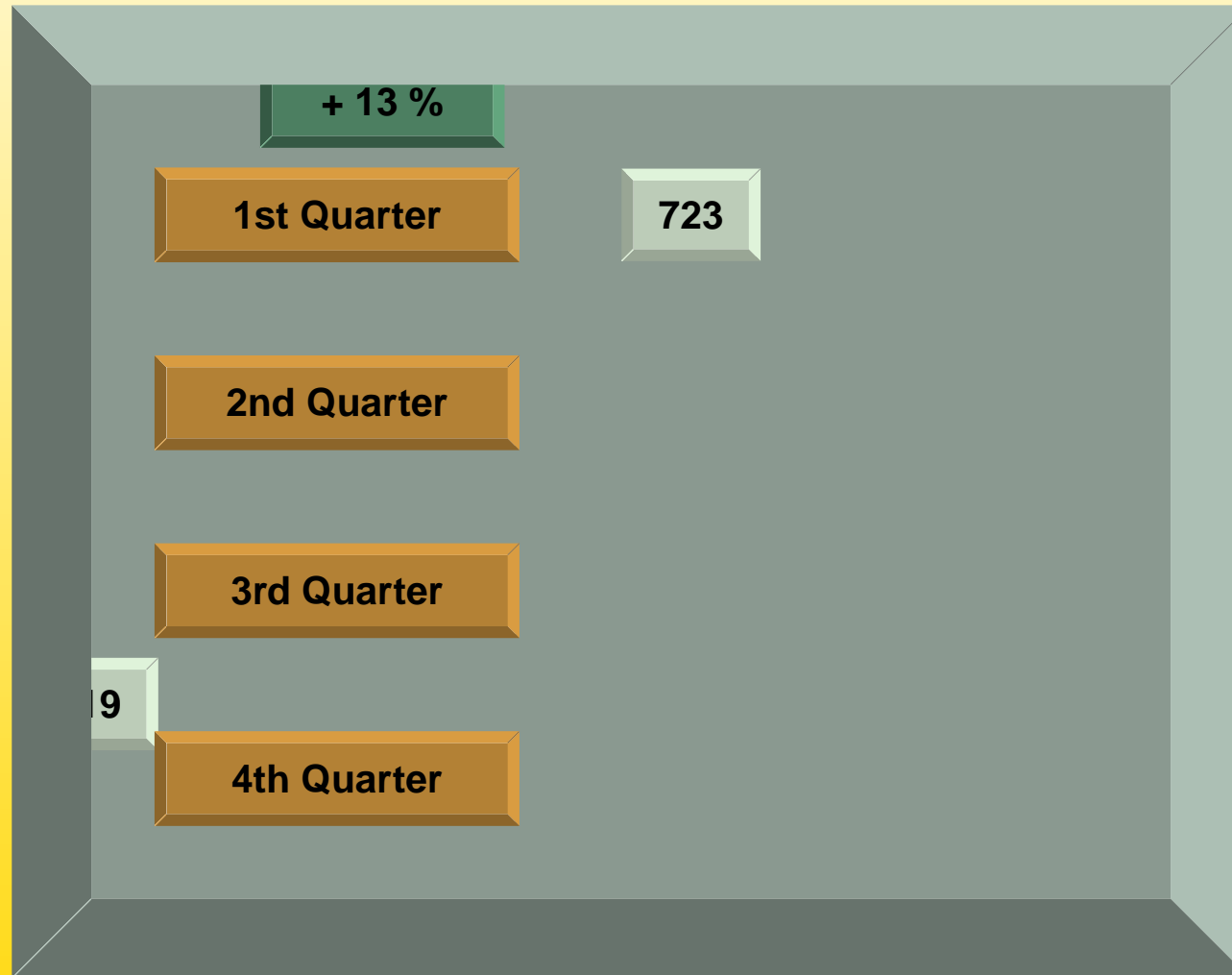


End of animation



## 4 – Results of the year

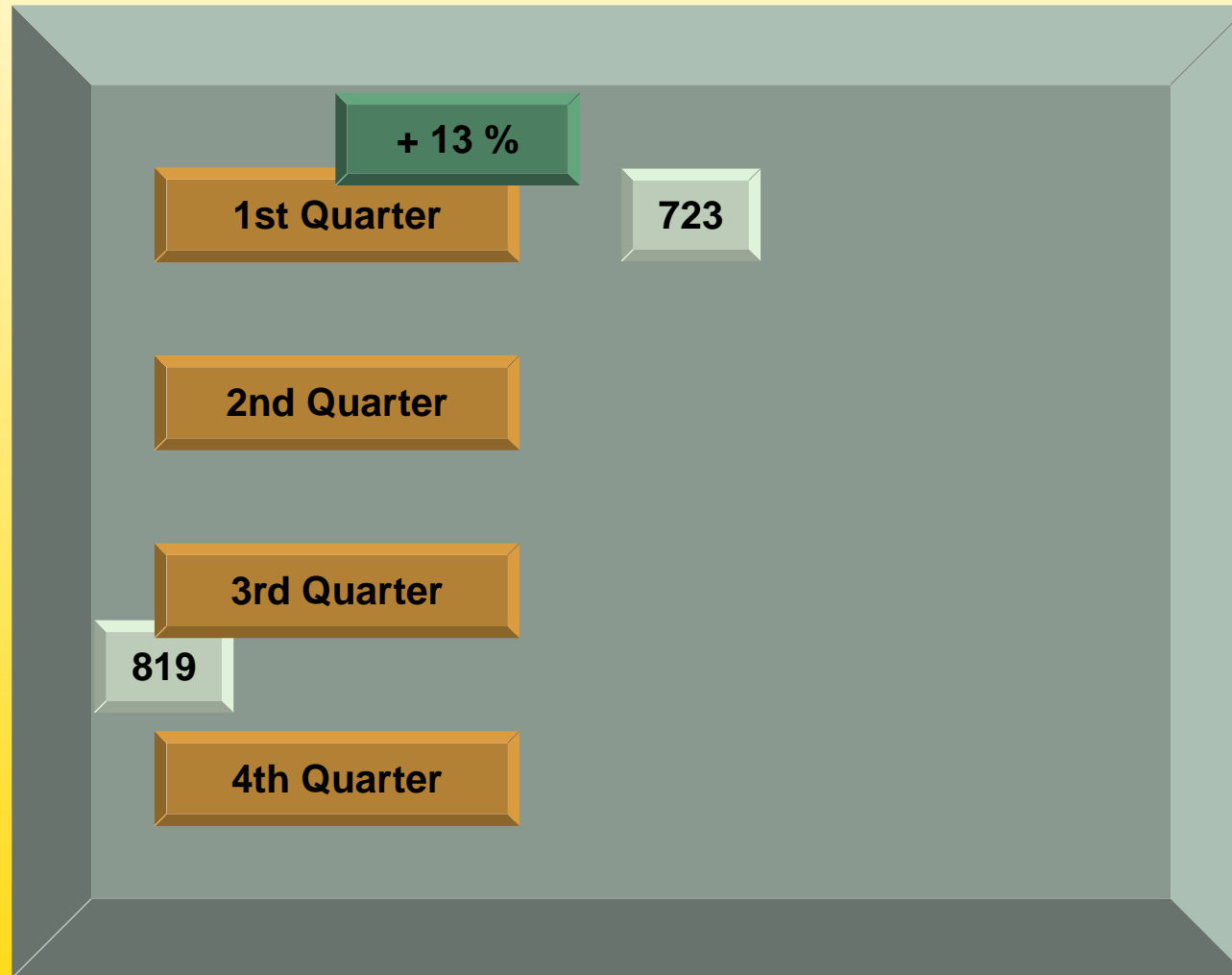
Table 1: Results of the year



End of animation

## 4 – Results of the year

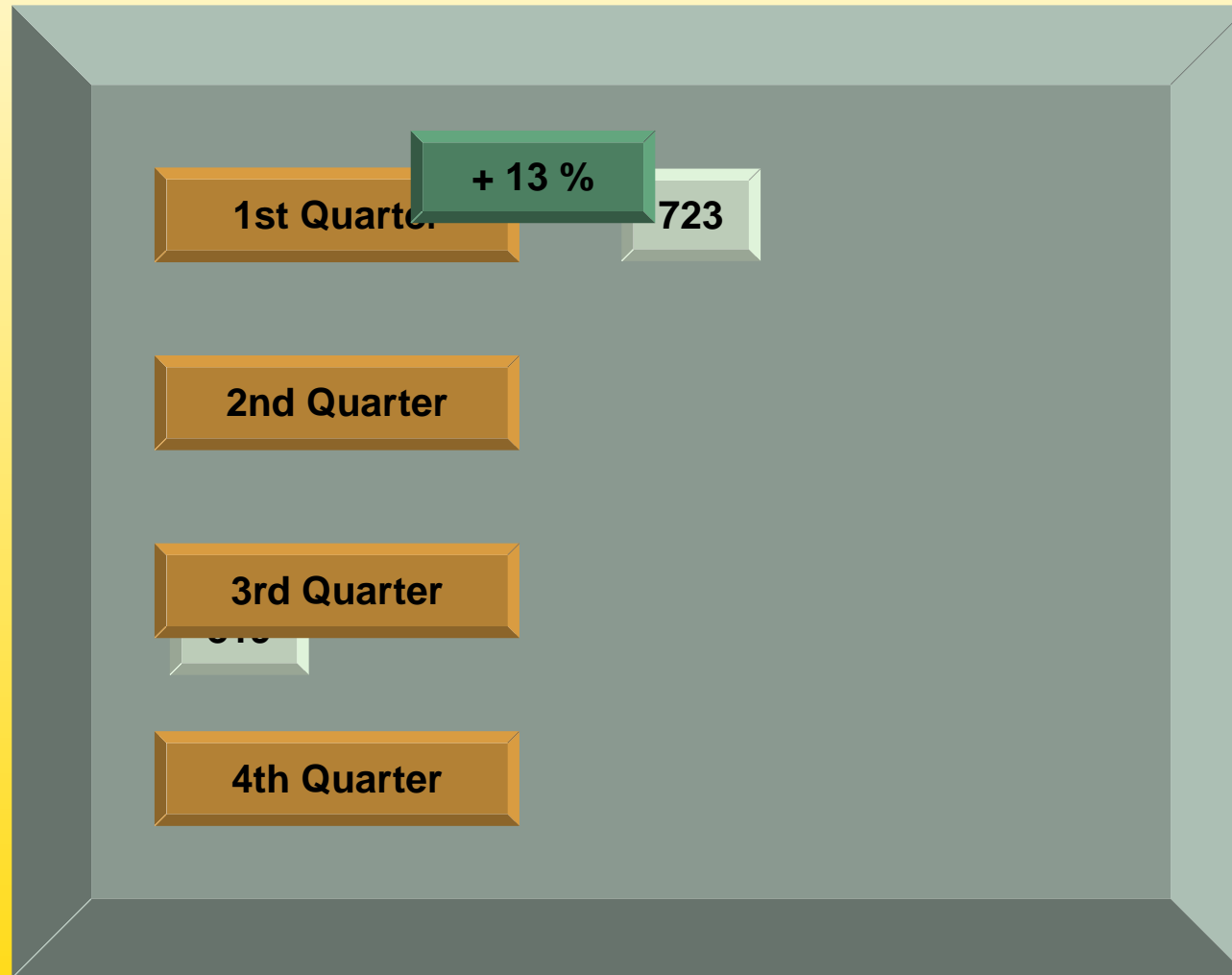
Table 1: Results of the year



End of animation

## 4 – Results of the year

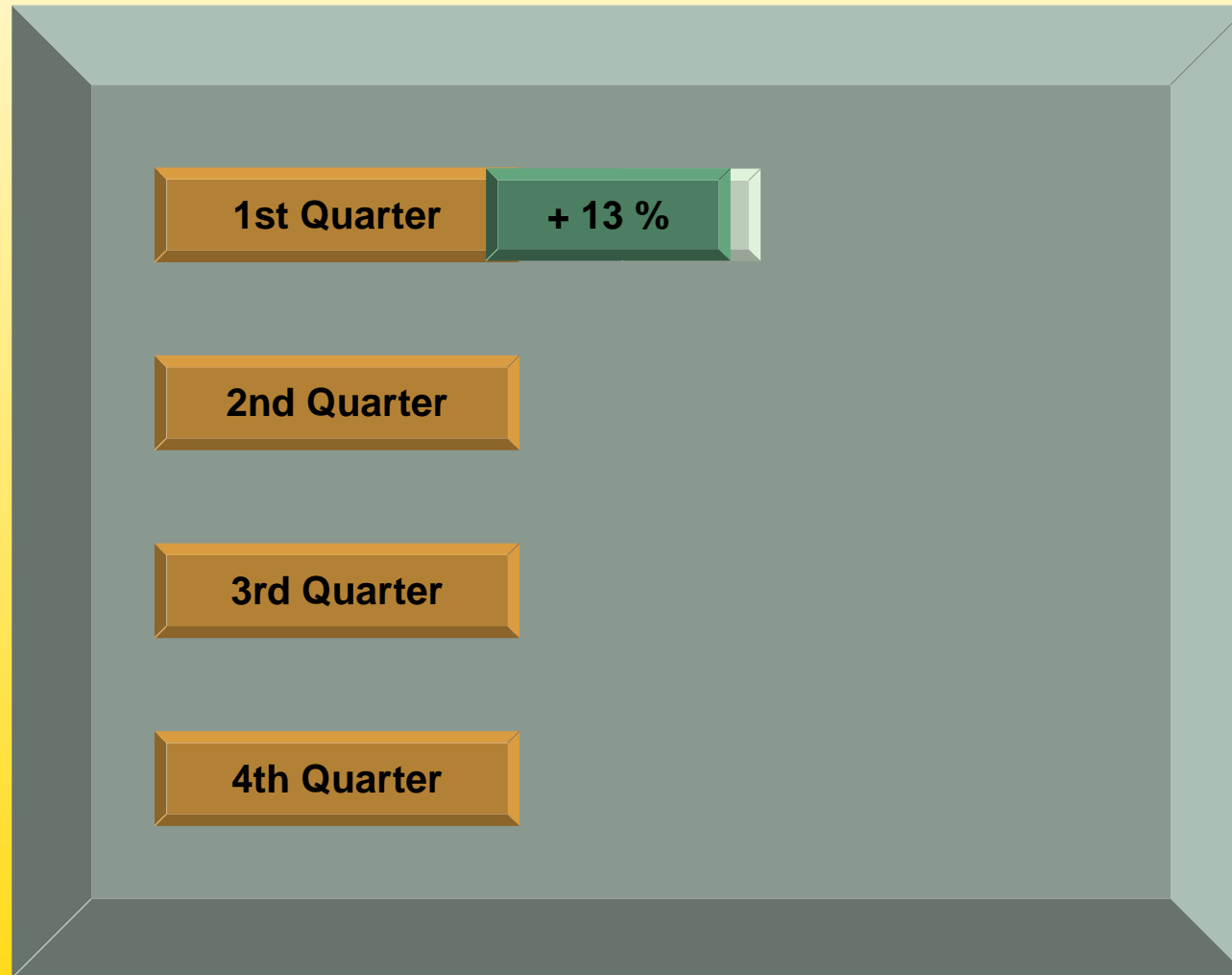
Table 1: Results of the year



End of animation

## 4 – Results of the year

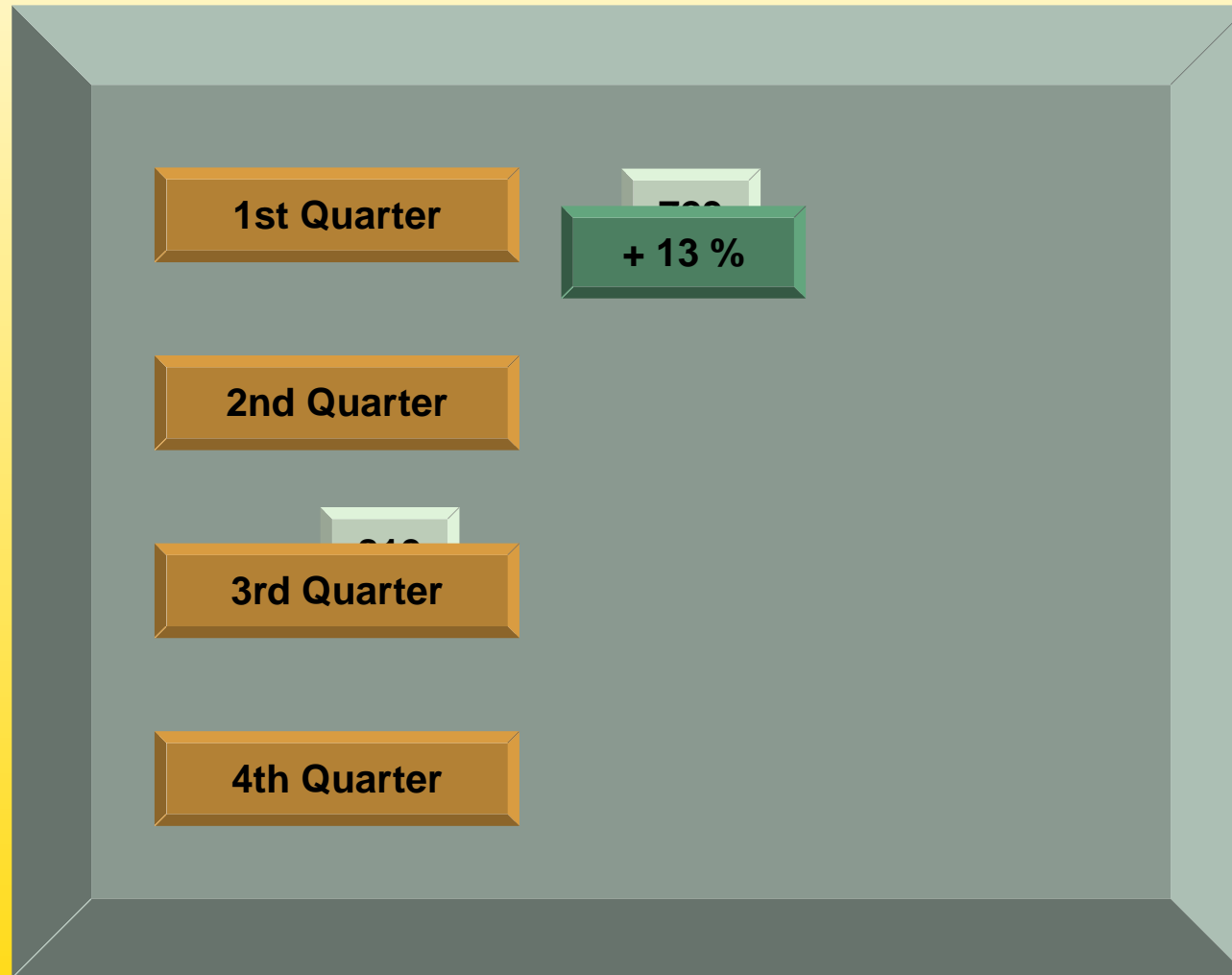
Table 1: Results of the year



End of animation

## 4 – Results of the year

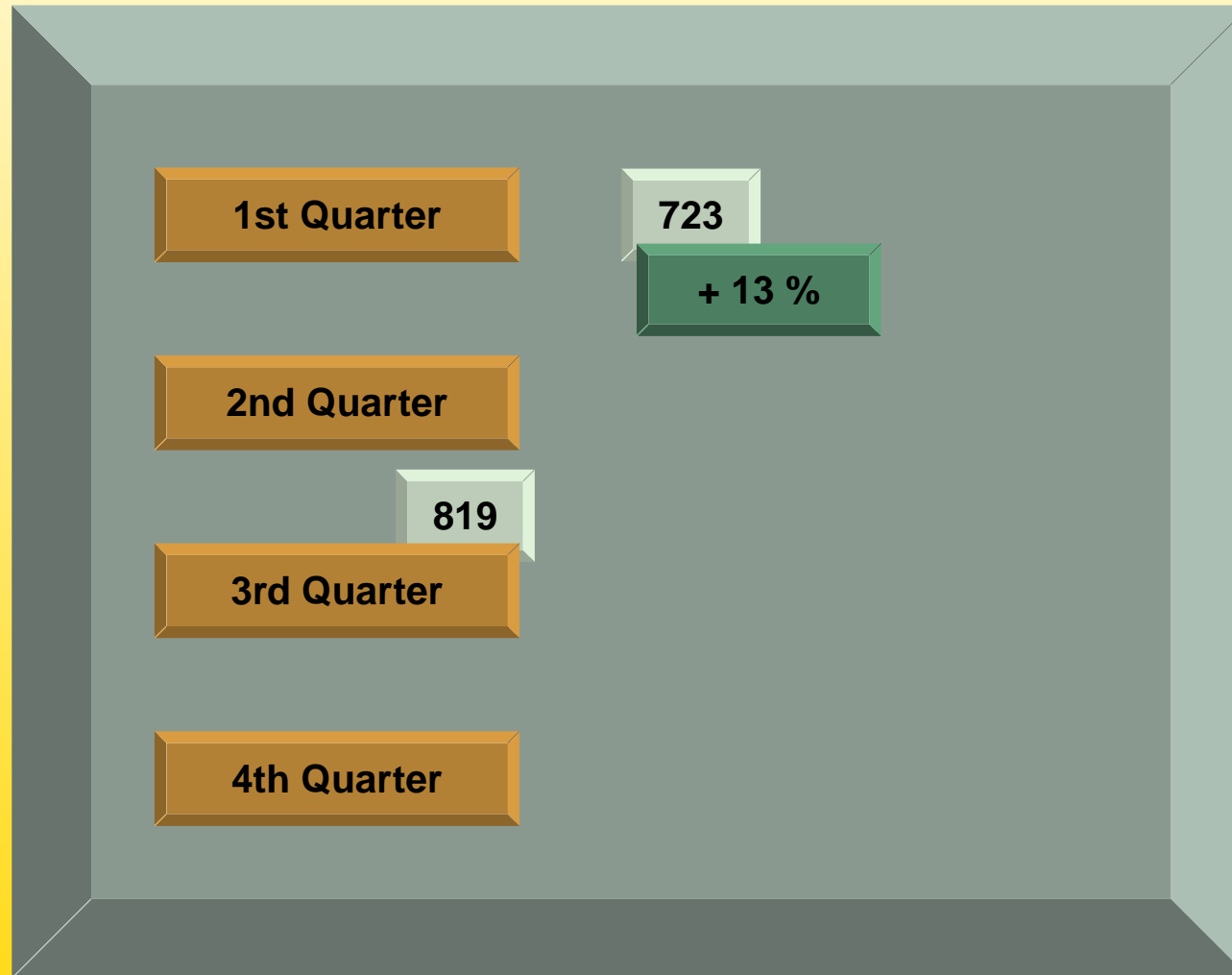
Table 1: Results of the year



End of animation

## 4 – Results of the year

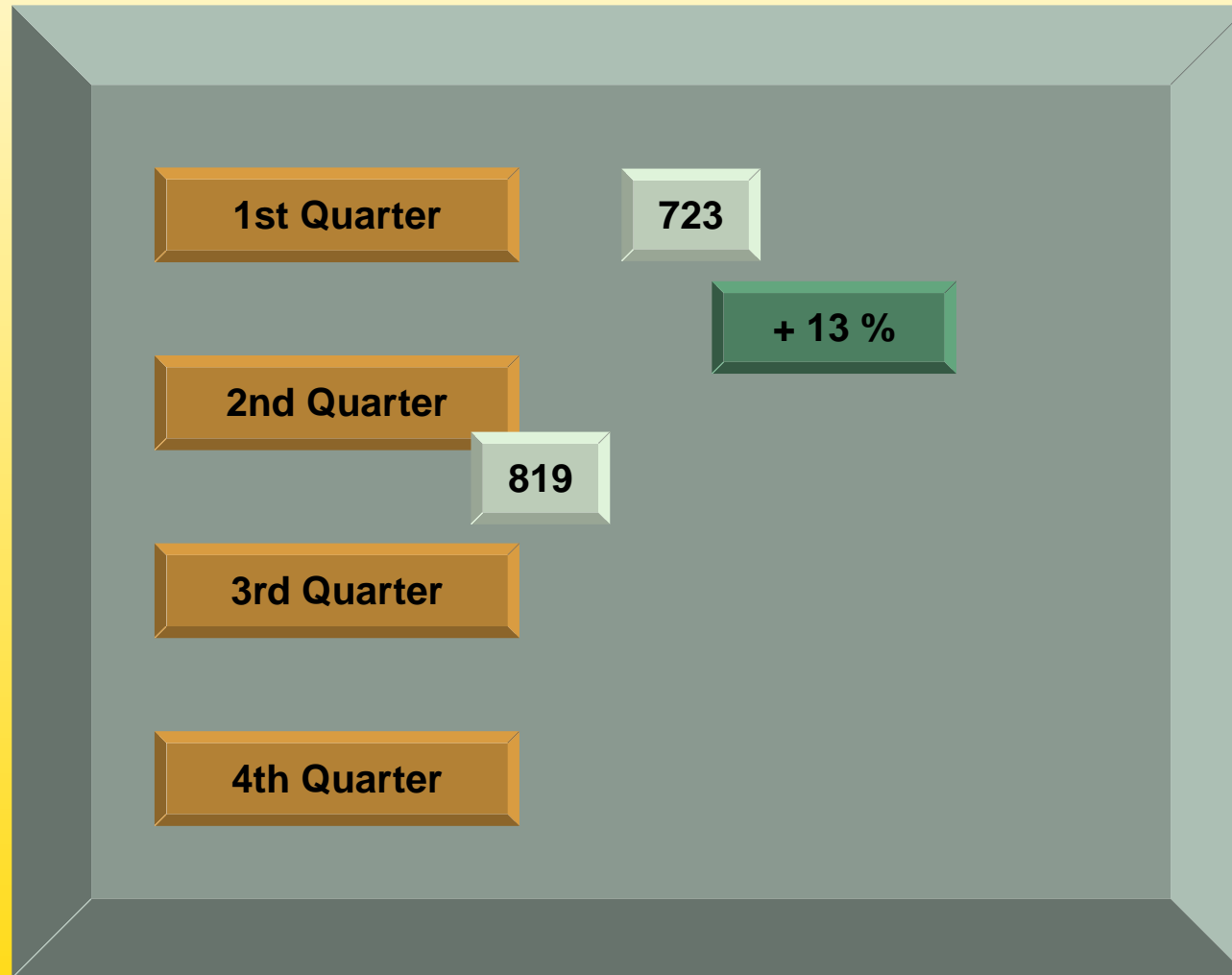
Table 1: Results of the year



End of animation

## 4 – Results of the year

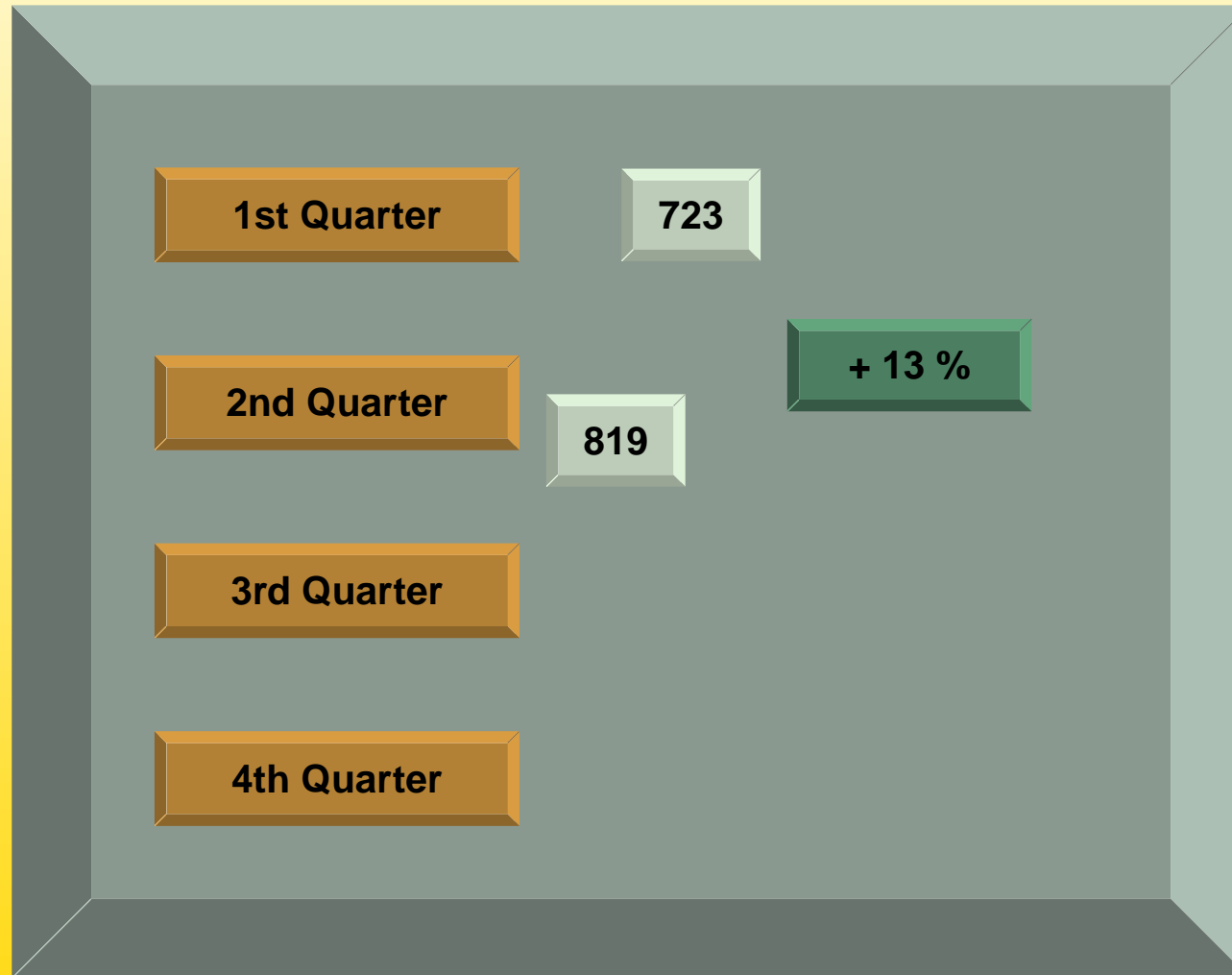
Table 1: Results of the year



End of animation

## 4 – Results of the year

Table 1: Results of the year



End of animation



## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter		
4th Quarter		

End of animation

## 4 – Results of the year

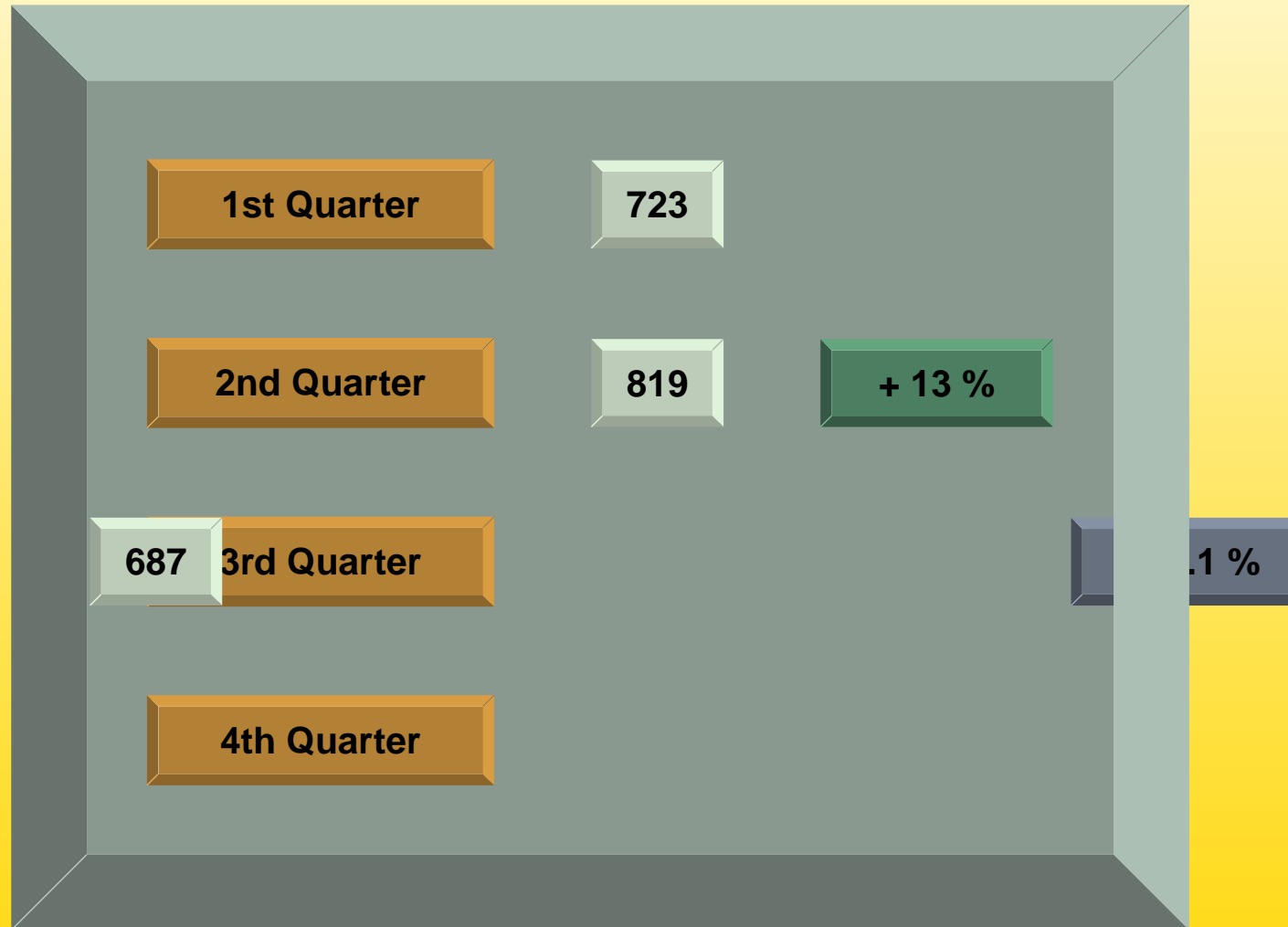
Table 1: Results of the year



End of animation

## 4 – Results of the year

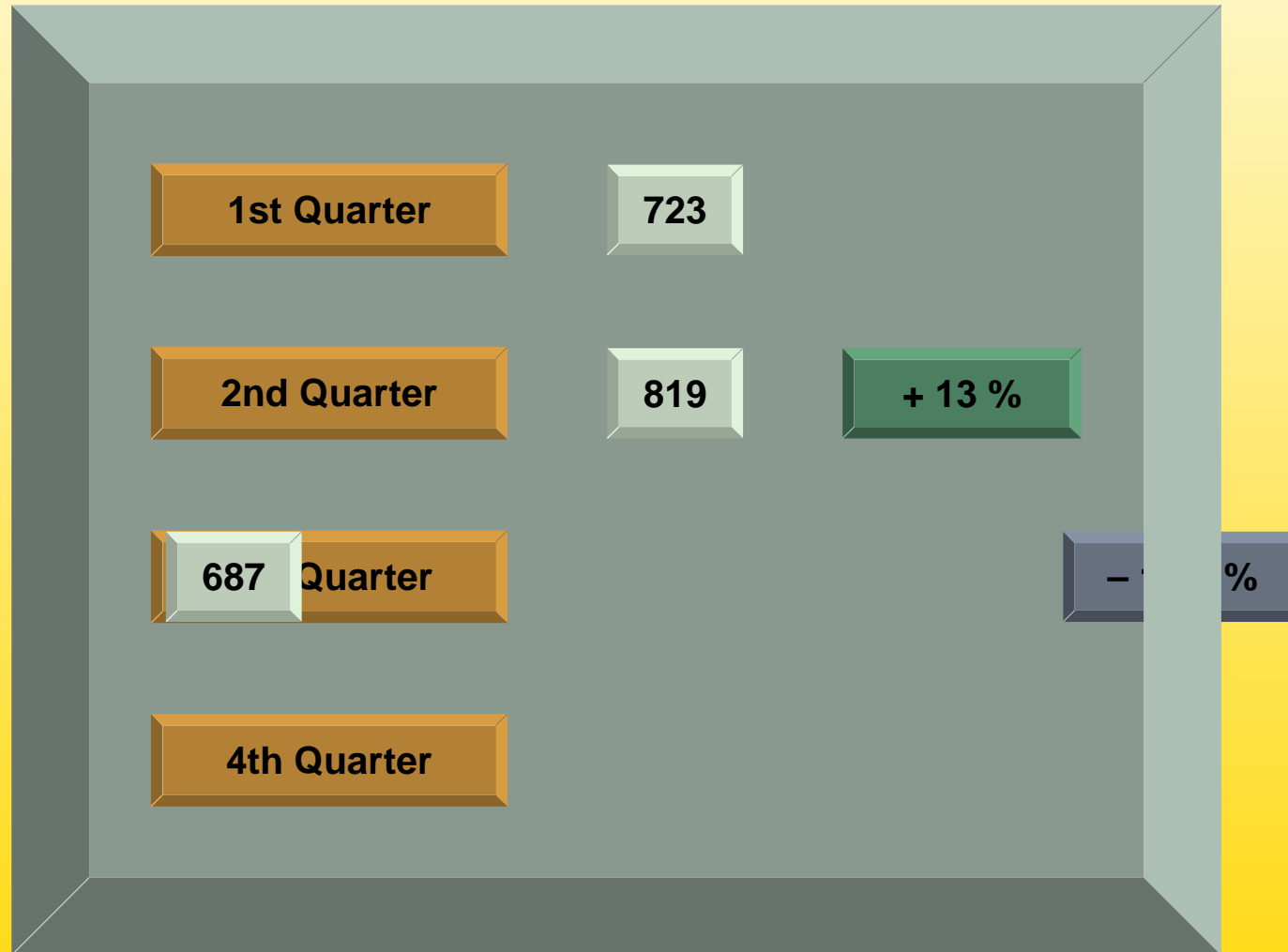
Table 1: Results of the year



End of animation

## 4 – Results of the year

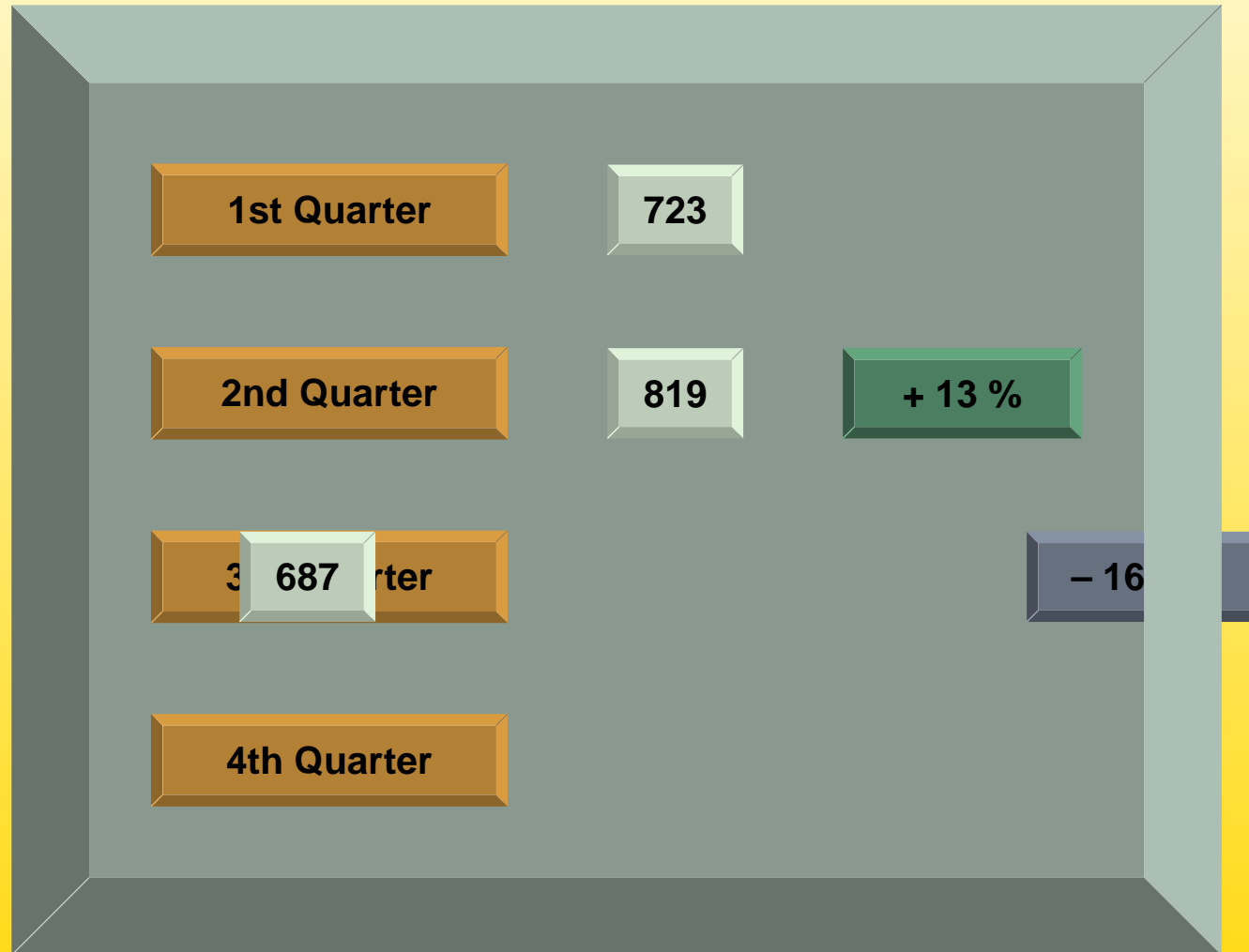
Table 1: Results of the year



End of animation

## 4 – Results of the year

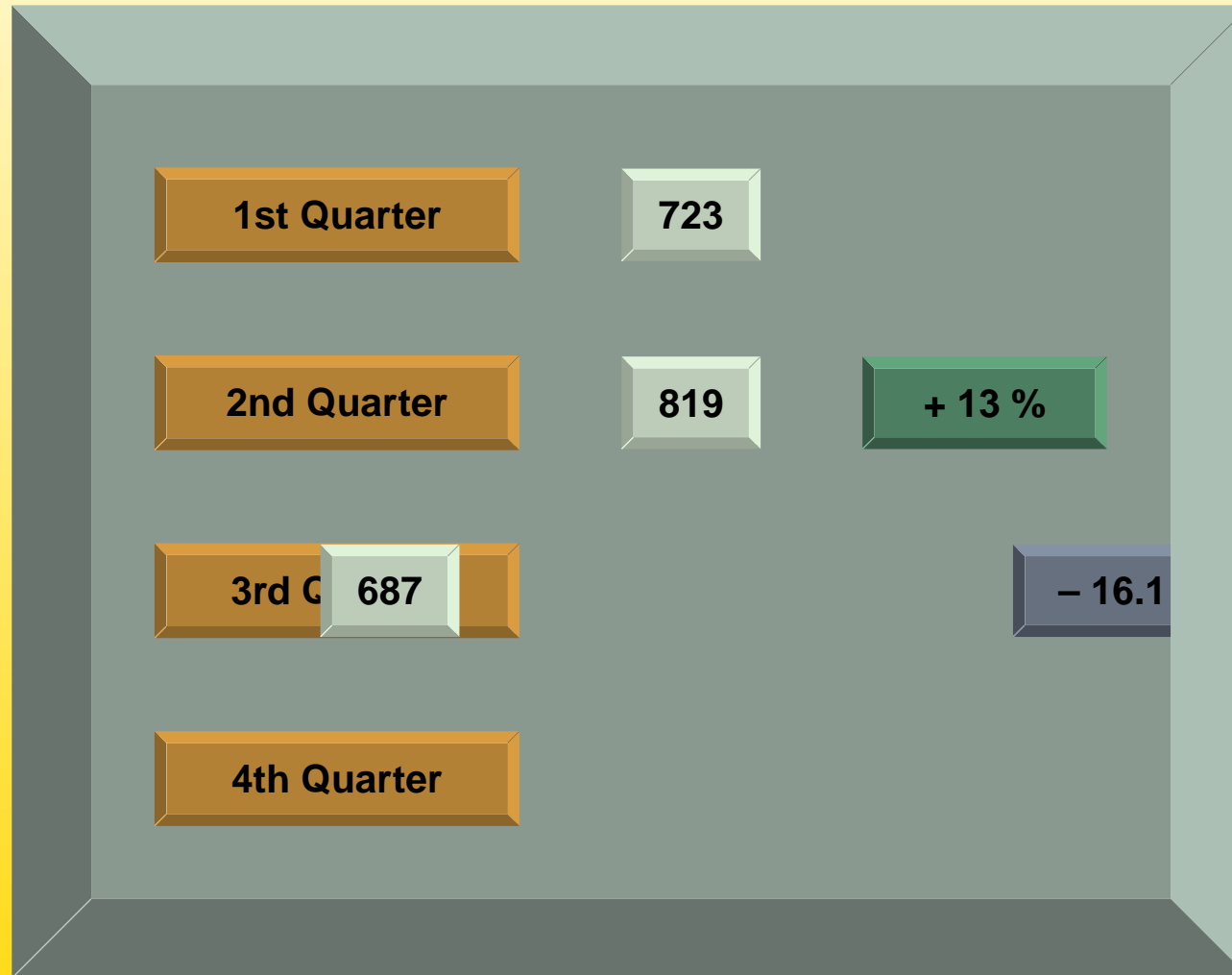
Table 1: Results of the year



End of animation

## 4 – Results of the year

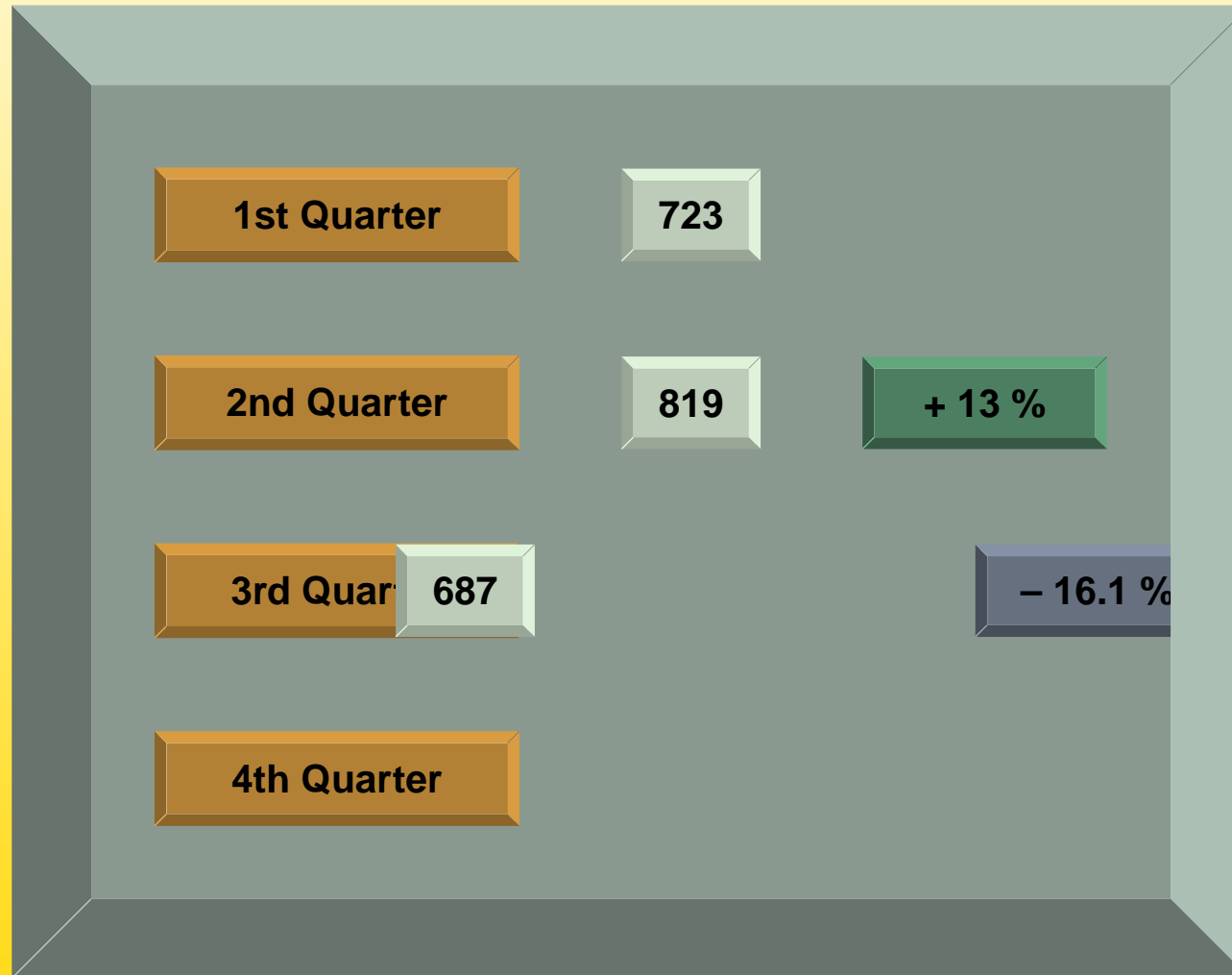
Table 1: Results of the year



End of animation

## 4 – Results of the year

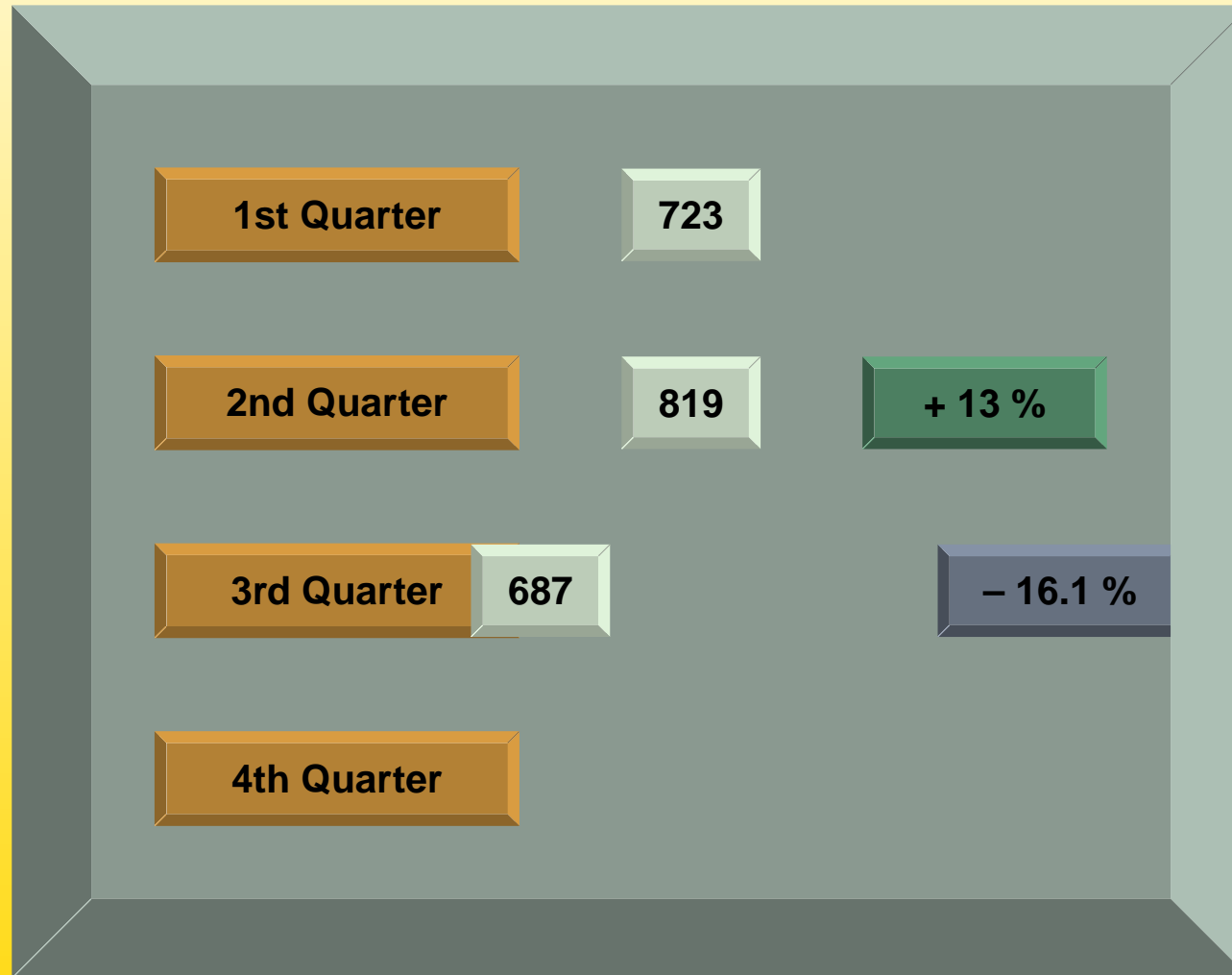
Table 1: Results of the year



End of animation

## 4 – Results of the year

Table 1: Results of the year



End of animation



## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	894	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	894	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	894	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	894	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
	894	
3rd Quarter	687	- 16.1 %
4th Quarter		

End of animation

+ 30.1 %

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	894	- 16.1 %
4th Quarter		

+ 30.1 %

End of animation



## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	887 894	- 16.1 %
4th Quarter		

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter	894	+ 30.1 %

End of animation

## 4 – Results of the year

Table 1: Results of the year

1st Quarter	723	
2nd Quarter	819	+ 13 %
3rd Quarter	687	- 16.1 %
4th Quarter	894	+ 30.1 %

End of animation

5 – Clock

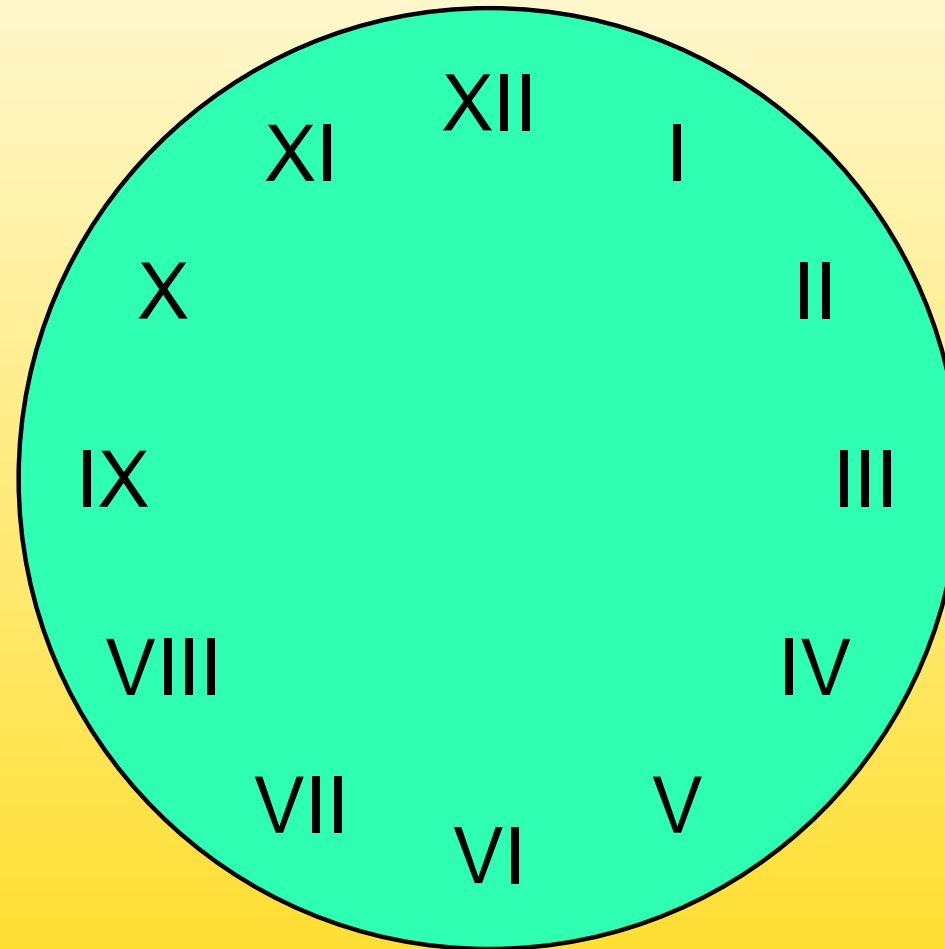


Figure 3: Clock

End of animation

5 – Clock

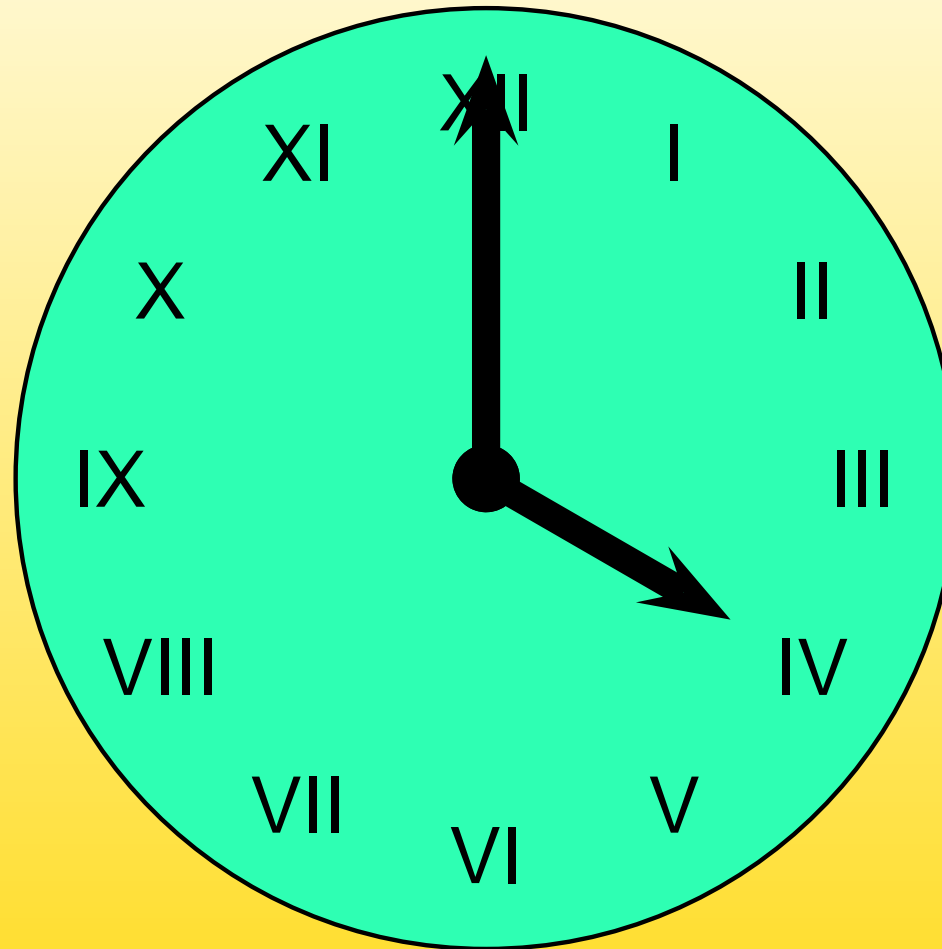


Figure 3: Clock

End of animation

5 – Clock

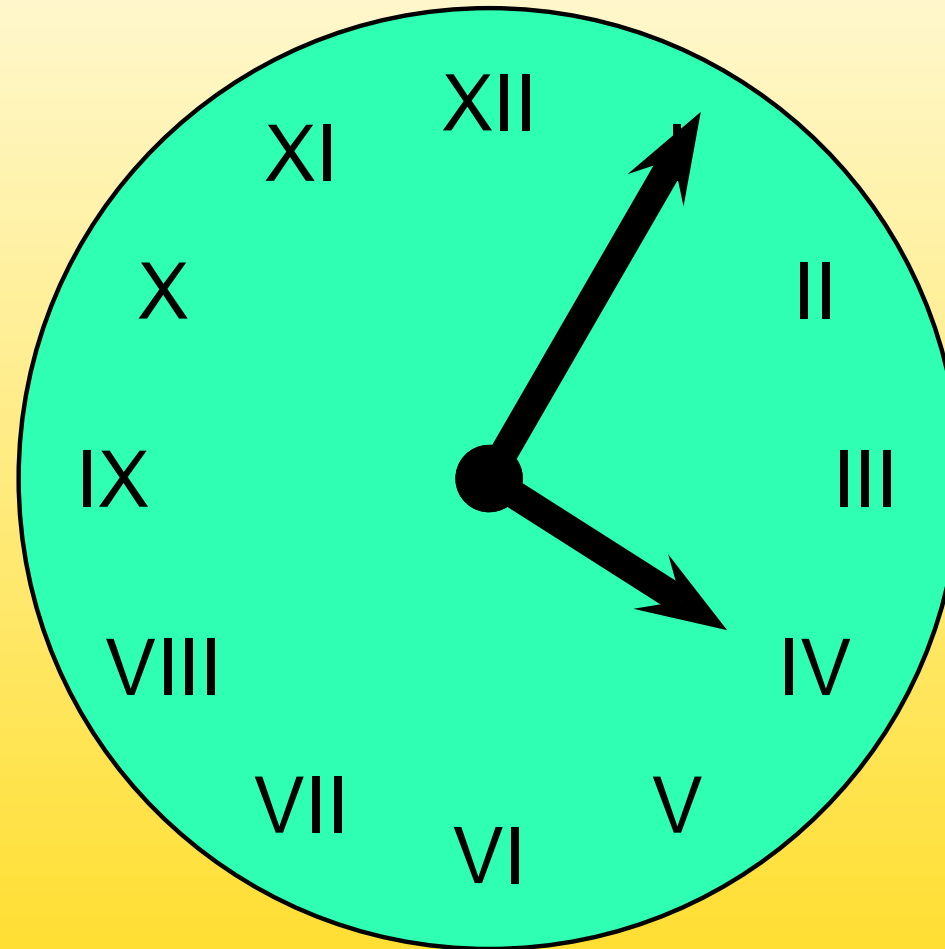


Figure 3: Clock

End of animation

5 – Clock

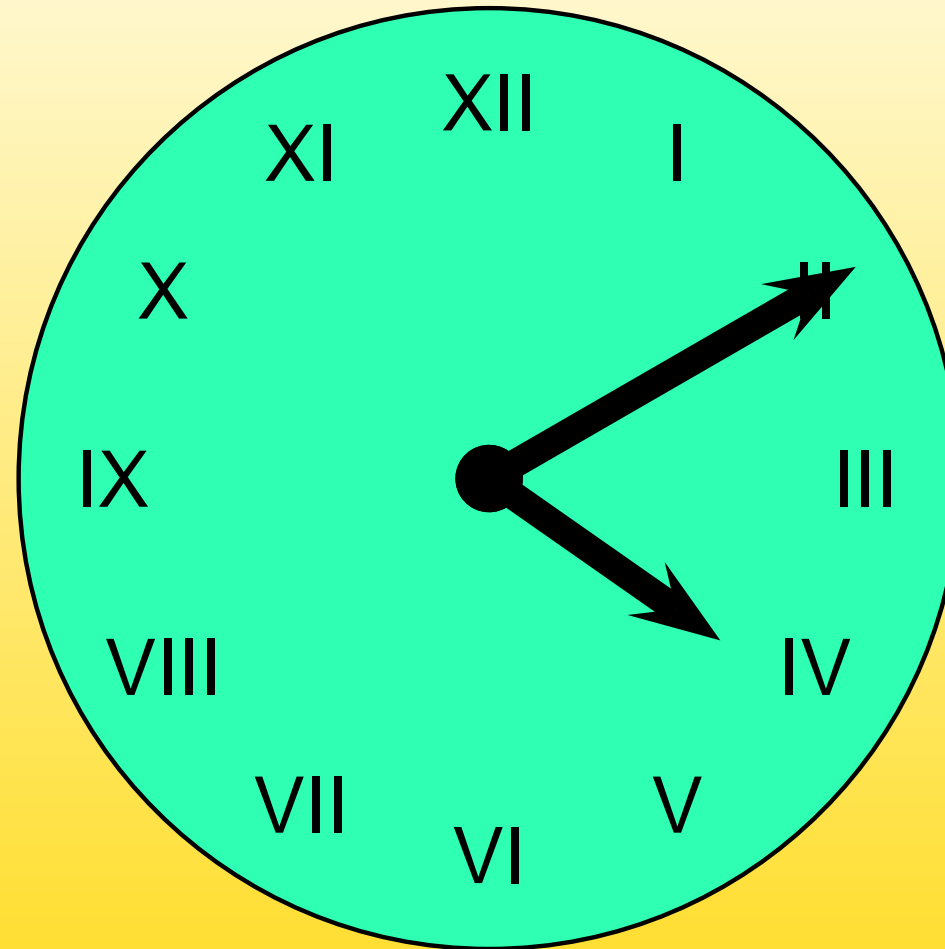


Figure 3: Clock

End of animation

5 – Clock

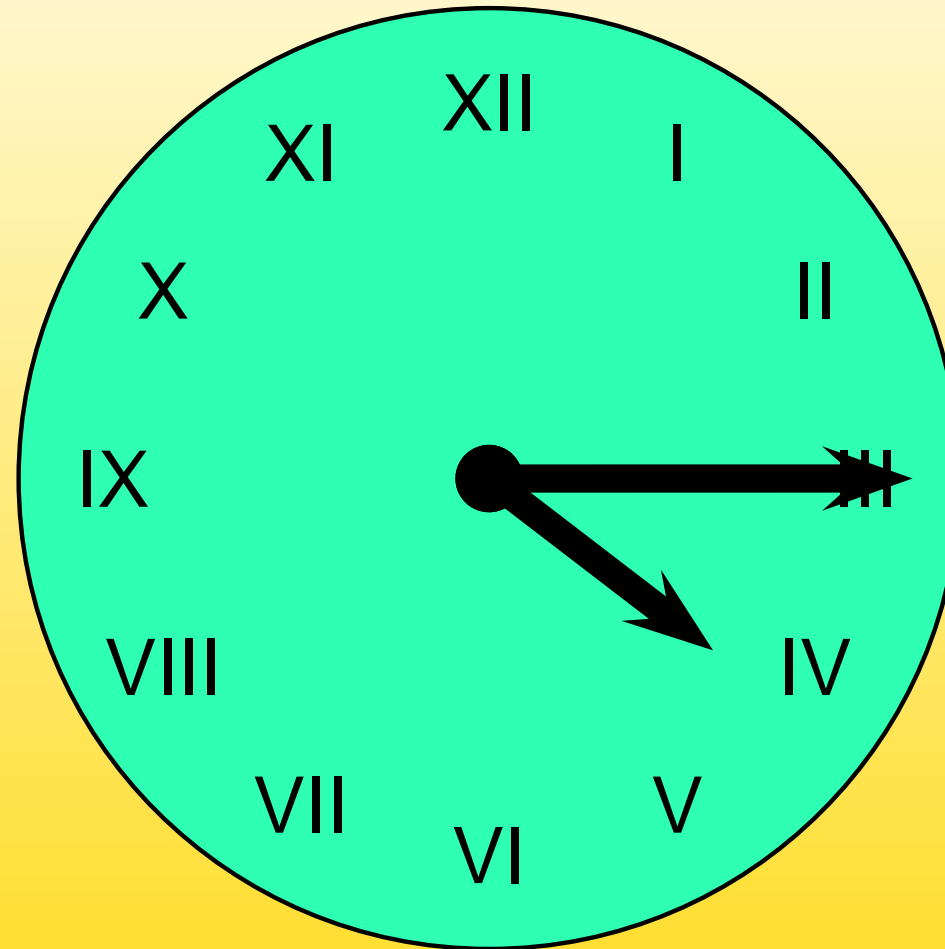


Figure 3: Clock

End of animation



5 – Clock



Figure 3: Clock

End of animation

5 – Clock



Figure 3: Clock

End of animation

5 – Clock



Figure 3: Clock

End of animation

5 – Clock

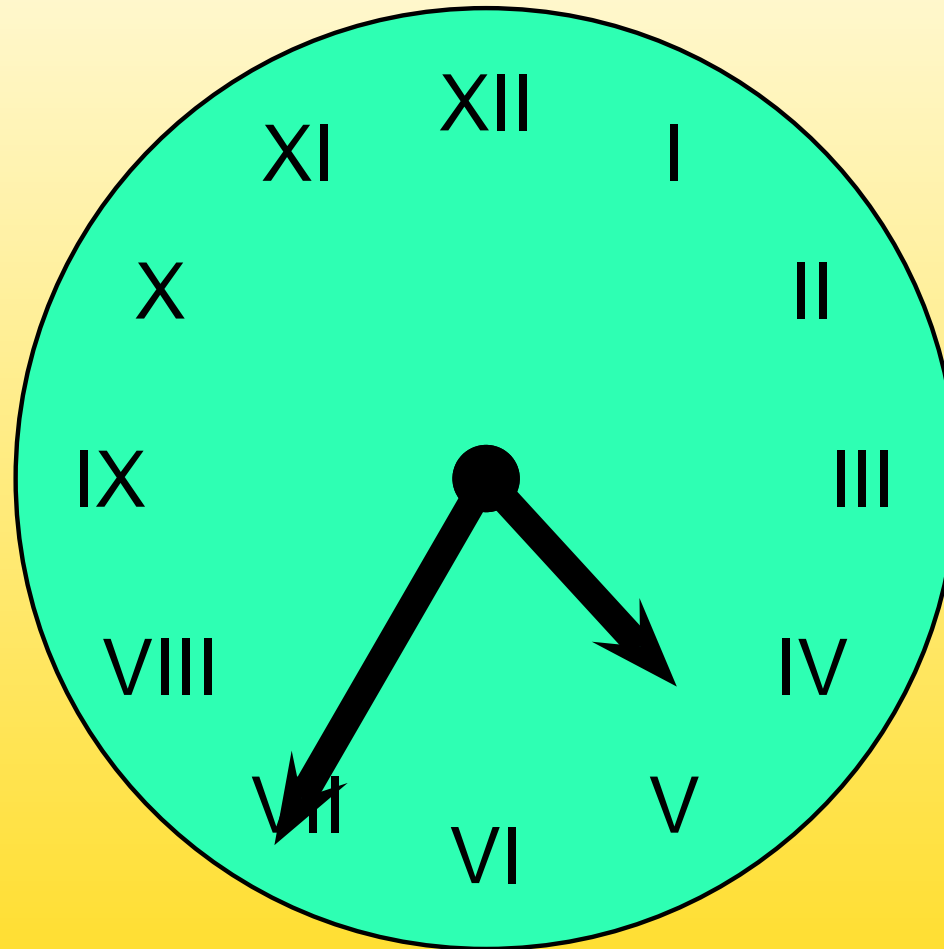


Figure 3: Clock

End of animation

5 – Clock

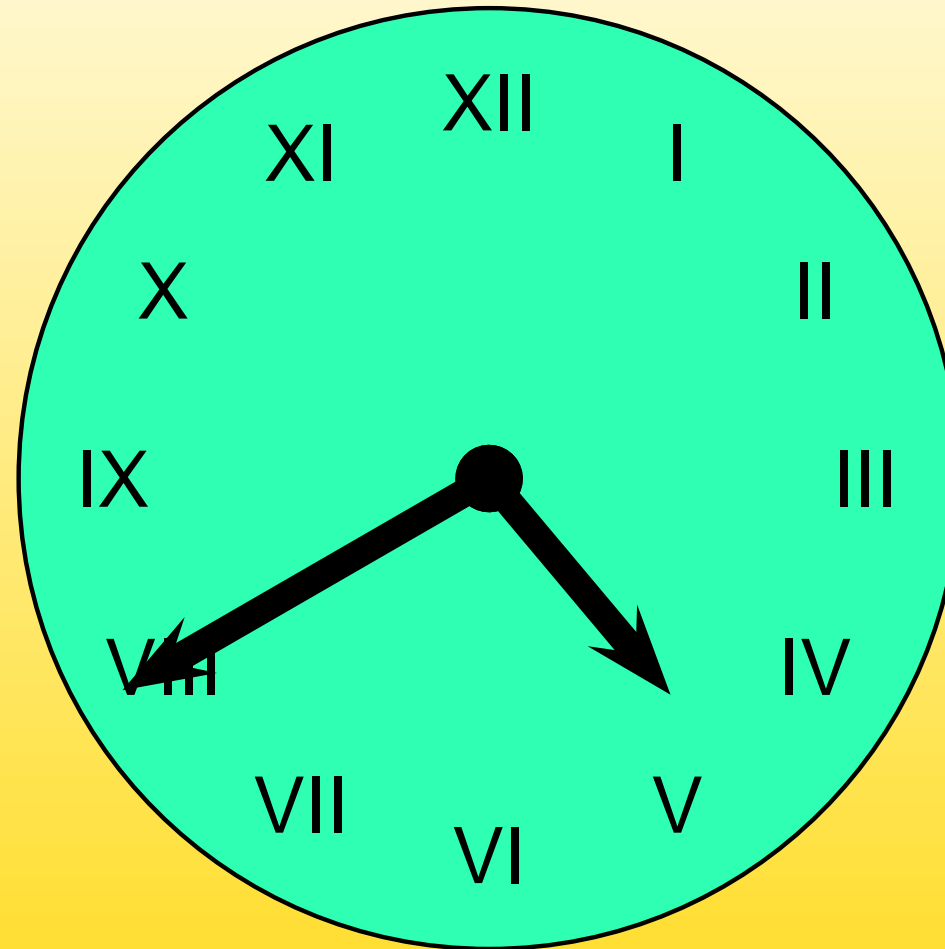


Figure 3: Clock

End of animation

5 – Clock

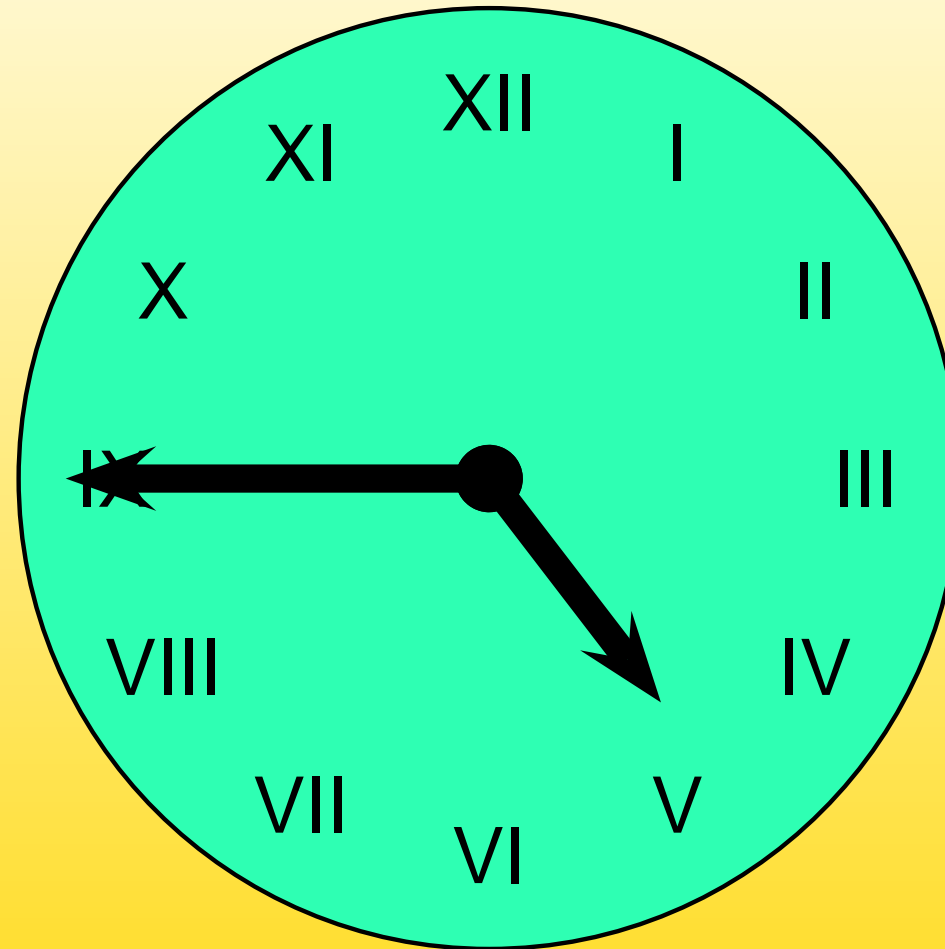


Figure 3: Clock

End of animation

5 – Clock

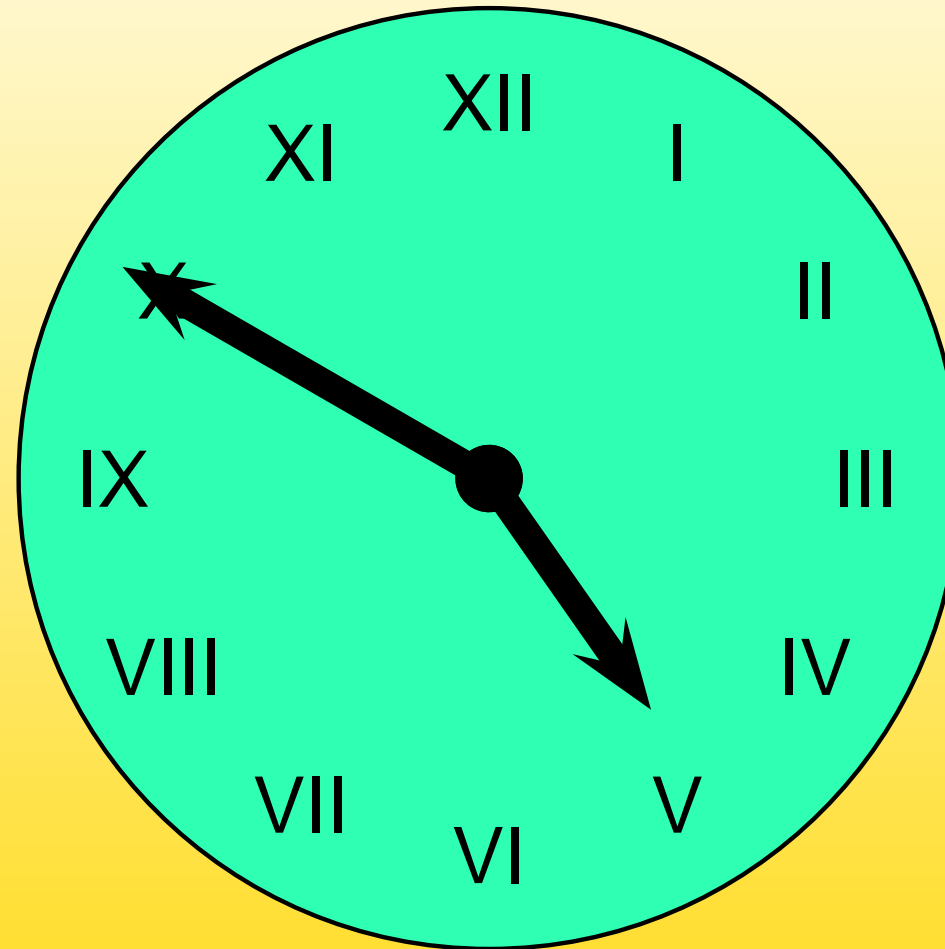


Figure 3: Clock

End of animation

5 – Clock

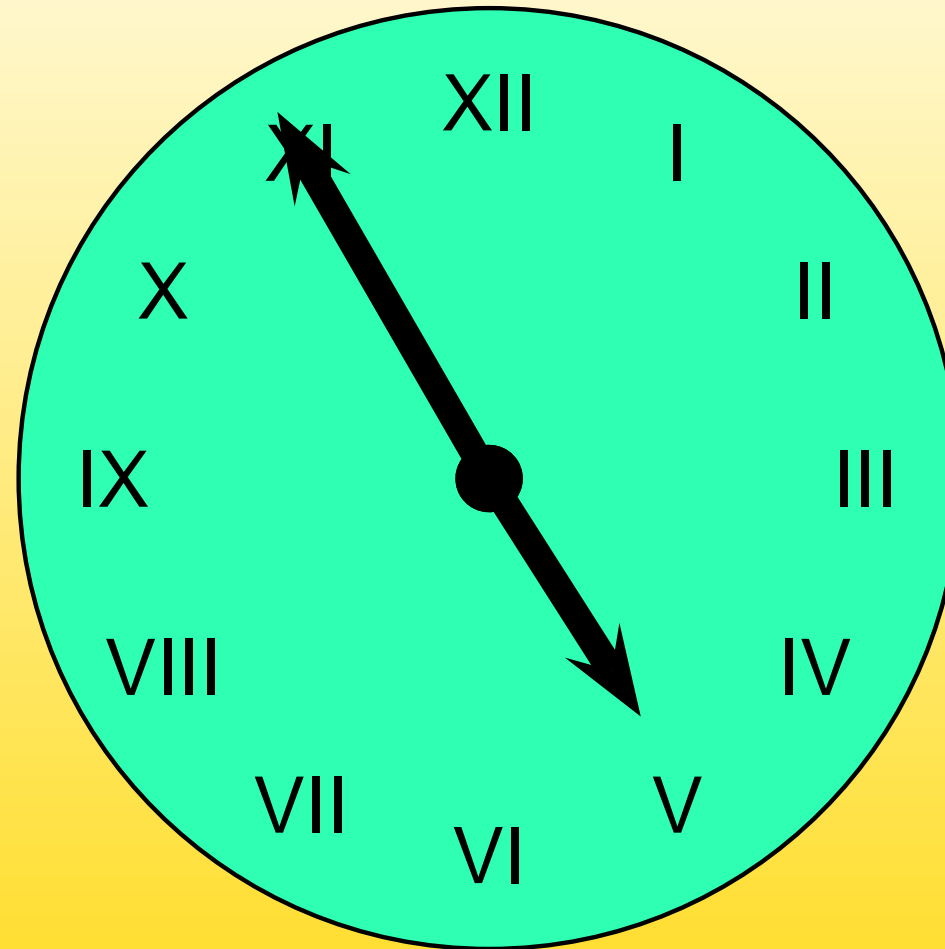


Figure 3: Clock

End of animation



5 – Clock



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation





Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation



Figure 3: Clock

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m

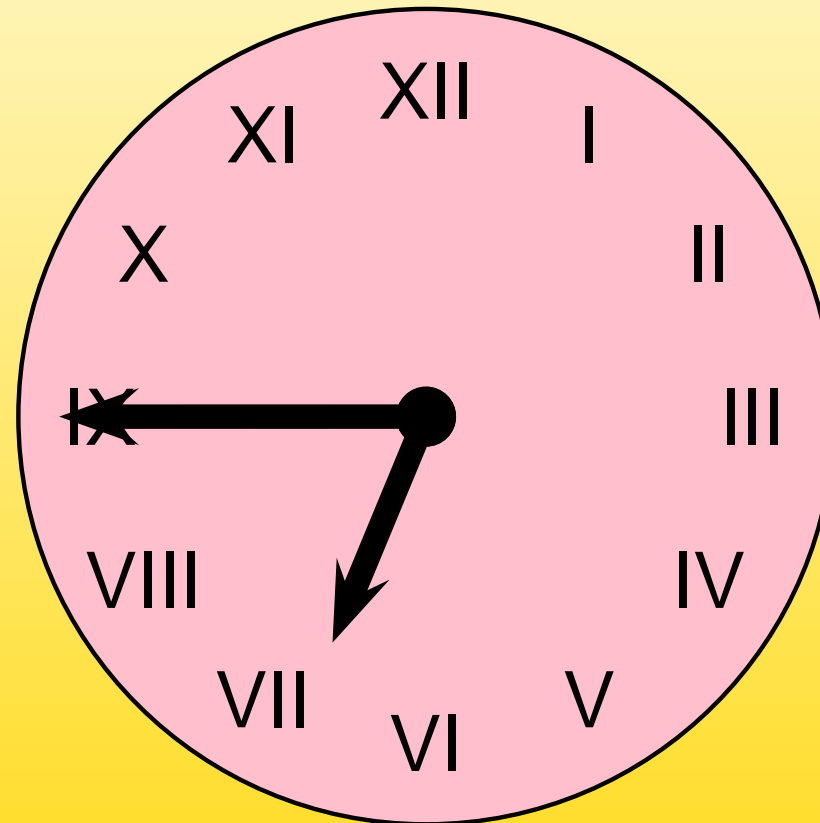


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 01s

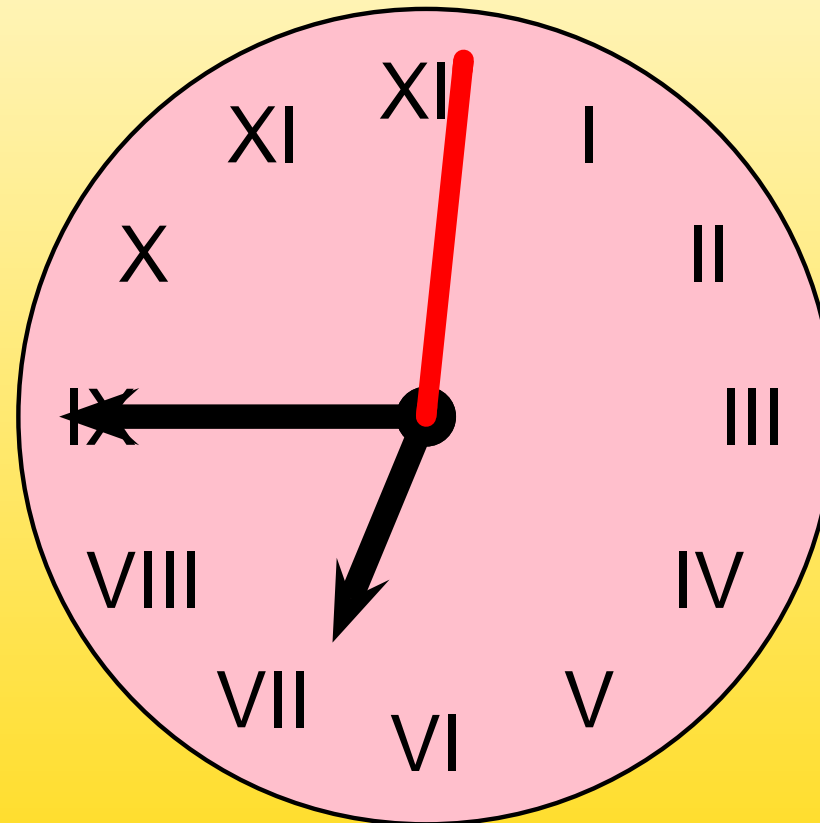


Figure 4: Clock with split-second hand

End of animation



## 6 – Clock with split-second hand

Document compiled at: 18h 45m 02s

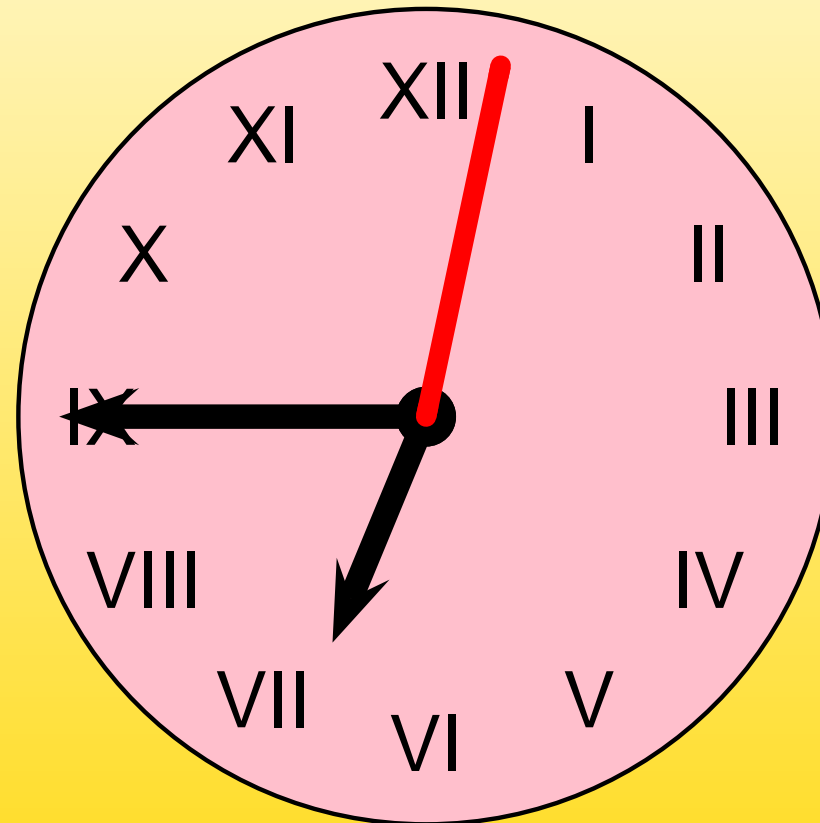


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 03s

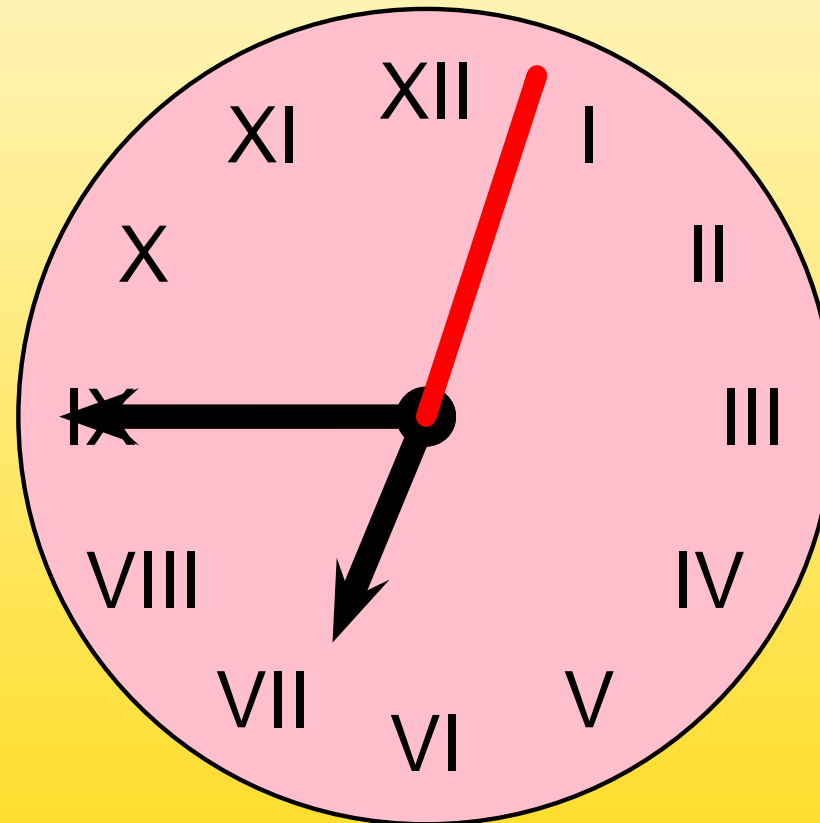


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 04s

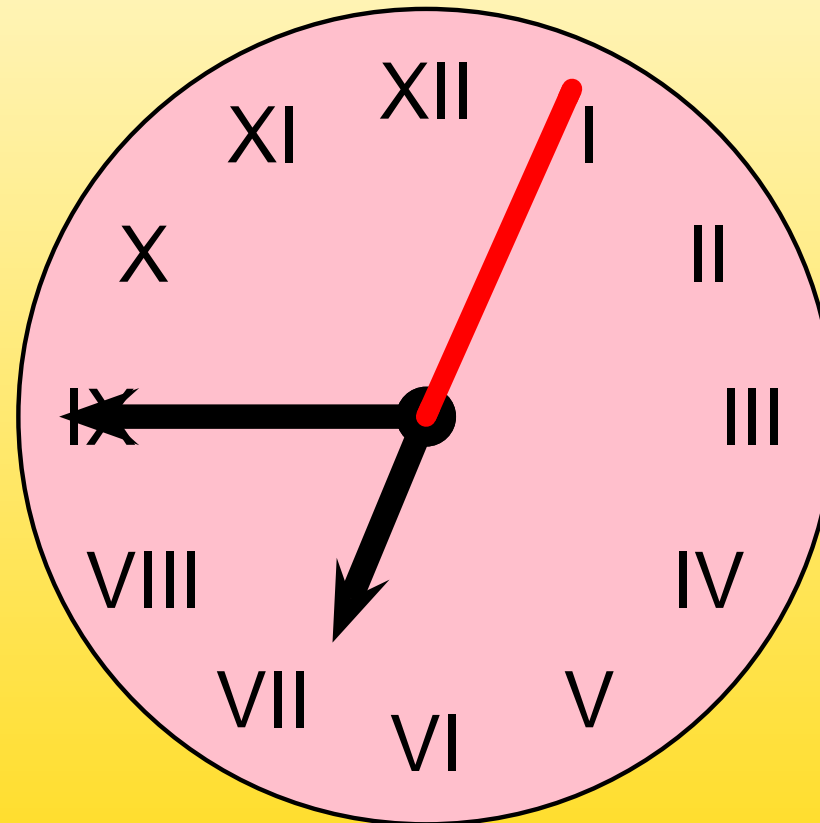


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 05s

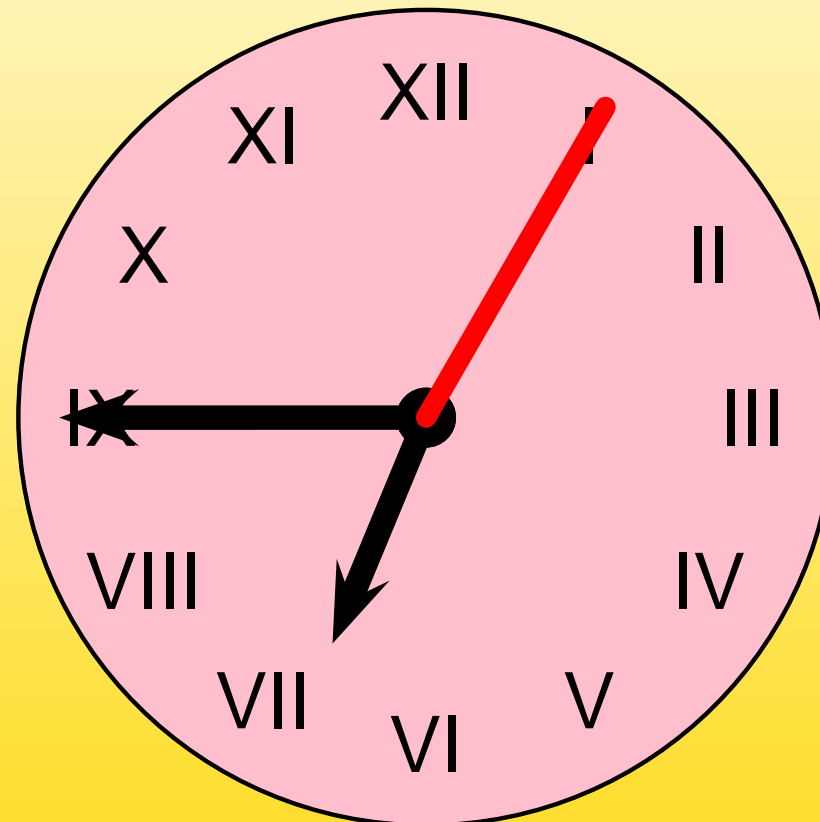


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 06s

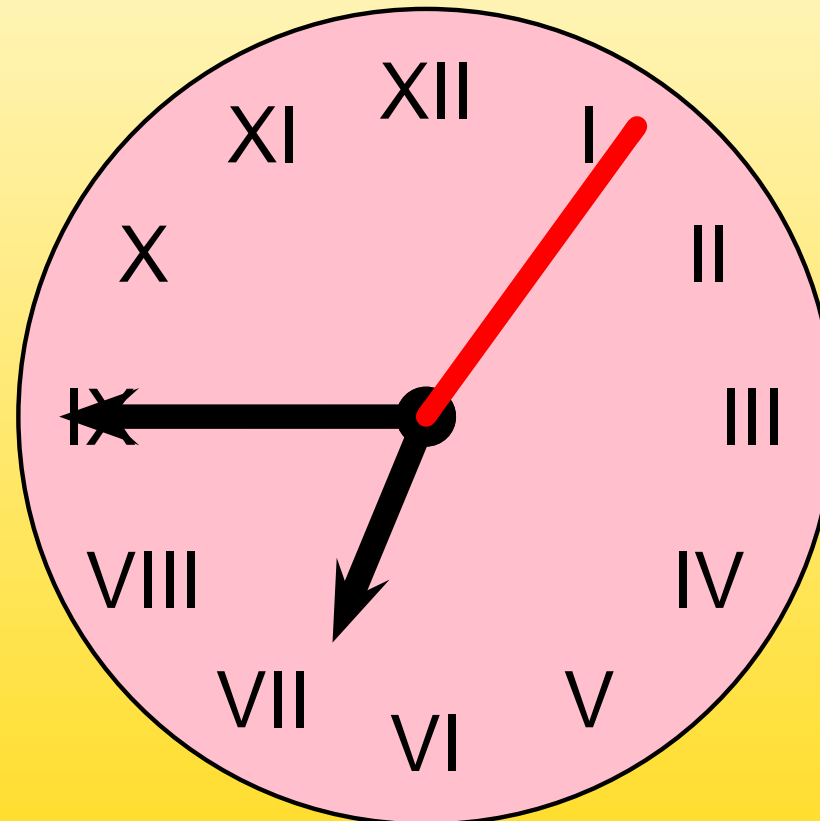


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 07s

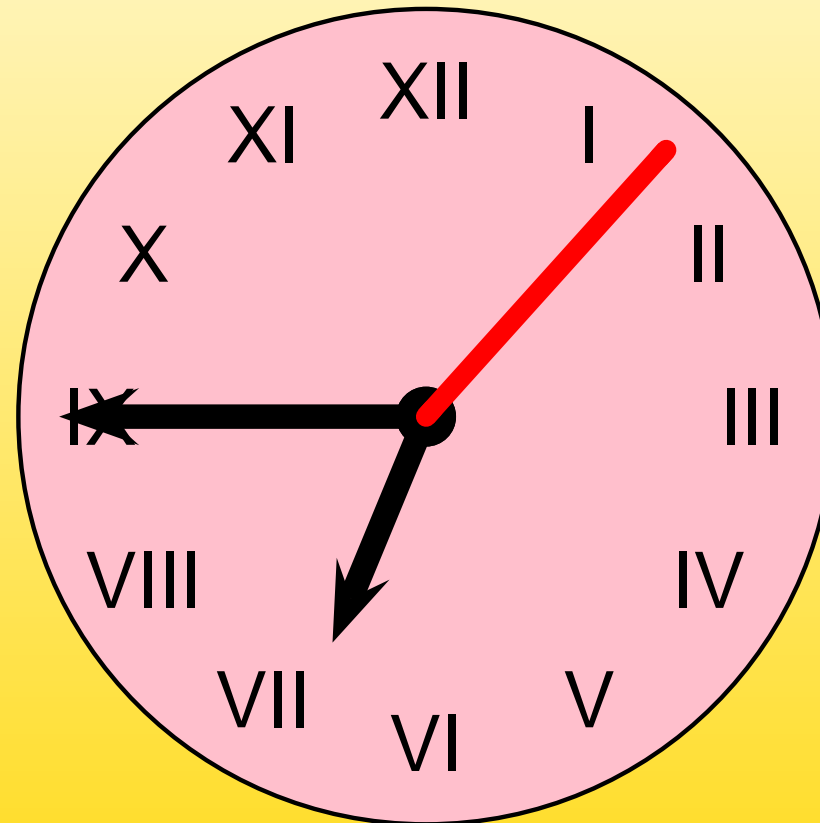


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 08s

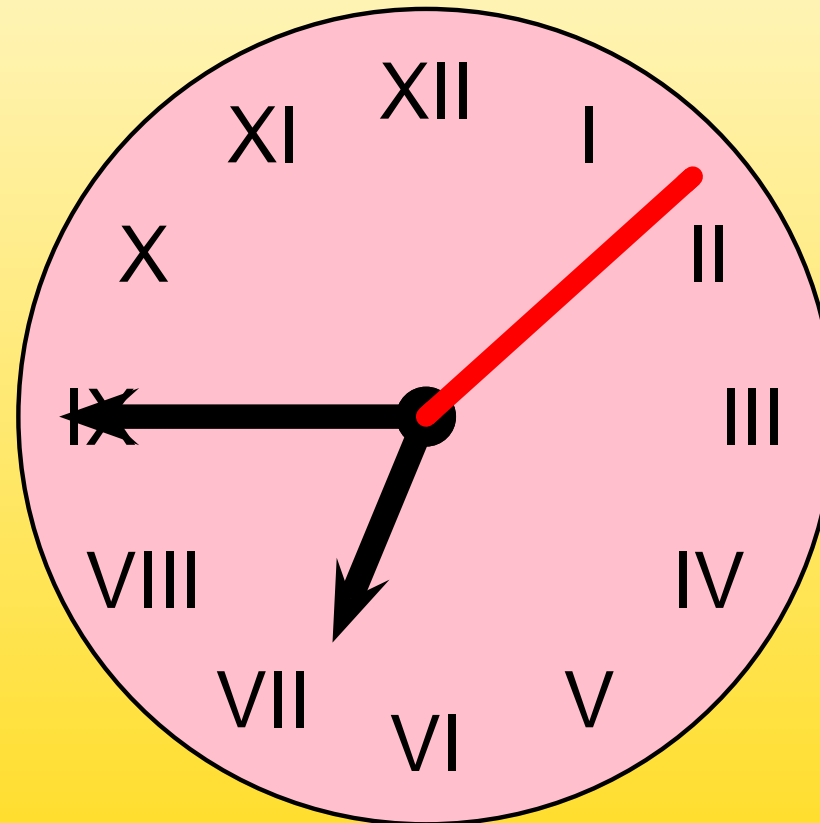


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 09s

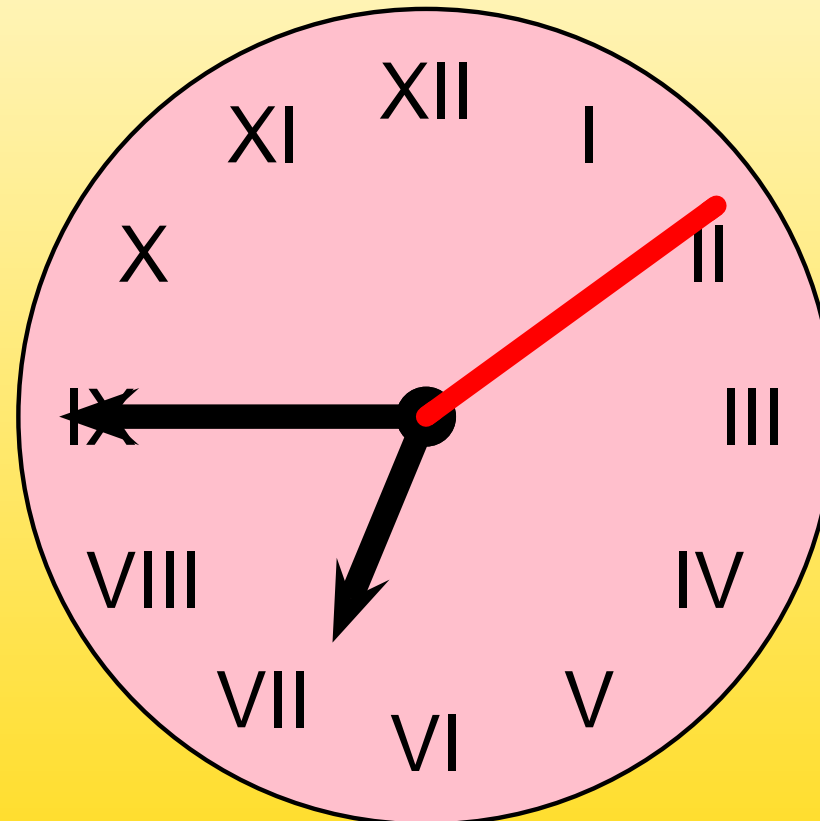


Figure 4: Clock with split-second hand

End of animation



## 6 – Clock with split-second hand

Document compiled at: 18h 45m 10s

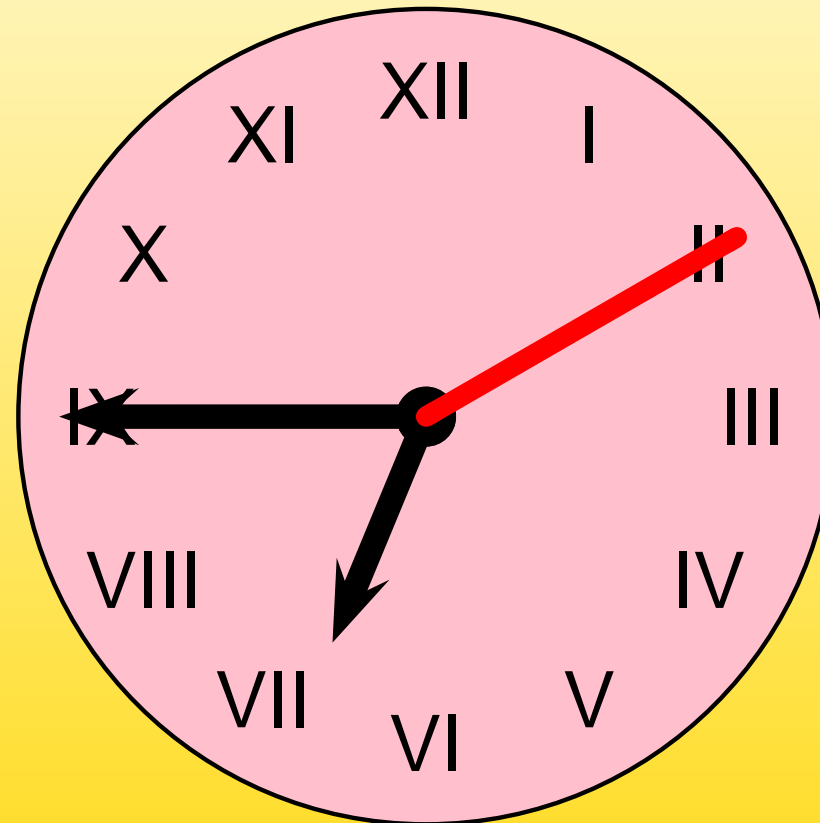


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 11s

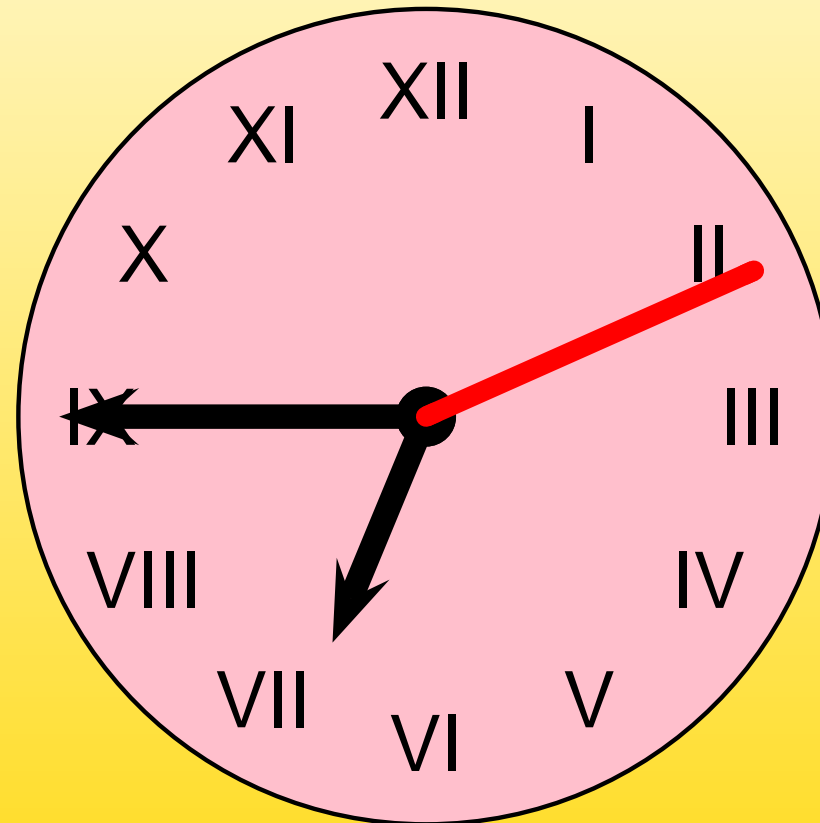


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 12s

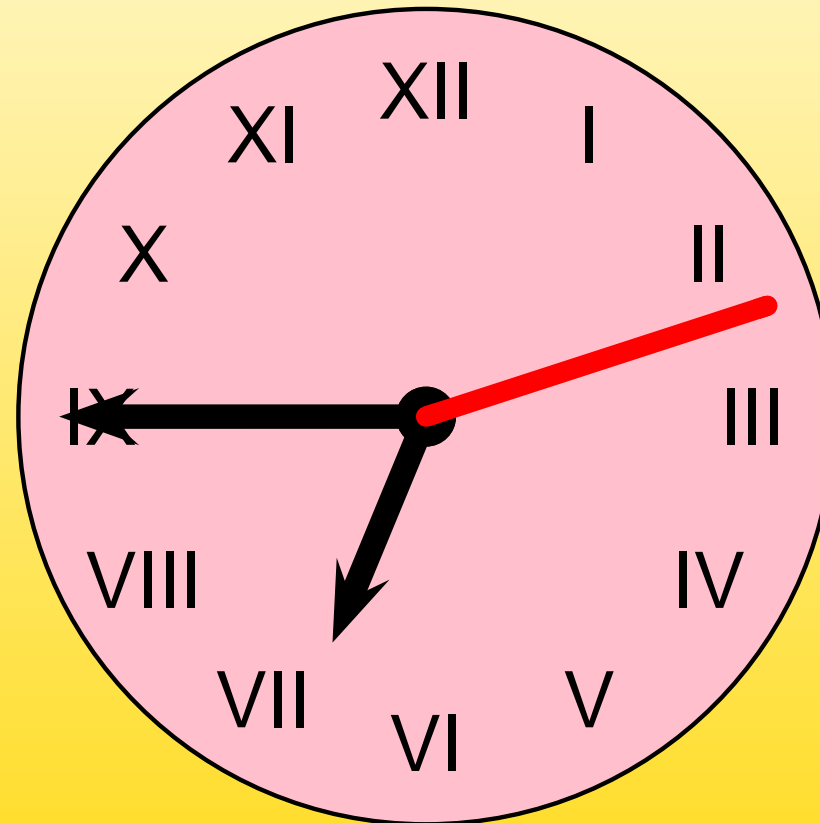


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 13s

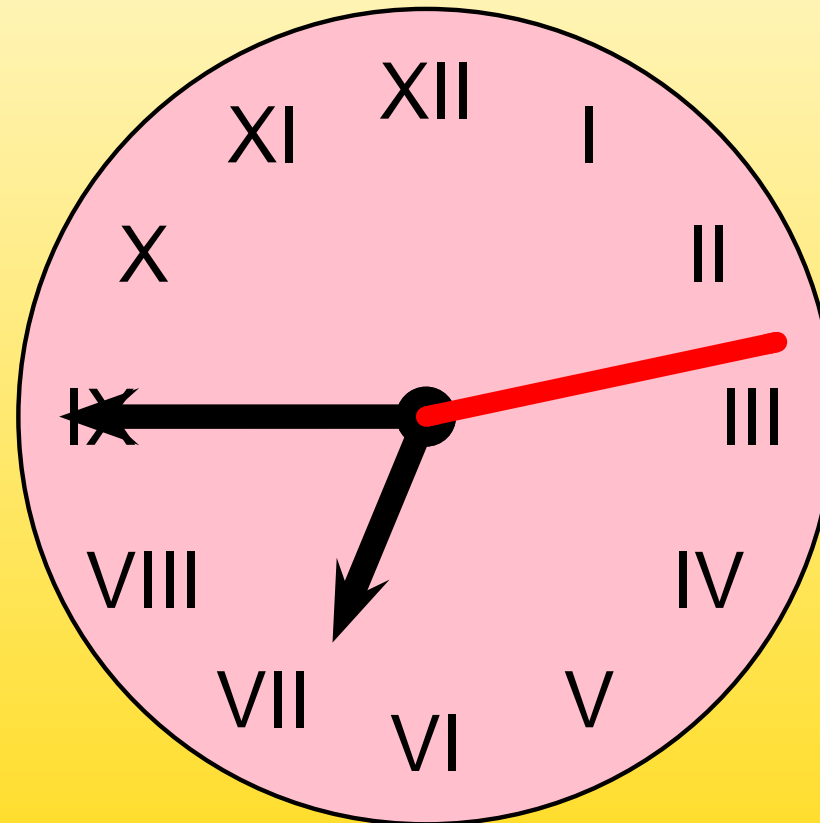


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 14s

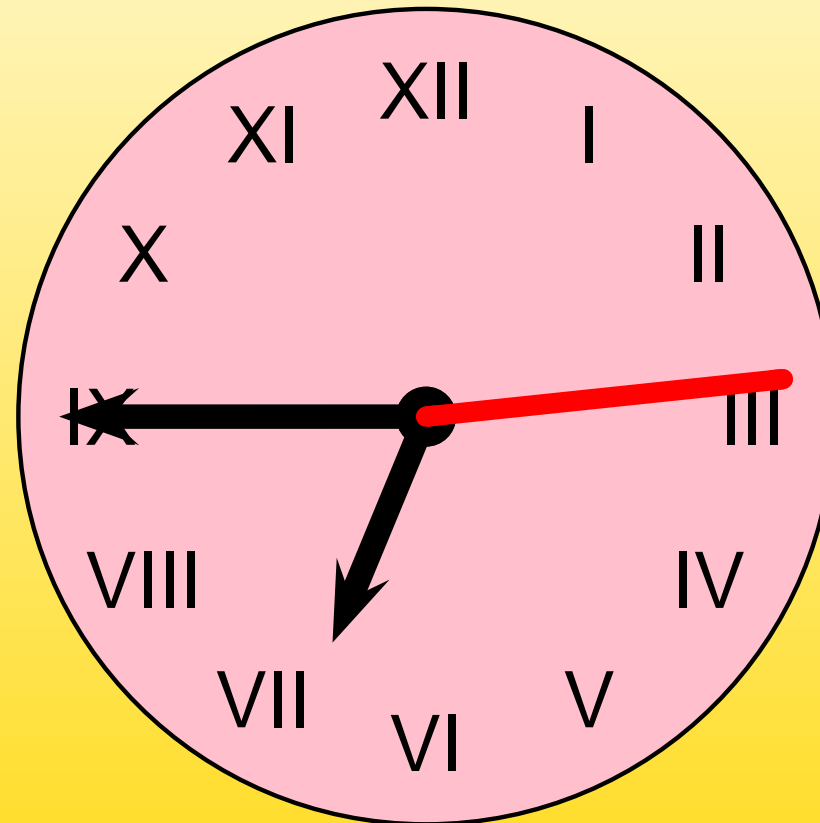


Figure 4: Clock with split-second hand

End of animation

## 6 – Clock with split-second hand

Document compiled at: 18h 45m 15s

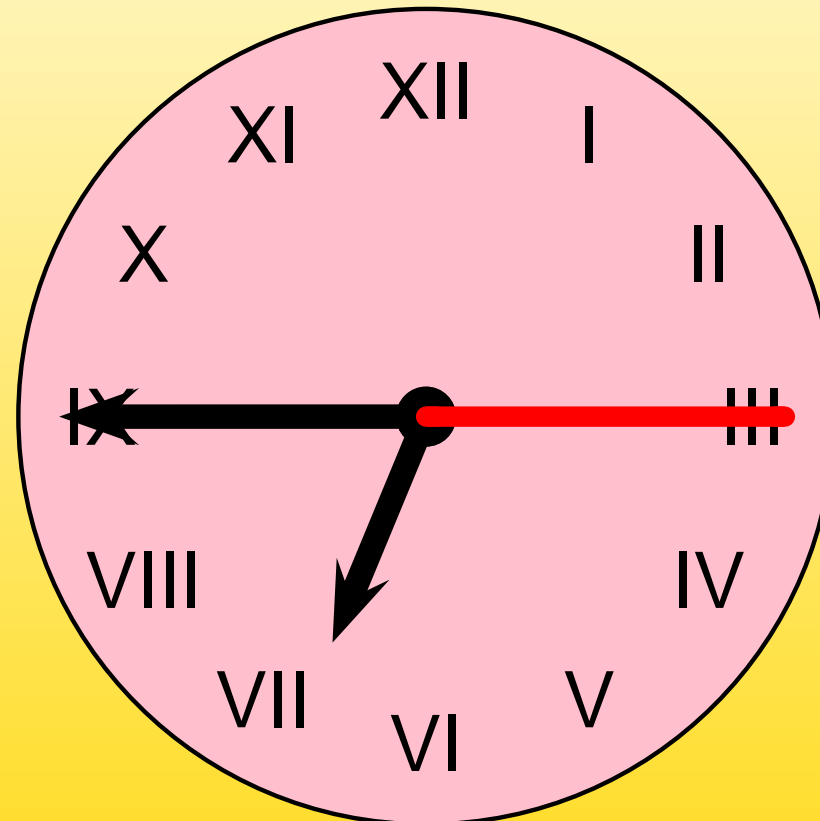


Figure 4: Clock with split-second hand

End of animation

## 7 – Random walk

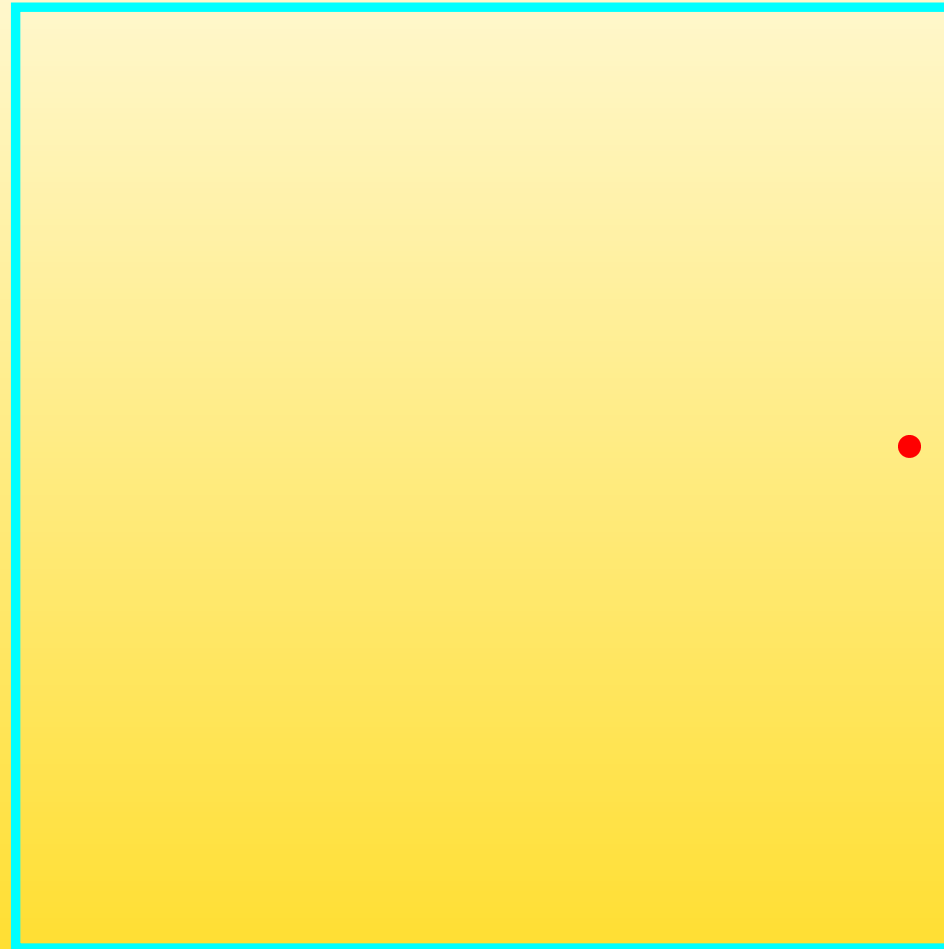


Figure 5: Random walk

End of animation

## 7 – Random walk

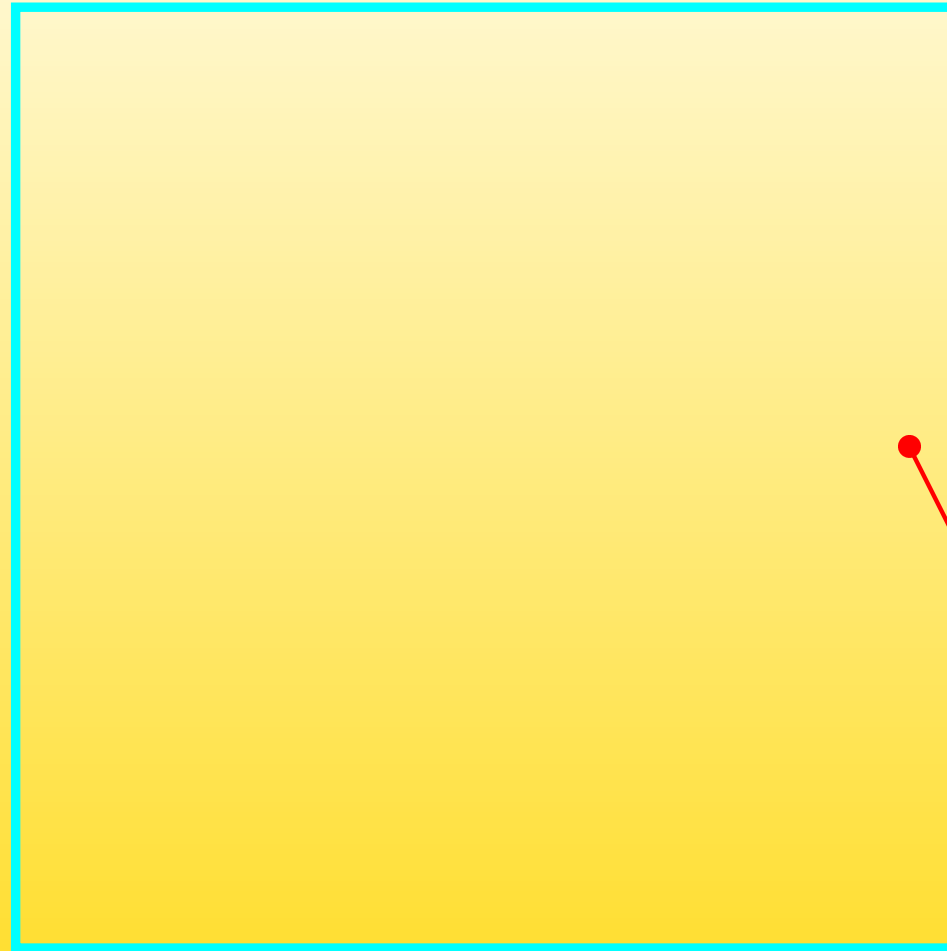


Figure 5: Random walk

End of animation



## 7 – Random walk

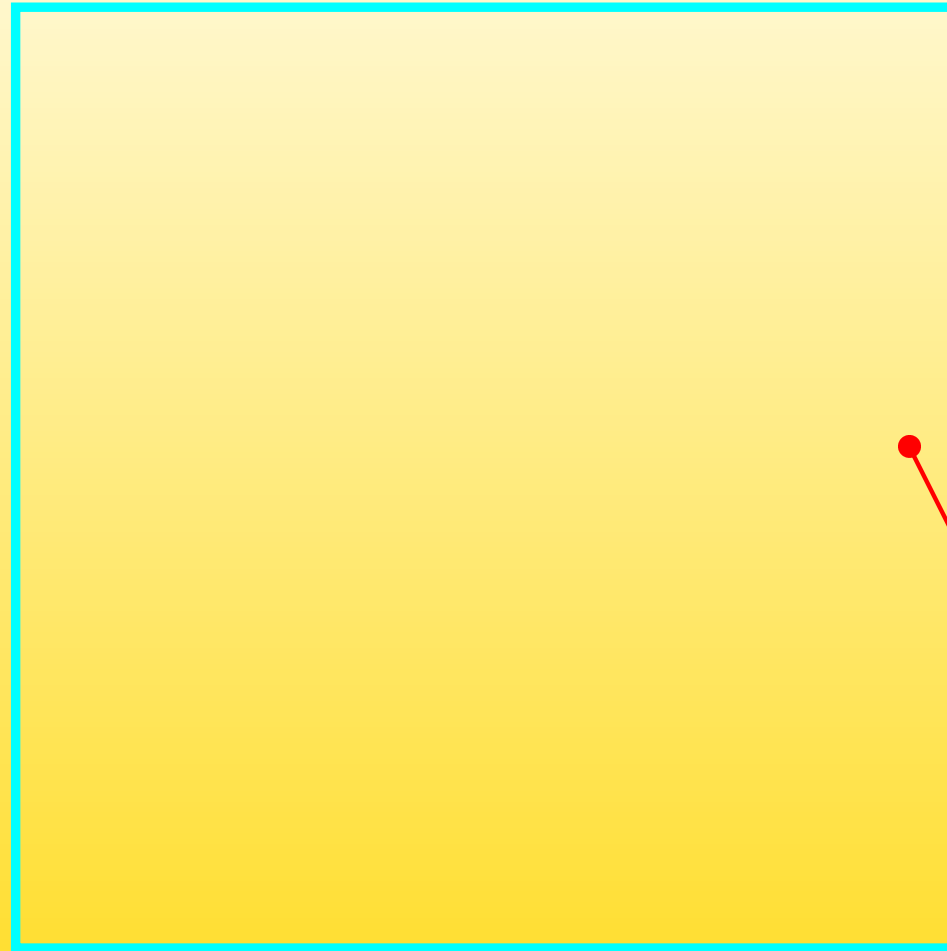


Figure 5: Random walk

End of animation

## 7 – Random walk

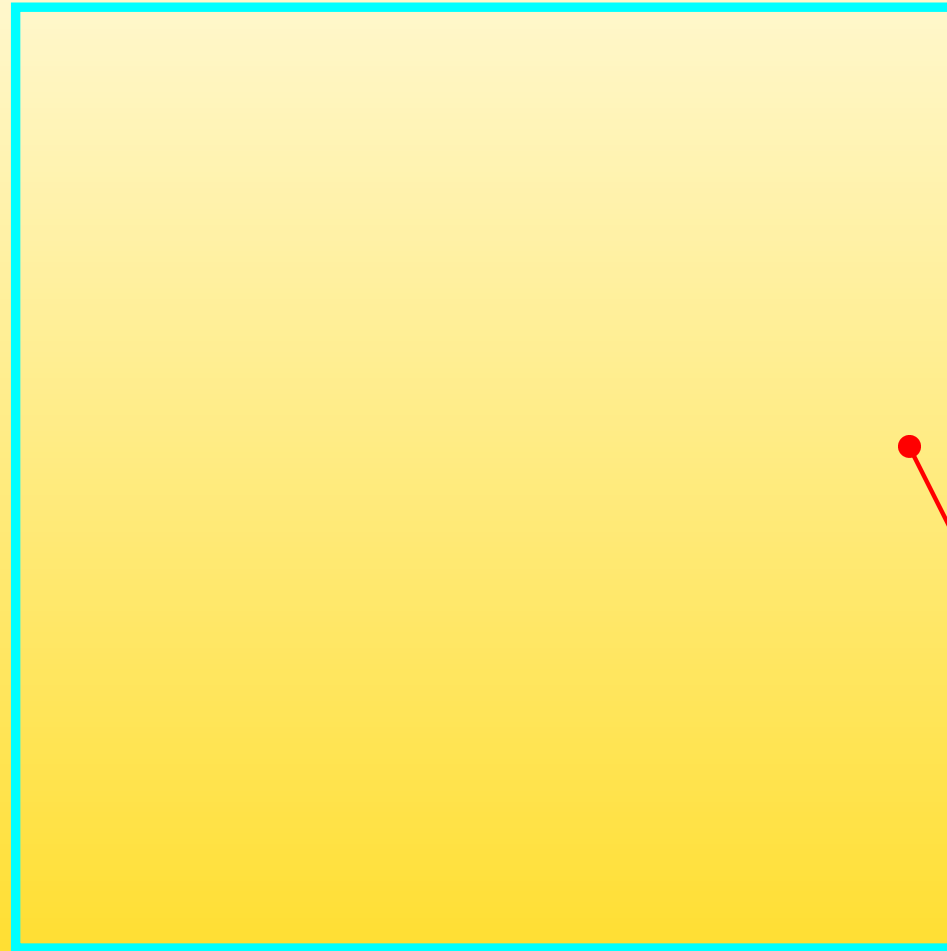


Figure 5: Random walk

End of animation

## 7 – Random walk

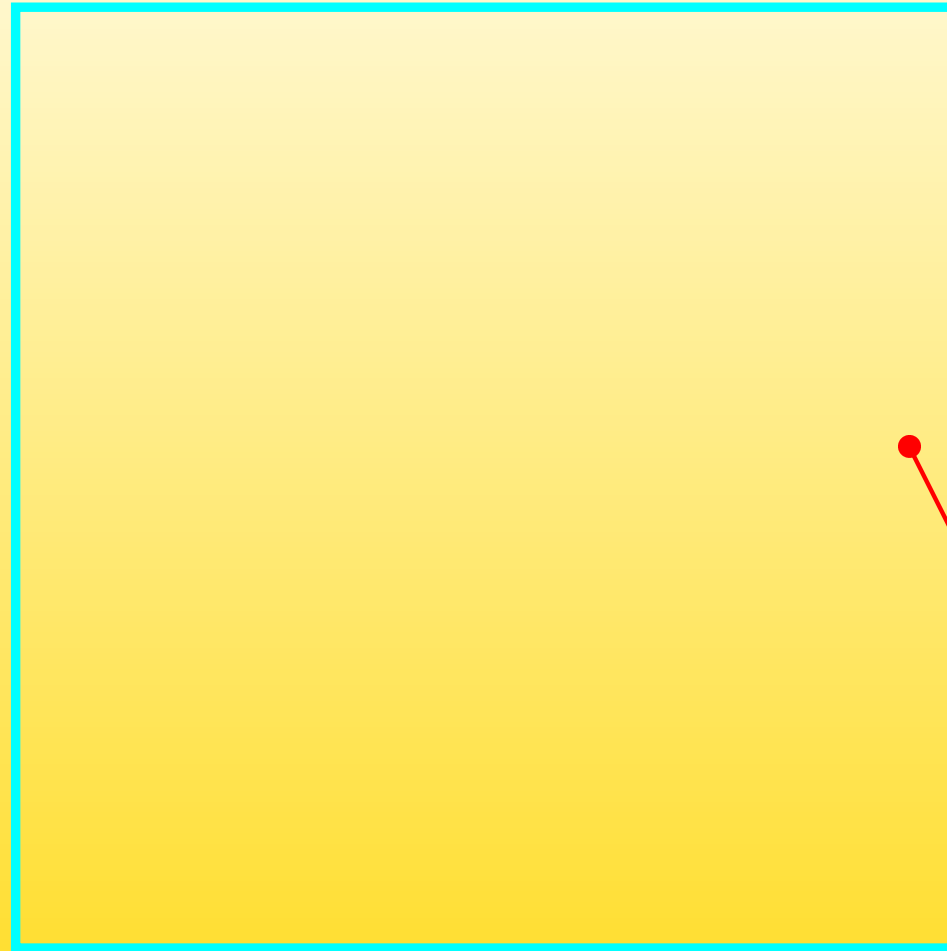


Figure 5: Random walk

End of animation

## 7 – Random walk

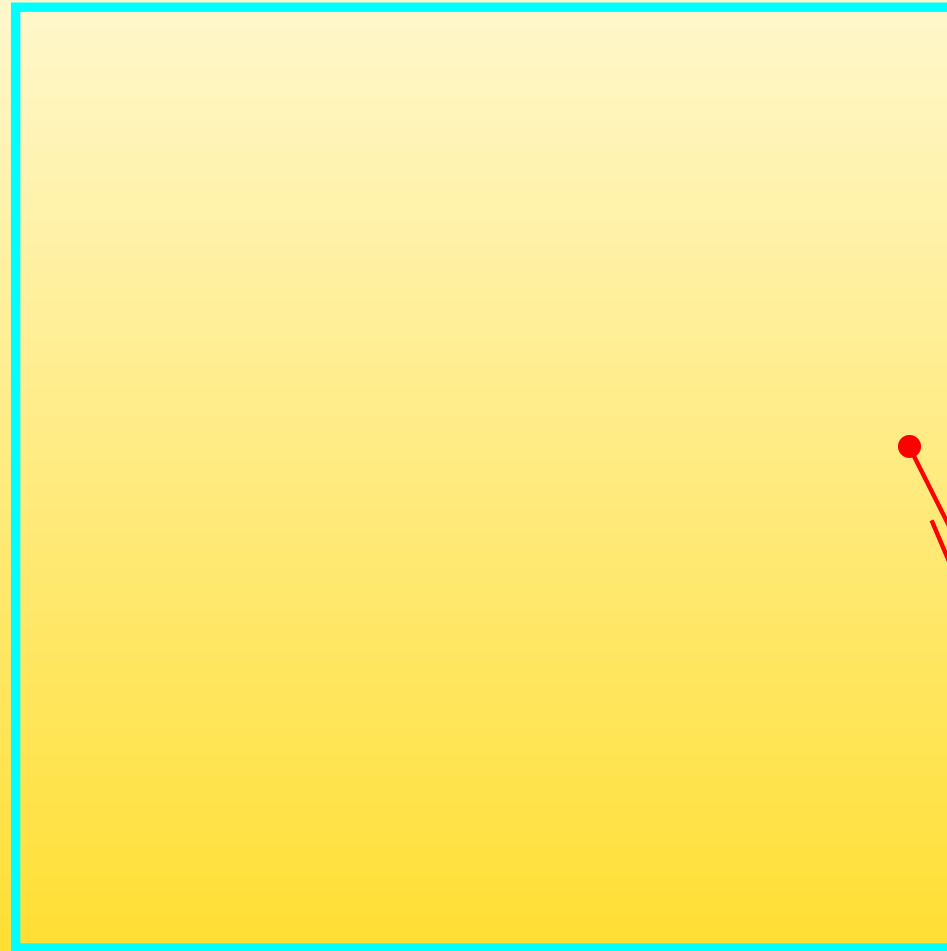


Figure 5: Random walk

End of animation

## 7 – Random walk

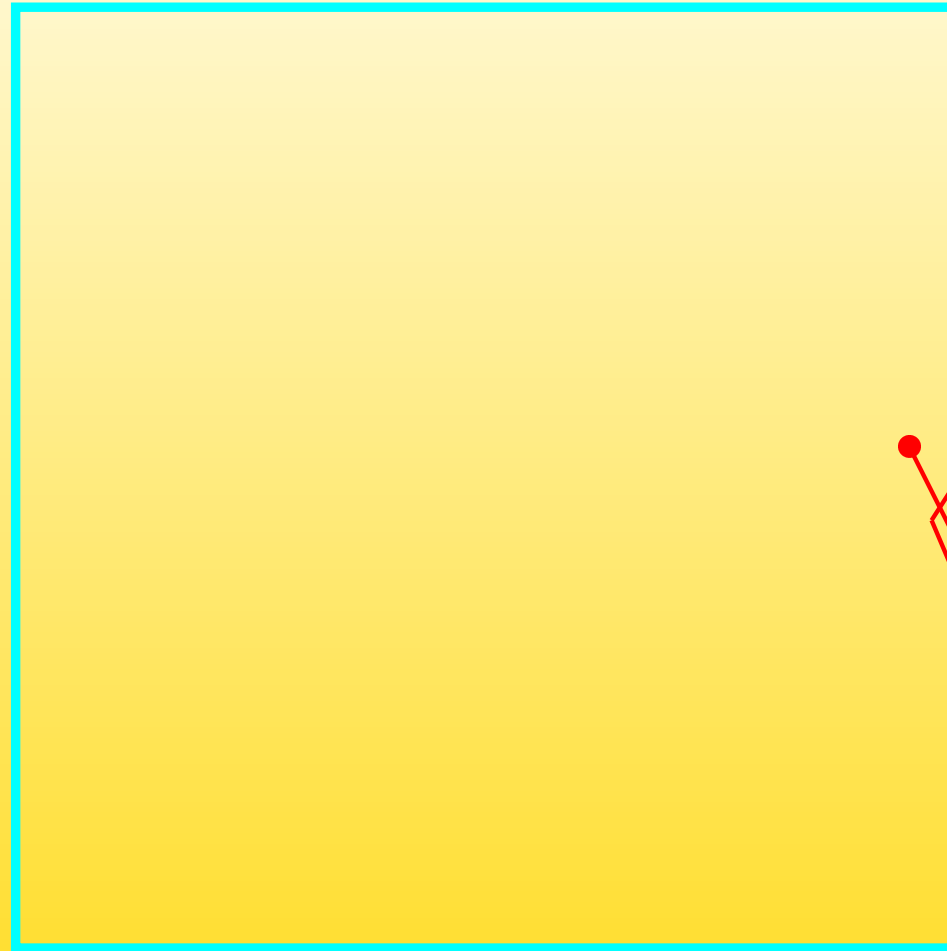


Figure 5: Random walk

End of animation

## 7 – Random walk

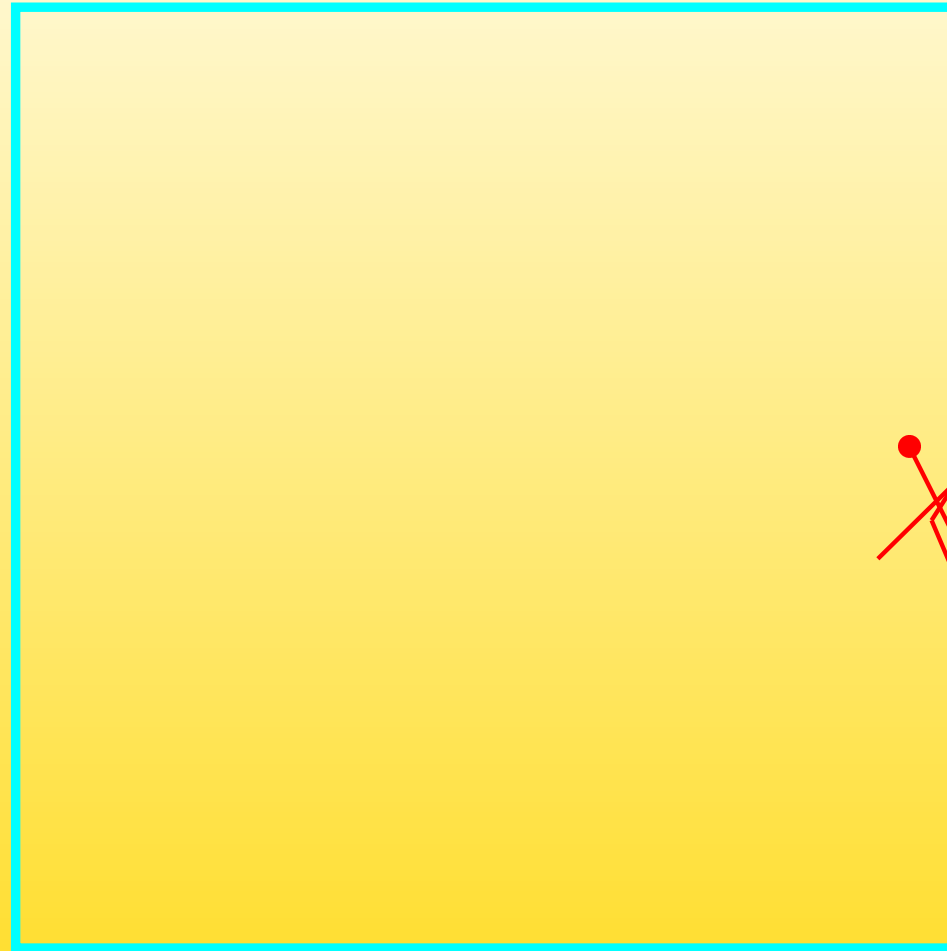


Figure 5: Random walk

End of animation

## 7 – Random walk

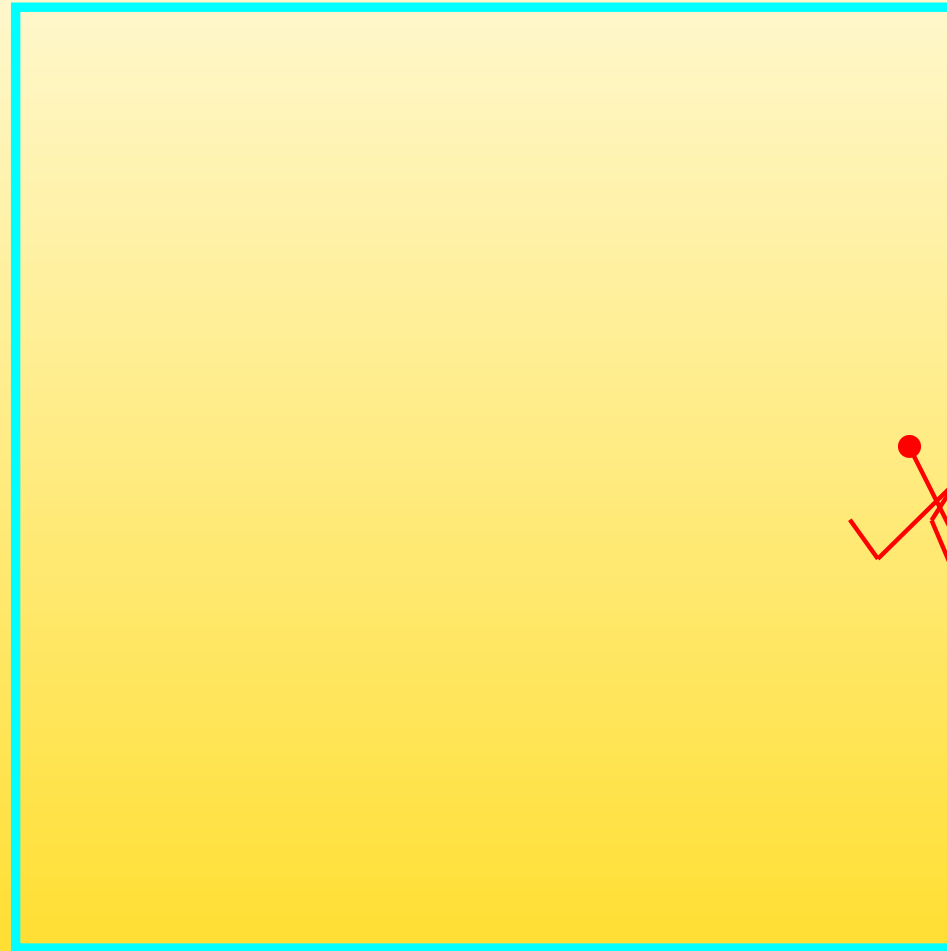


Figure 5: Random walk

End of animation

## 7 – Random walk

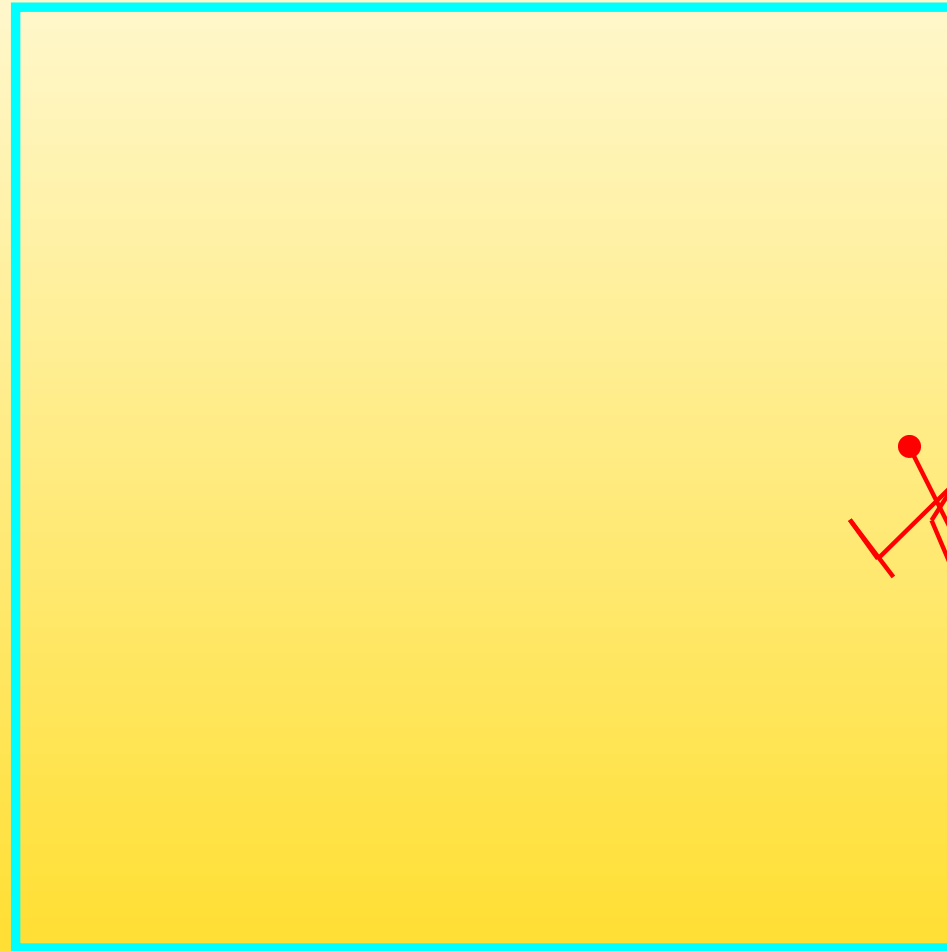


Figure 5: Random walk

End of animation



## 7 – Random walk

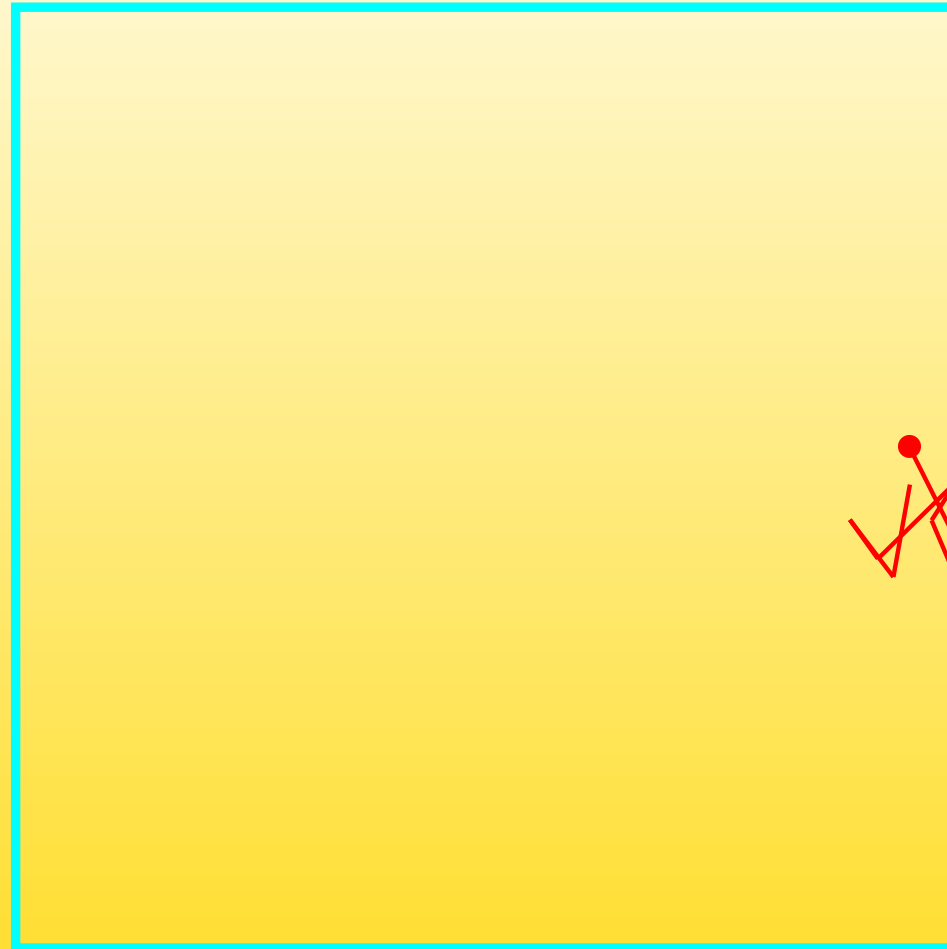


Figure 5: Random walk

End of animation

## 7 – Random walk

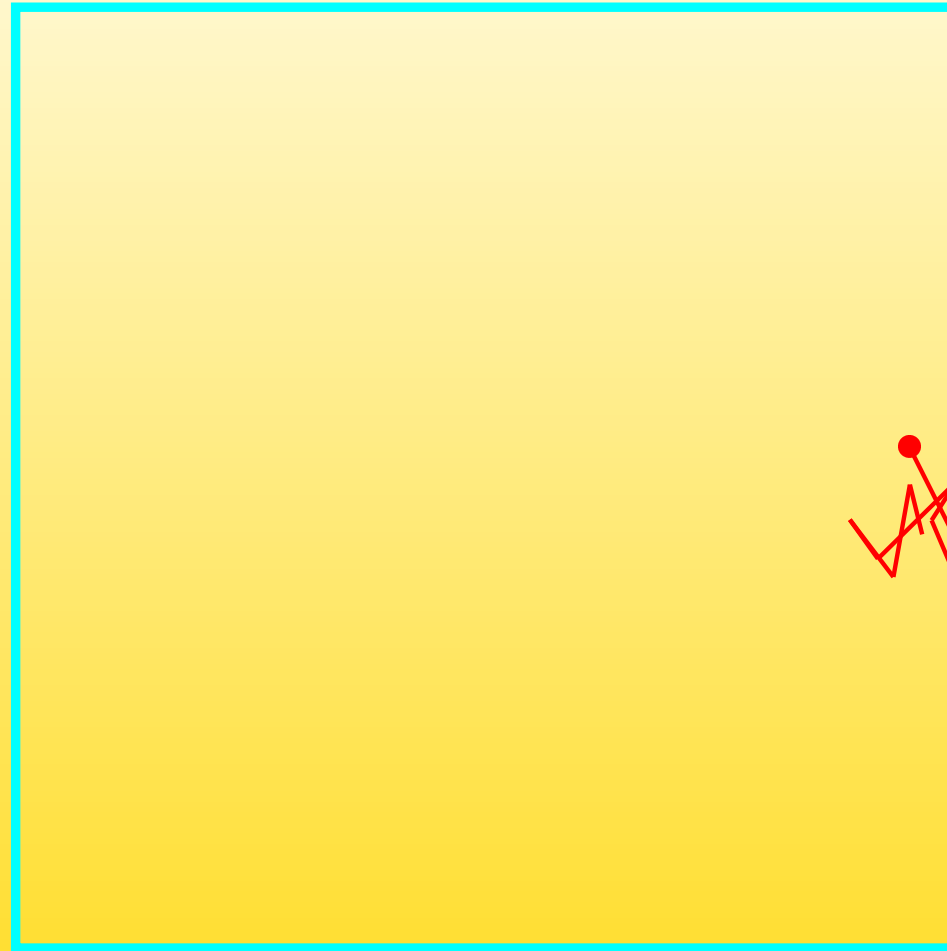


Figure 5: Random walk

End of animation

## 7 – Random walk

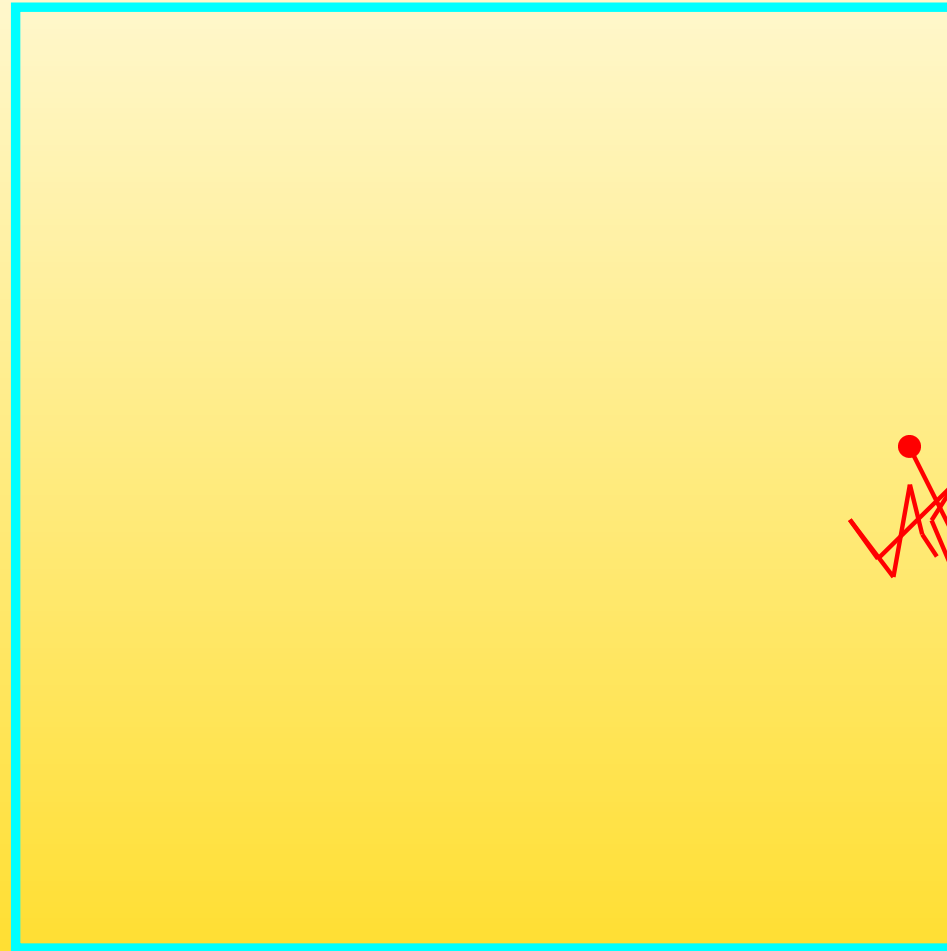


Figure 5: Random walk

End of animation

## 7 – Random walk

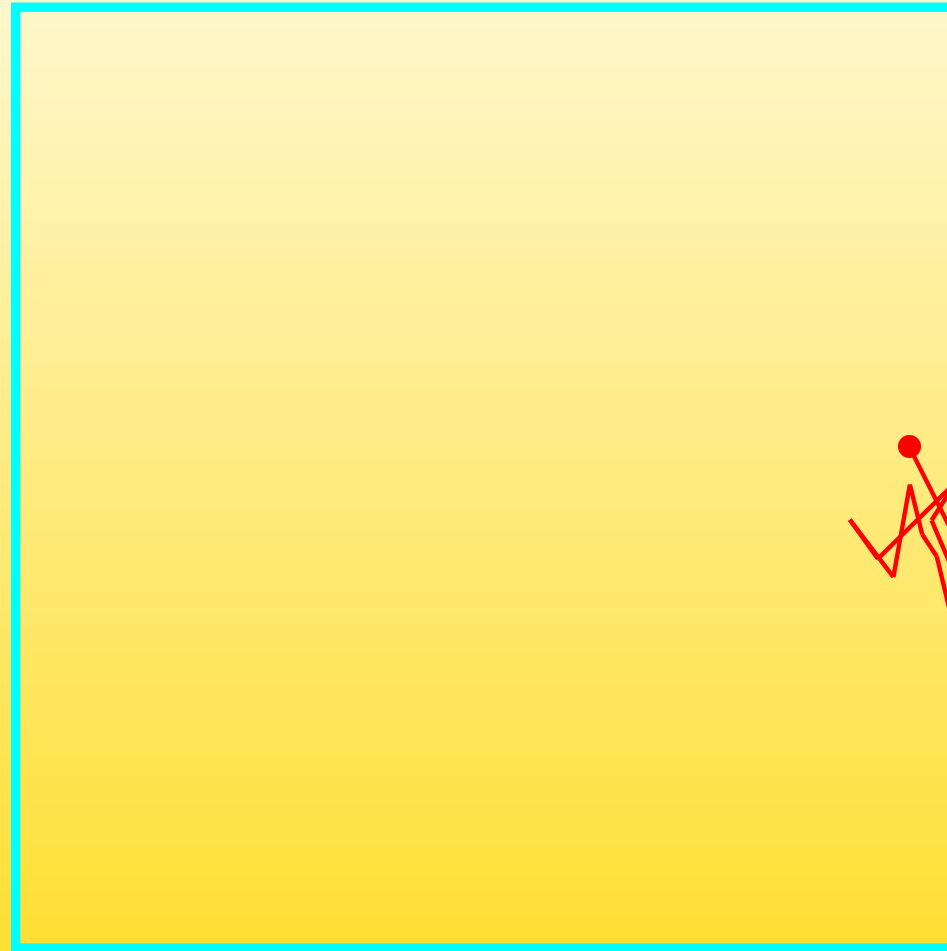


Figure 5: Random walk

End of animation

## 7 – Random walk

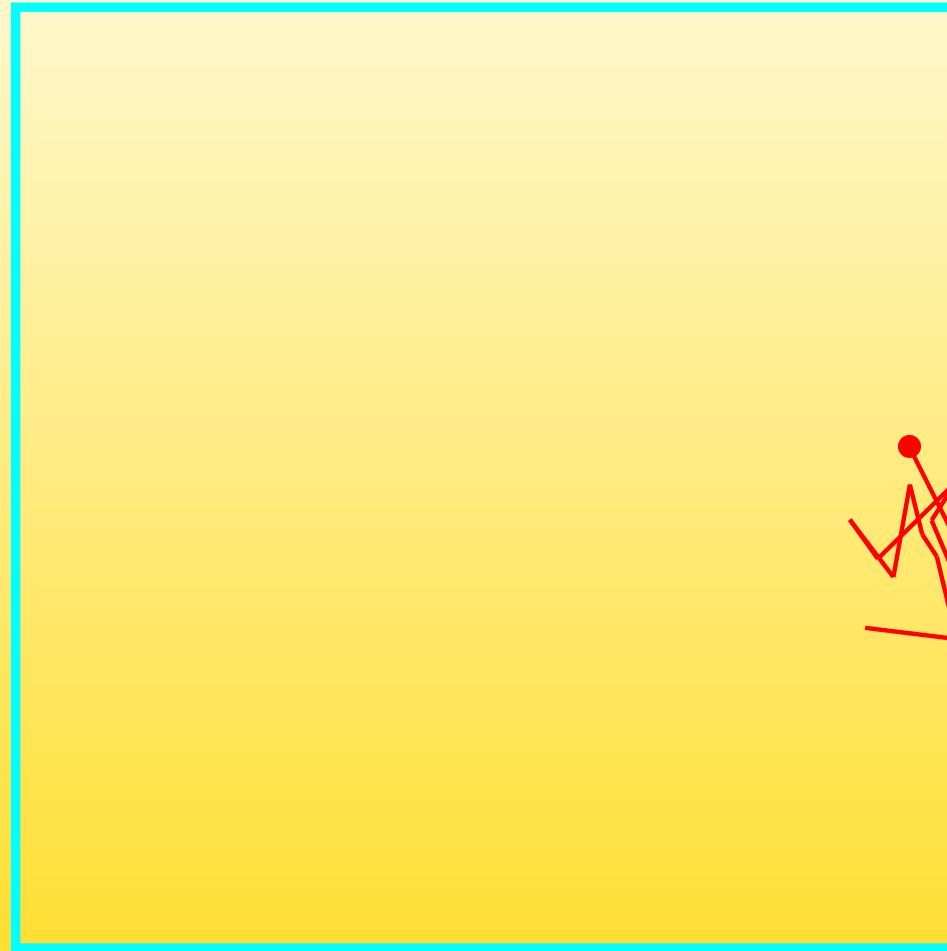


Figure 5: Random walk

End of animation

## 7 – Random walk

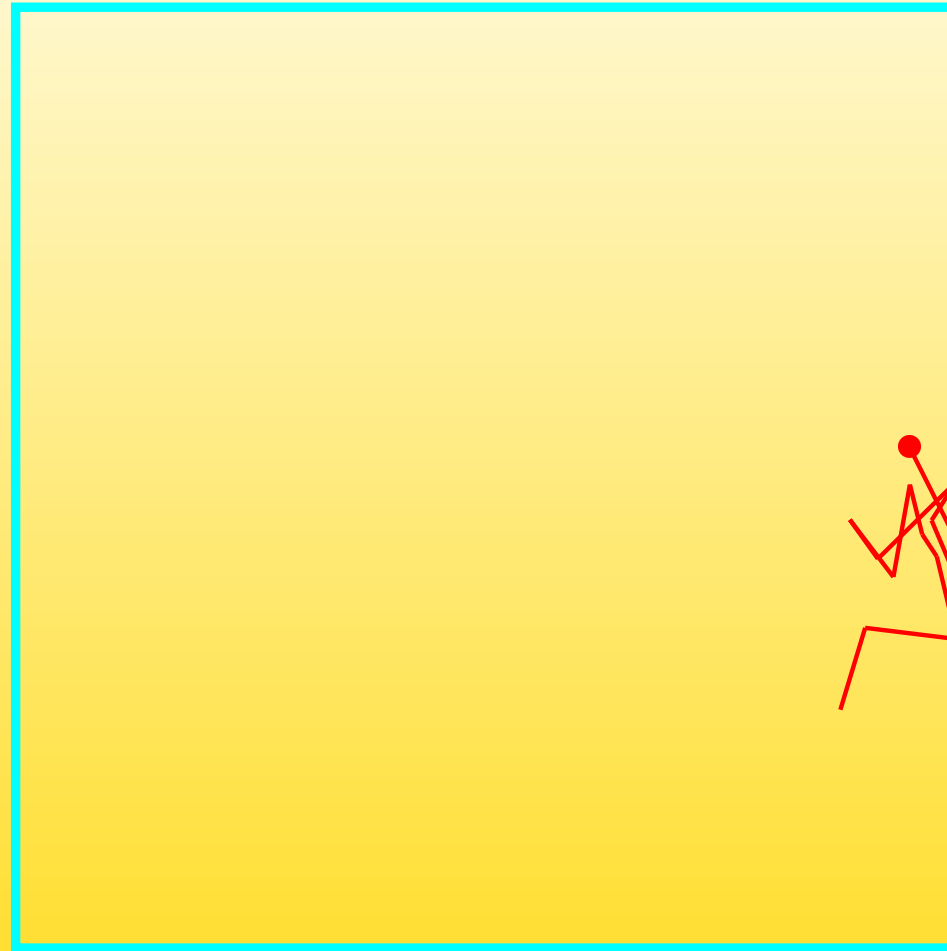


Figure 5: Random walk

End of animation

## 7 – Random walk

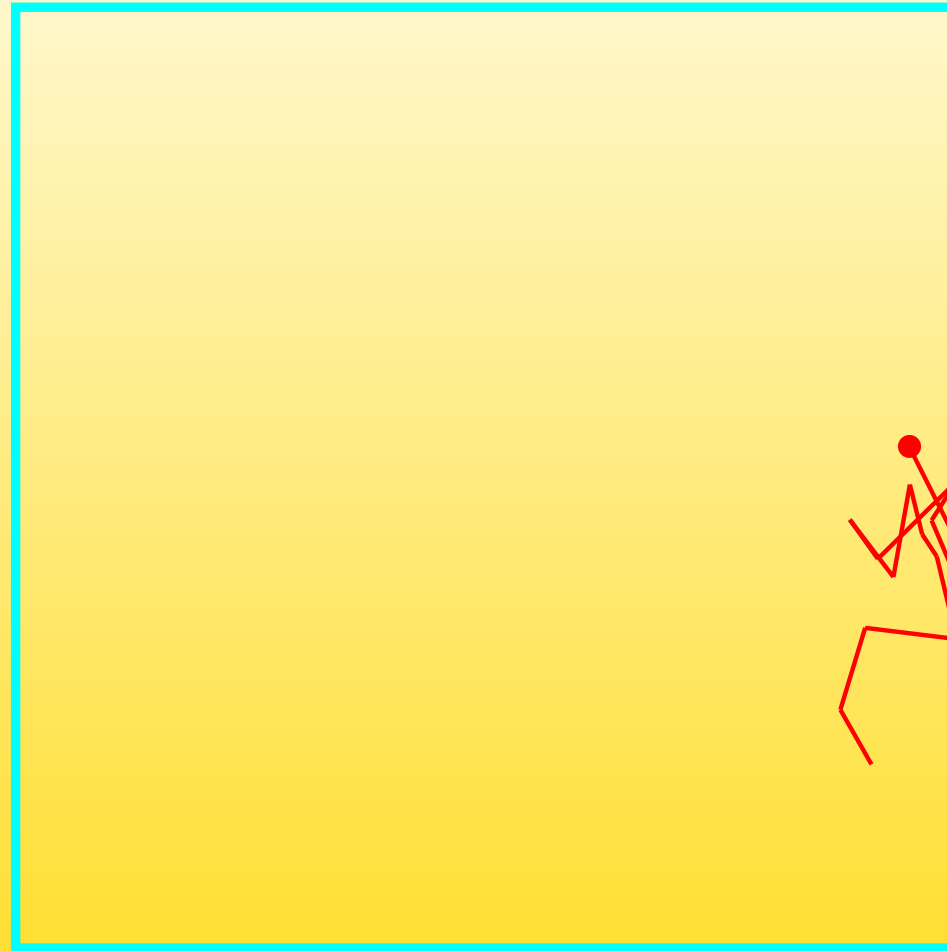


Figure 5: Random walk

End of animation

## 7 – Random walk

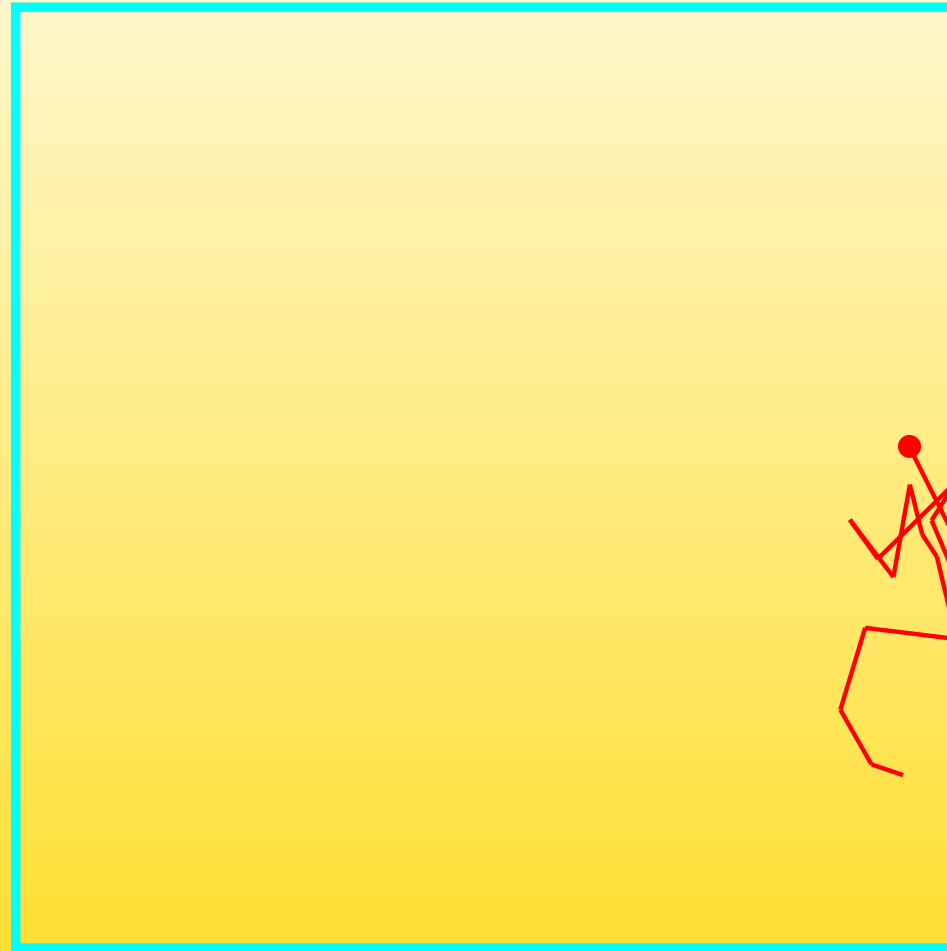


Figure 5: Random walk

End of animation



## 7 – Random walk

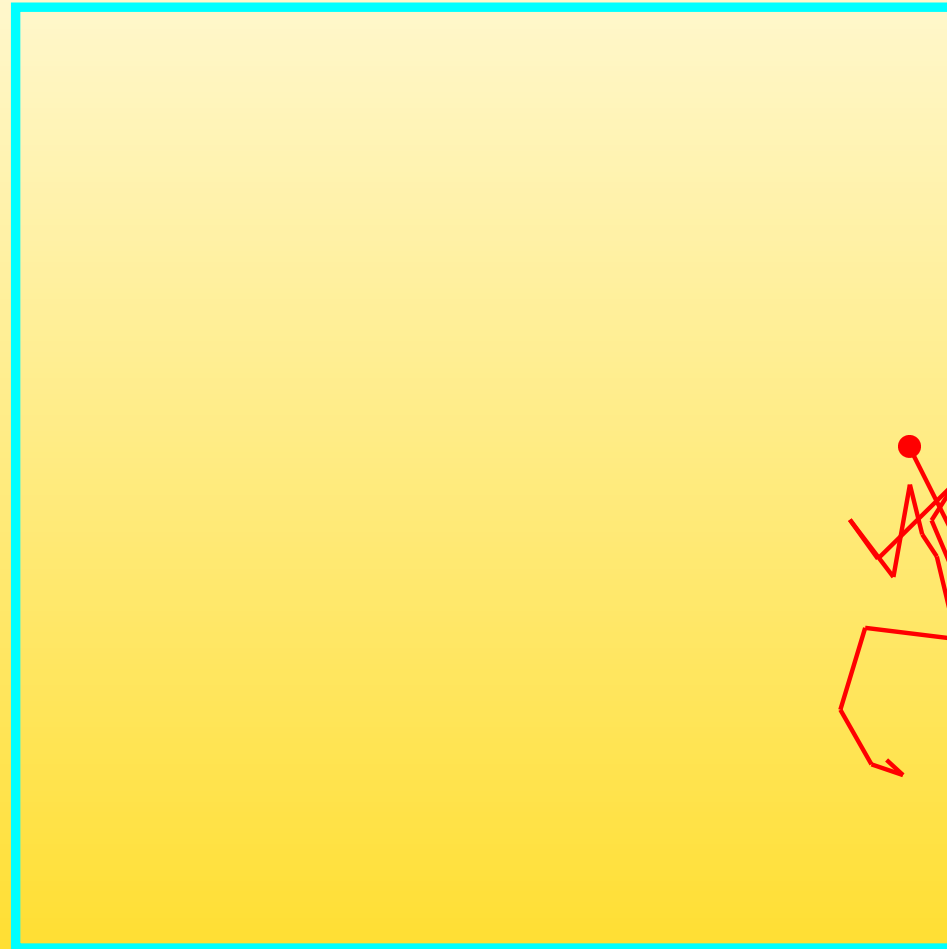


Figure 5: Random walk

End of animation

## 7 – Random walk

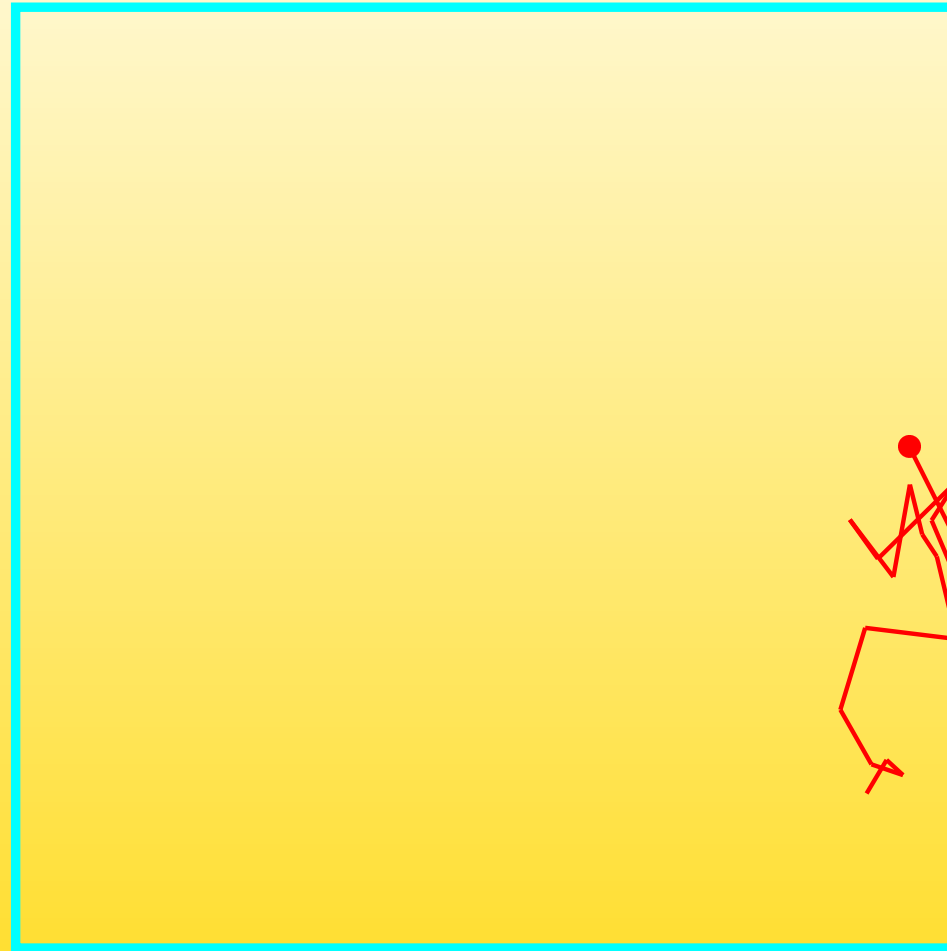


Figure 5: Random walk

End of animation

## 7 – Random walk

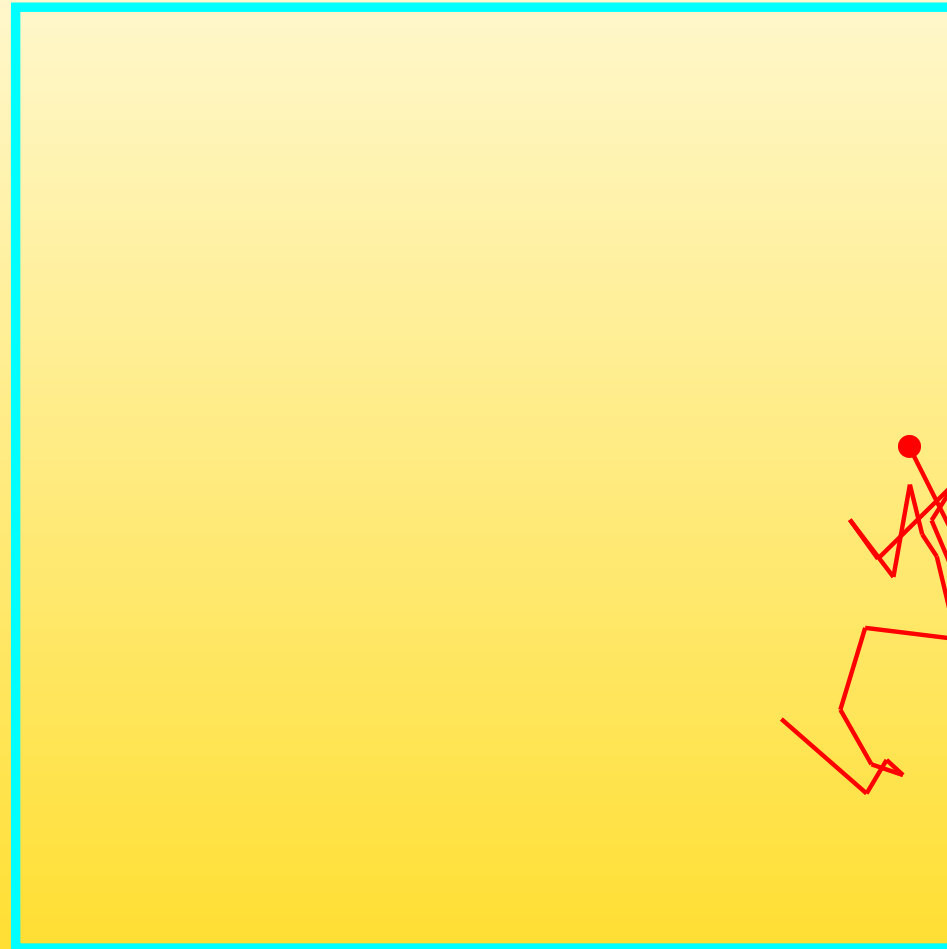


Figure 5: Random walk

End of animation

## 7 – Random walk

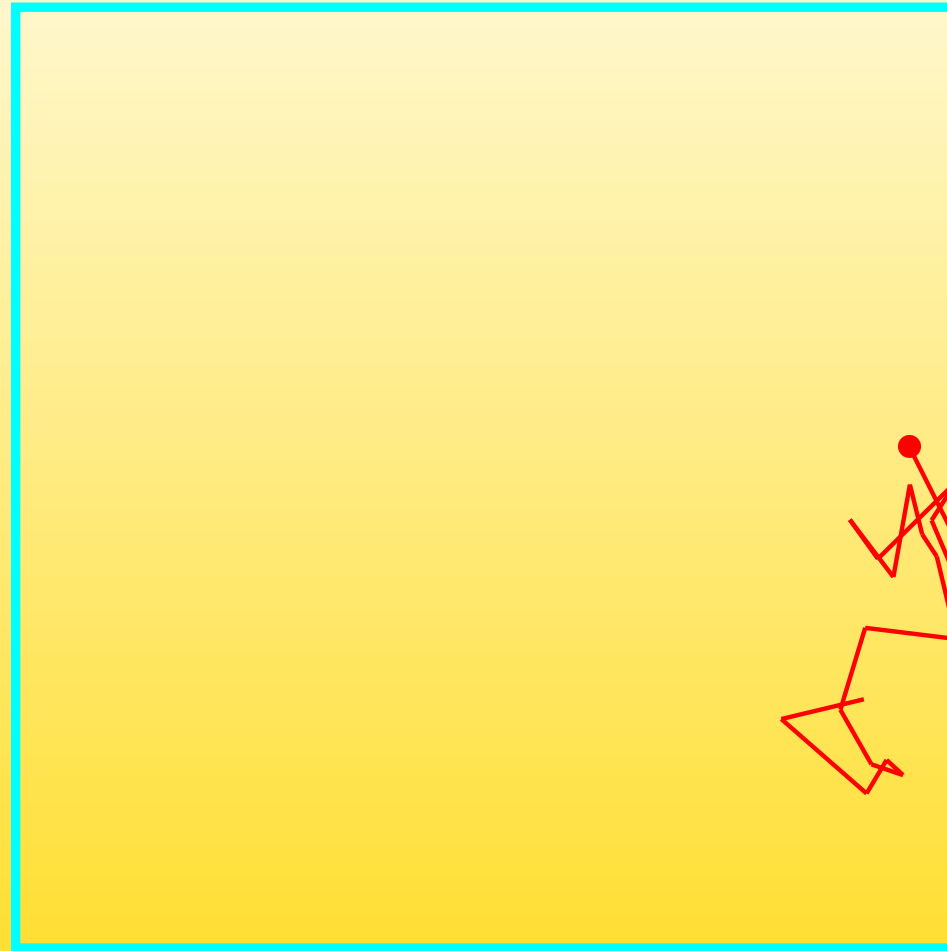


Figure 5: Random walk

End of animation

## 7 – Random walk

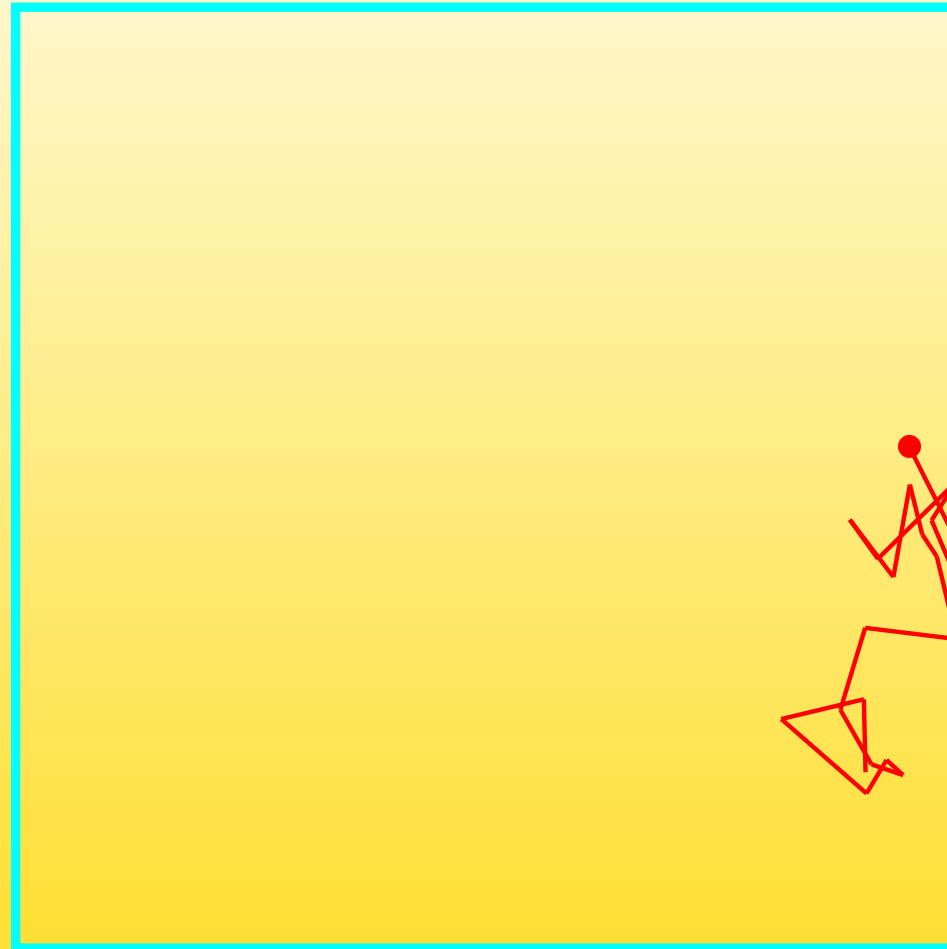


Figure 5: Random walk

End of animation

## 7 – Random walk

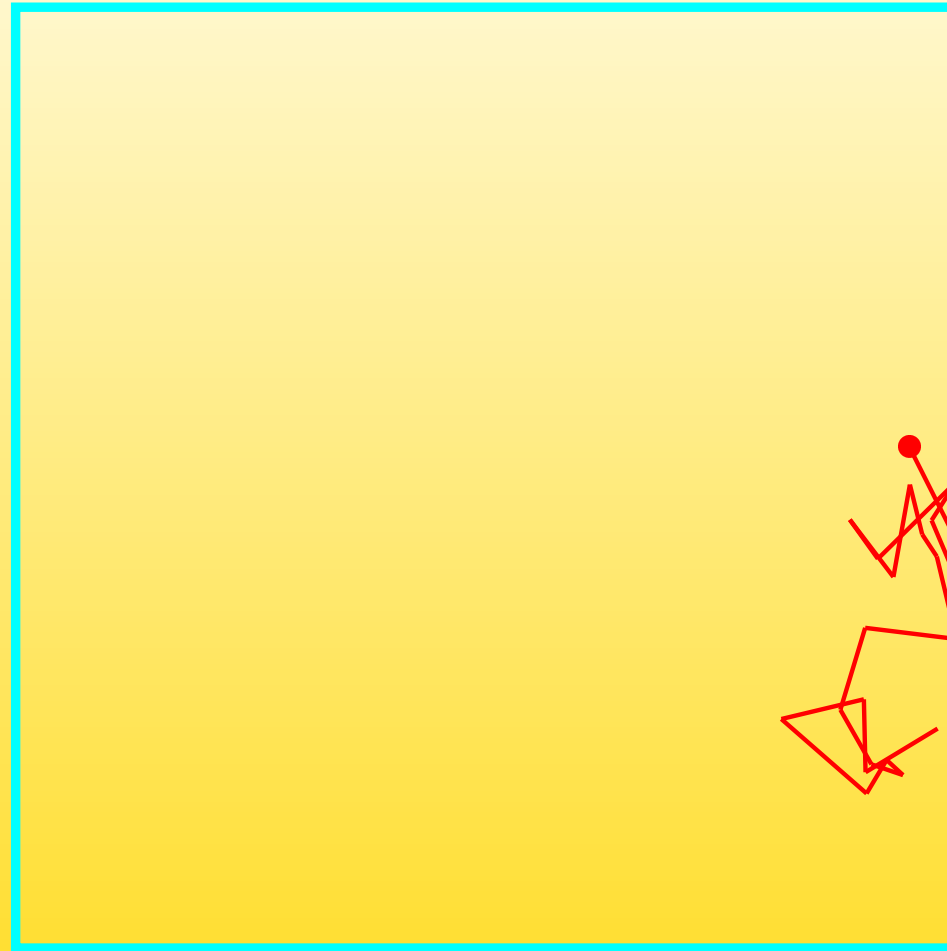


Figure 5: Random walk

End of animation

## 7 – Random walk

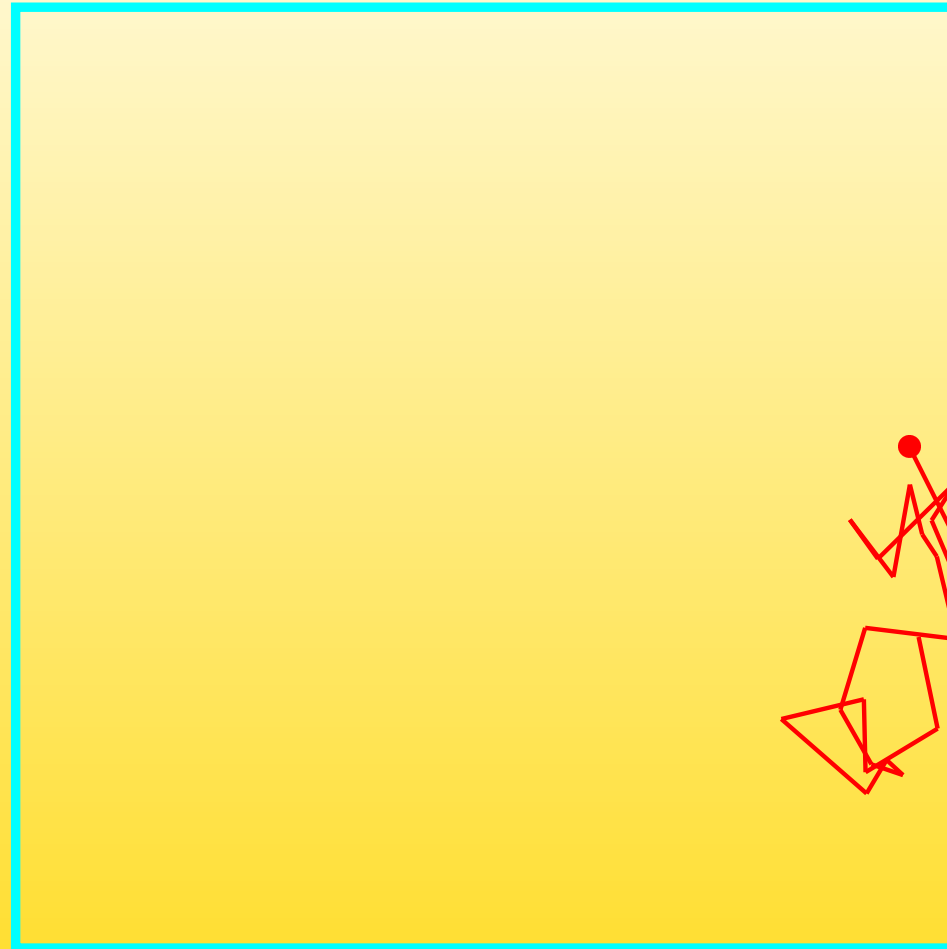


Figure 5: Random walk

End of animation

## 7 – Random walk

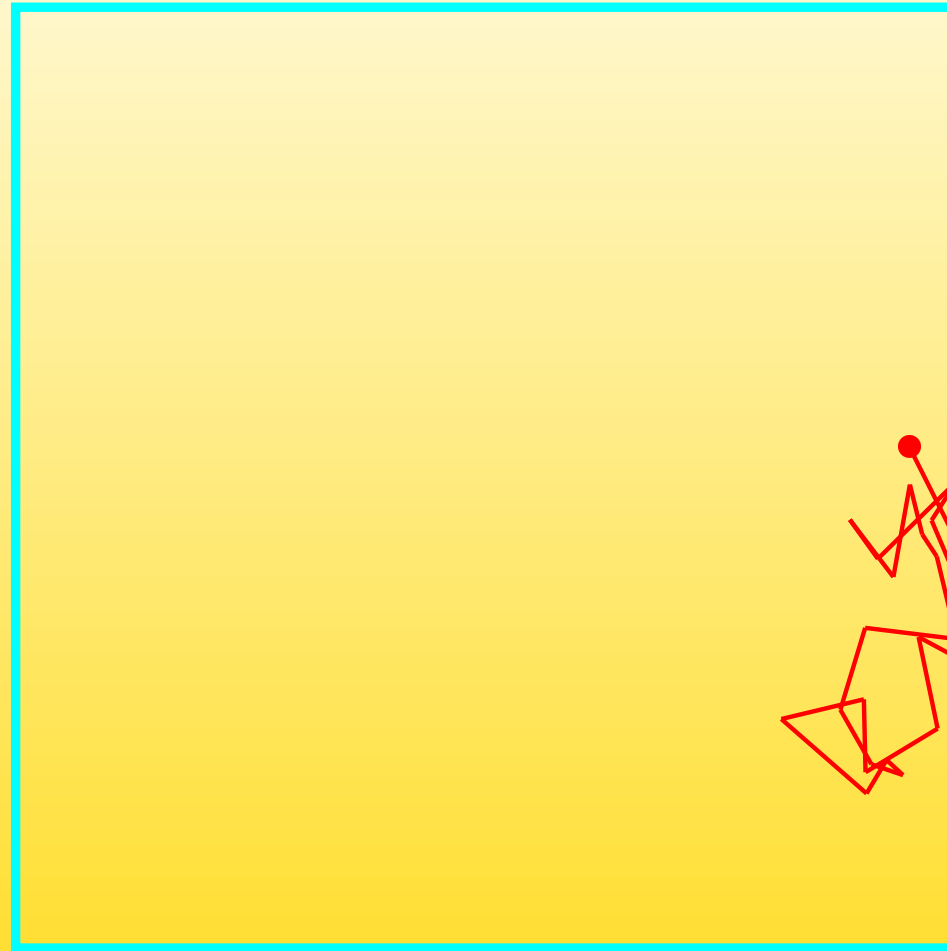


Figure 5: Random walk

End of animation



## 7 – Random walk

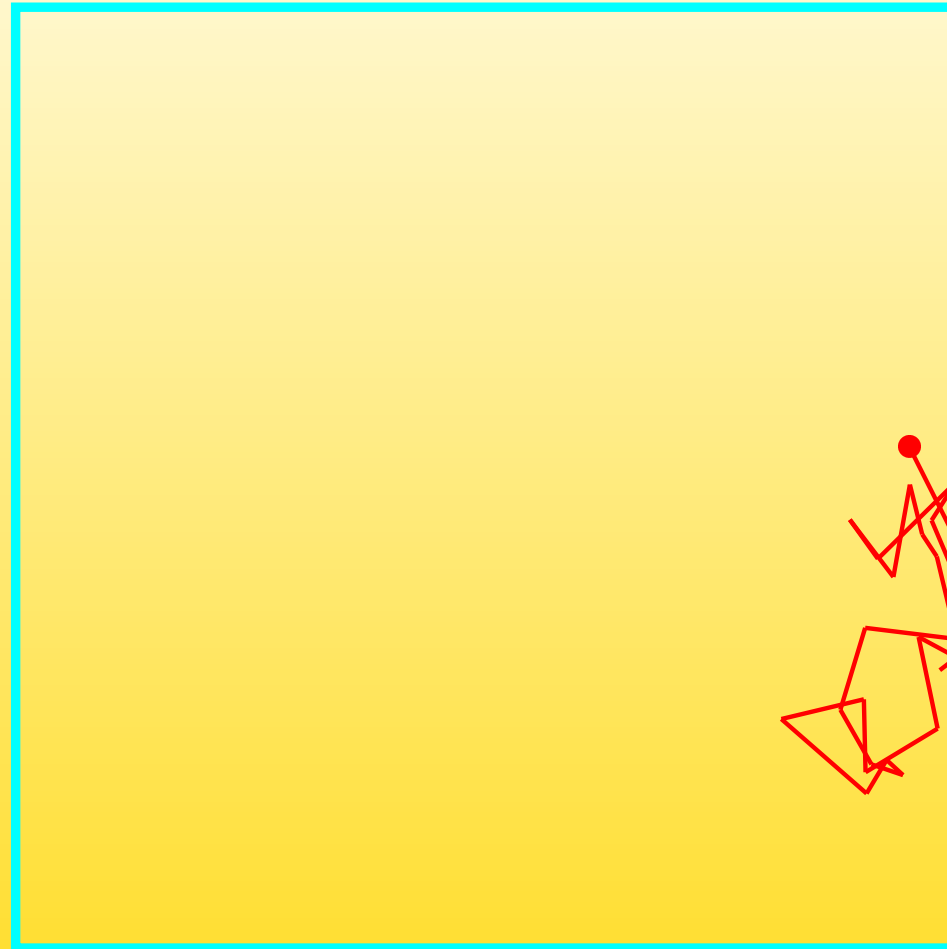


Figure 5: Random walk

End of animation

## 7 – Random walk

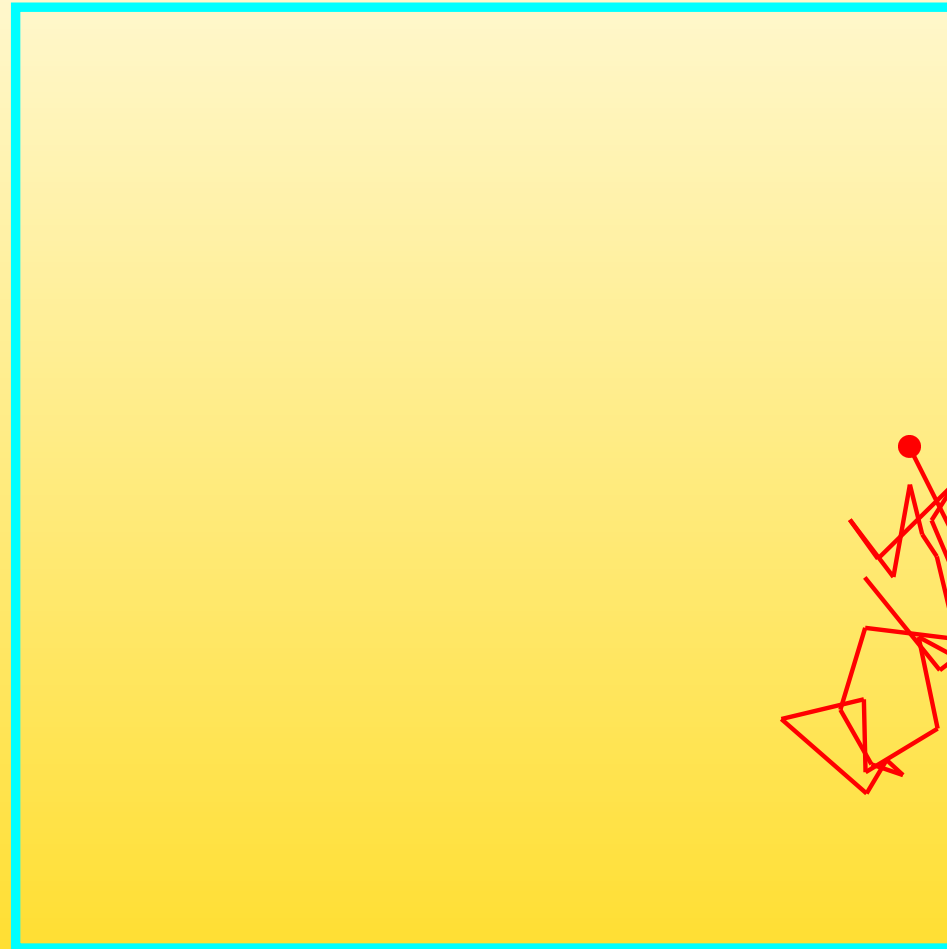


Figure 5: Random walk

End of animation

## 7 – Random walk

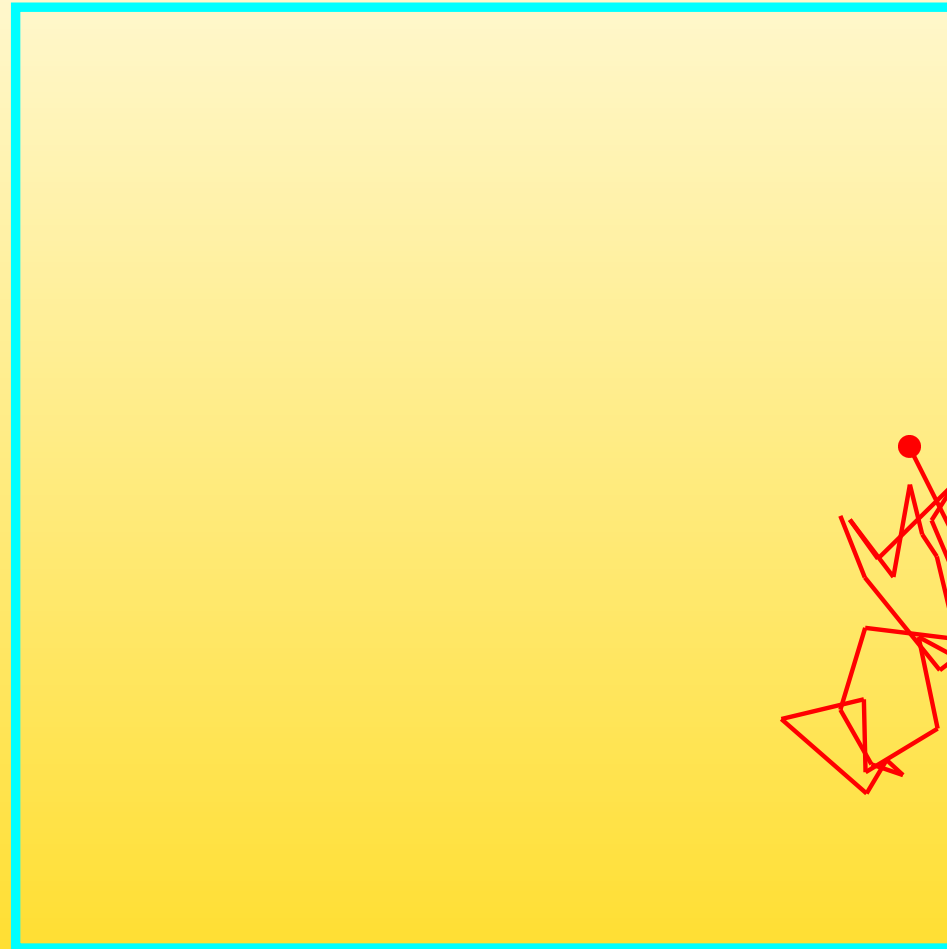


Figure 5: Random walk

End of animation

## 7 – Random walk

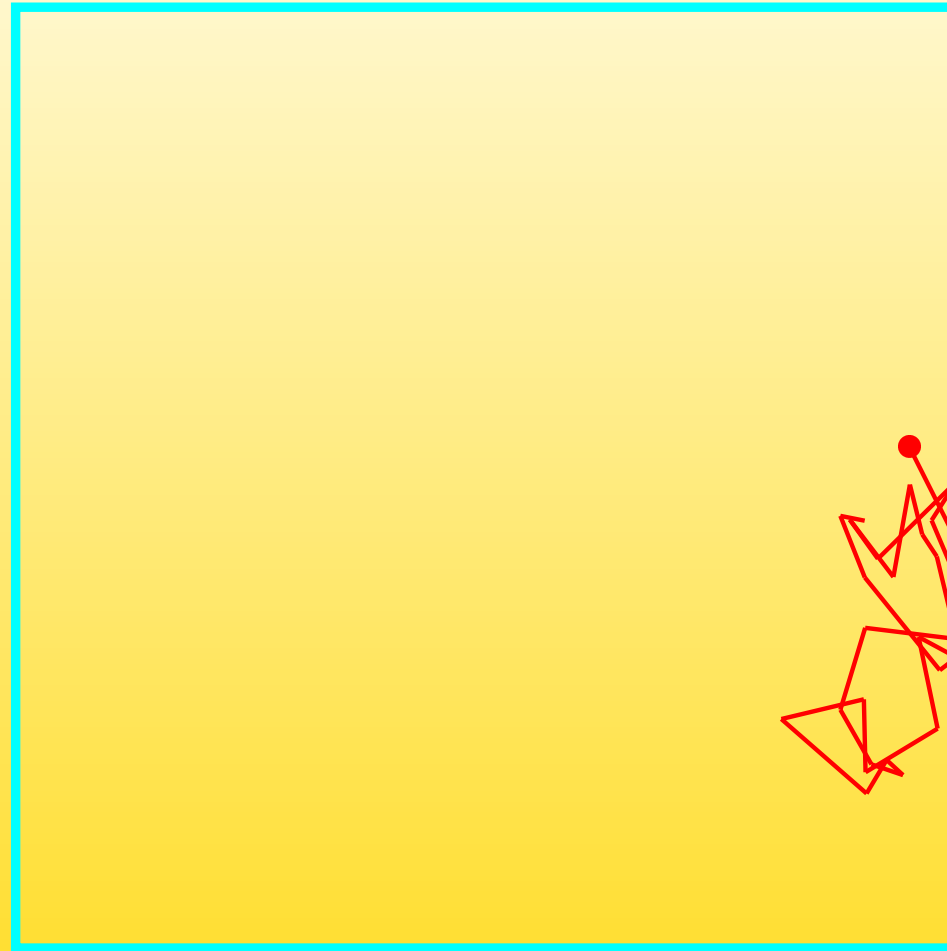


Figure 5: Random walk

End of animation

## 7 – Random walk

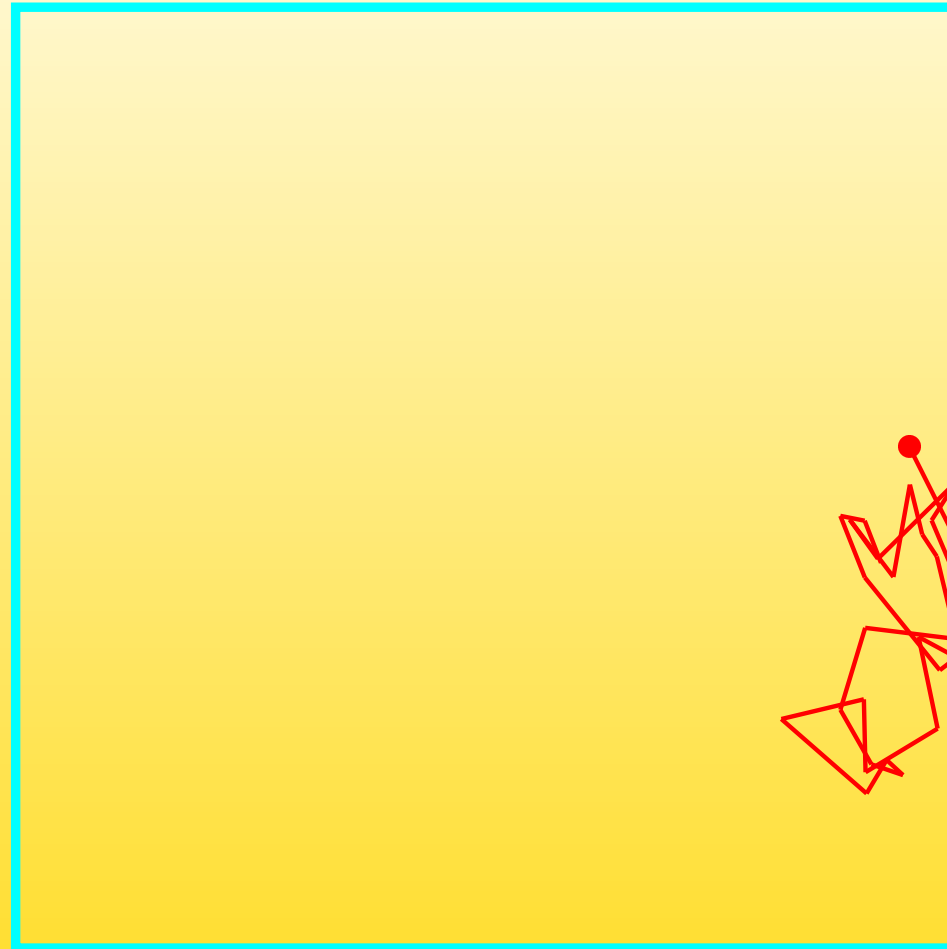


Figure 5: Random walk

End of animation

## 7 – Random walk

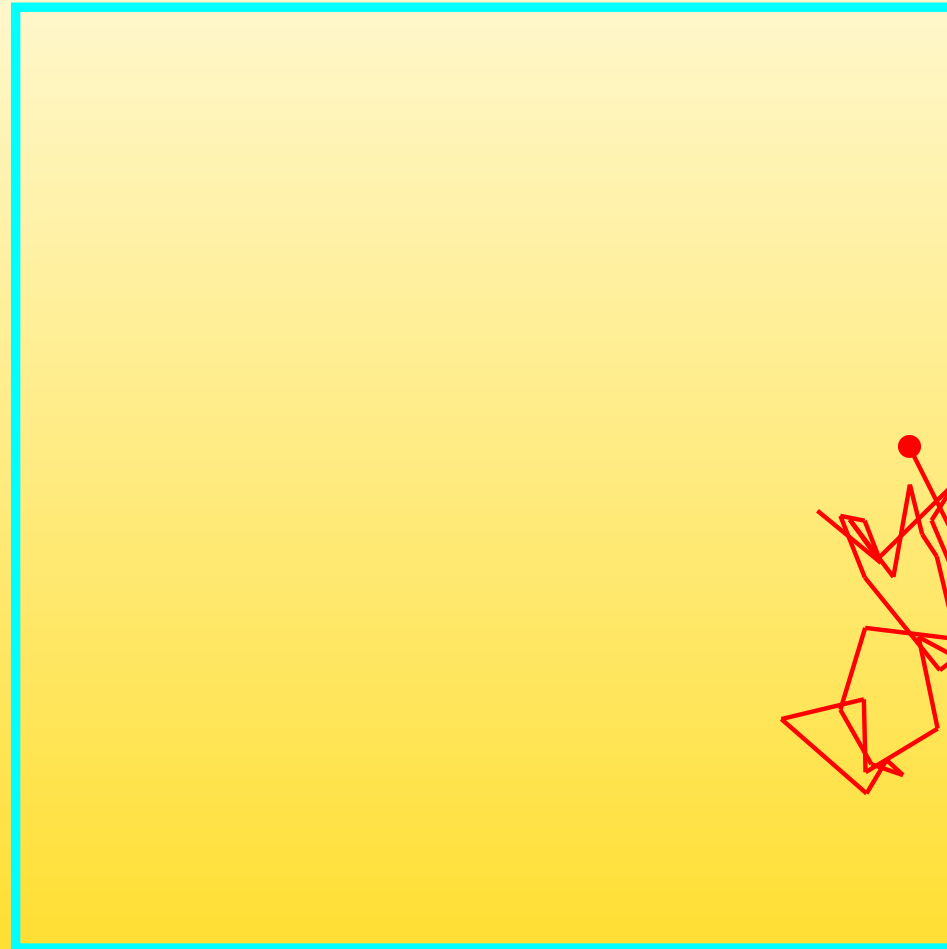


Figure 5: Random walk

End of animation

## 7 – Random walk

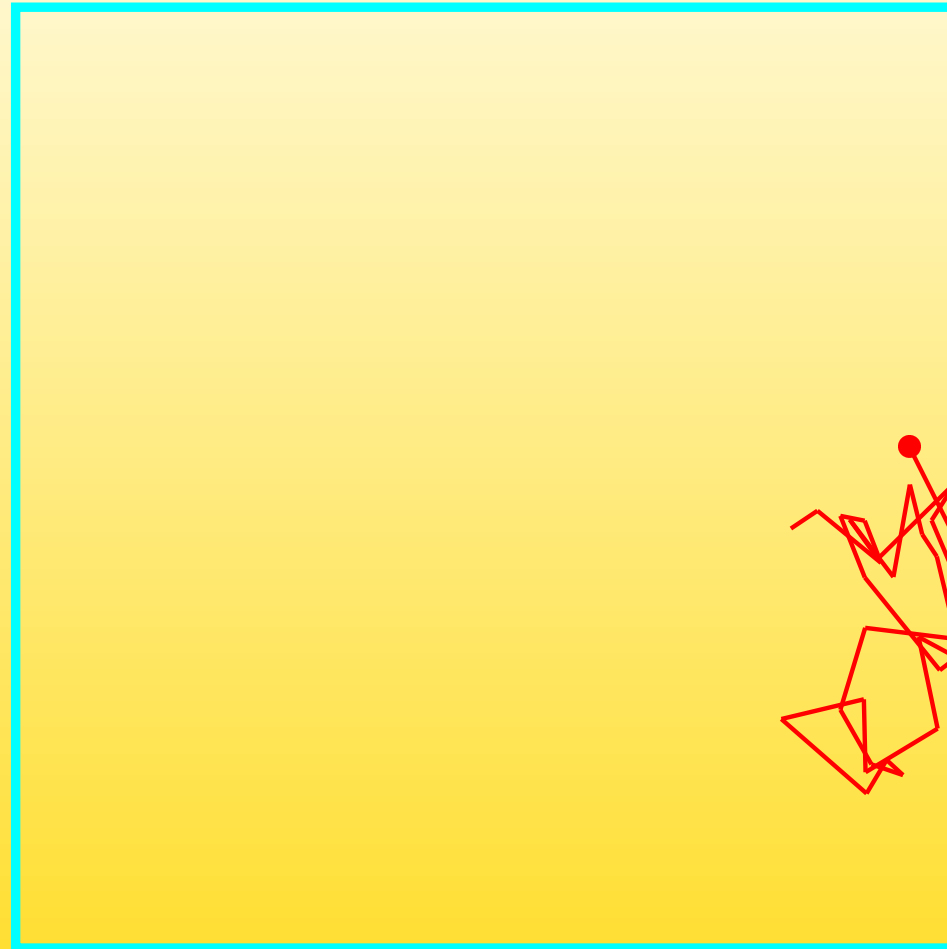


Figure 5: Random walk

End of animation

## 7 – Random walk

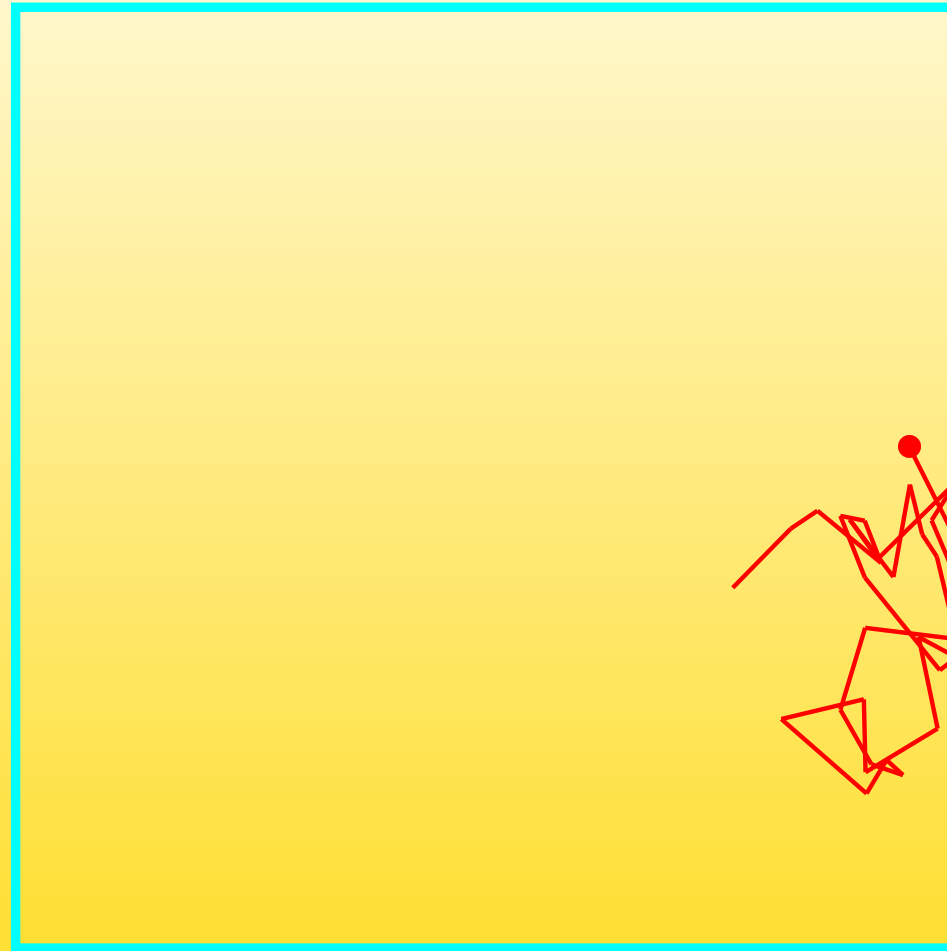


Figure 5: Random walk

End of animation



## 7 – Random walk

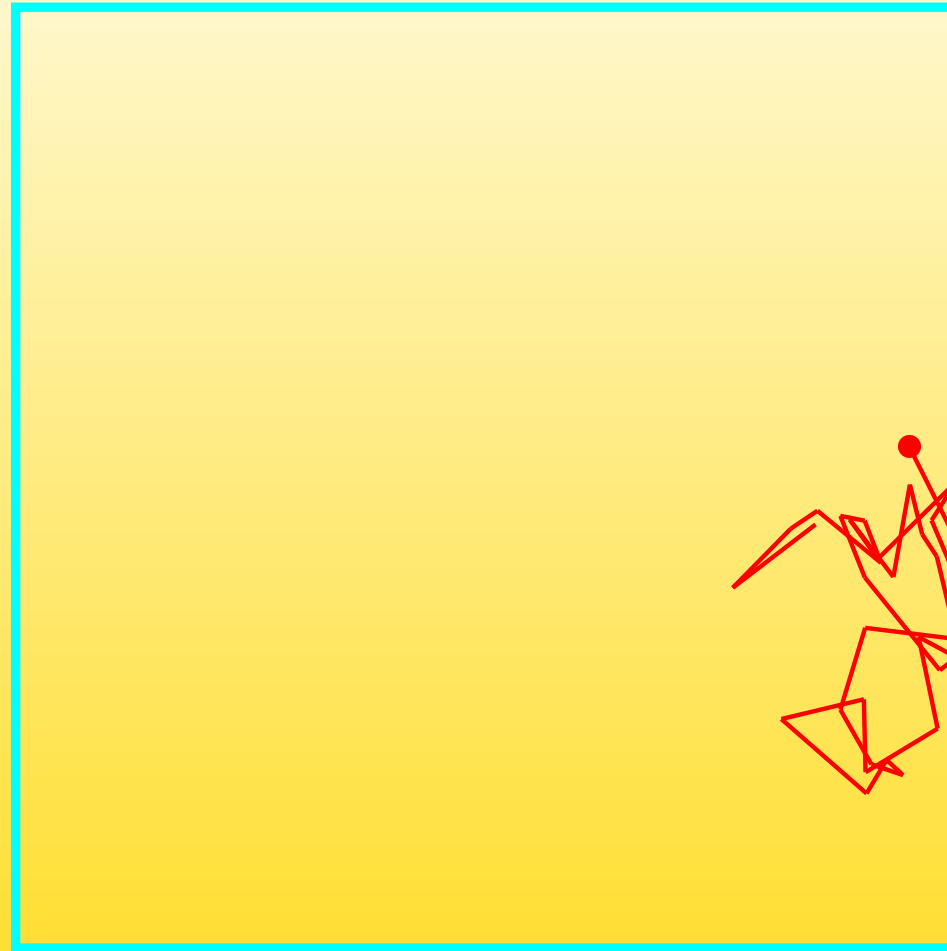


Figure 5: Random walk

End of animation

## 7 – Random walk

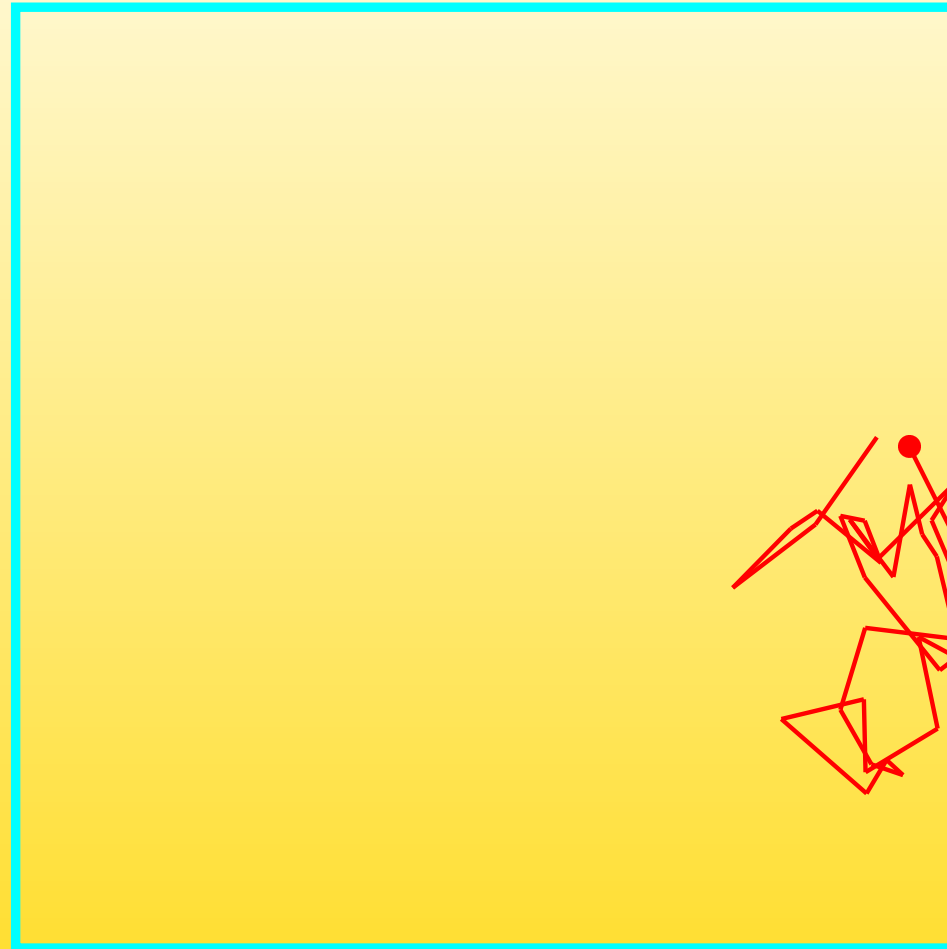


Figure 5: Random walk

End of animation

## 7 – Random walk

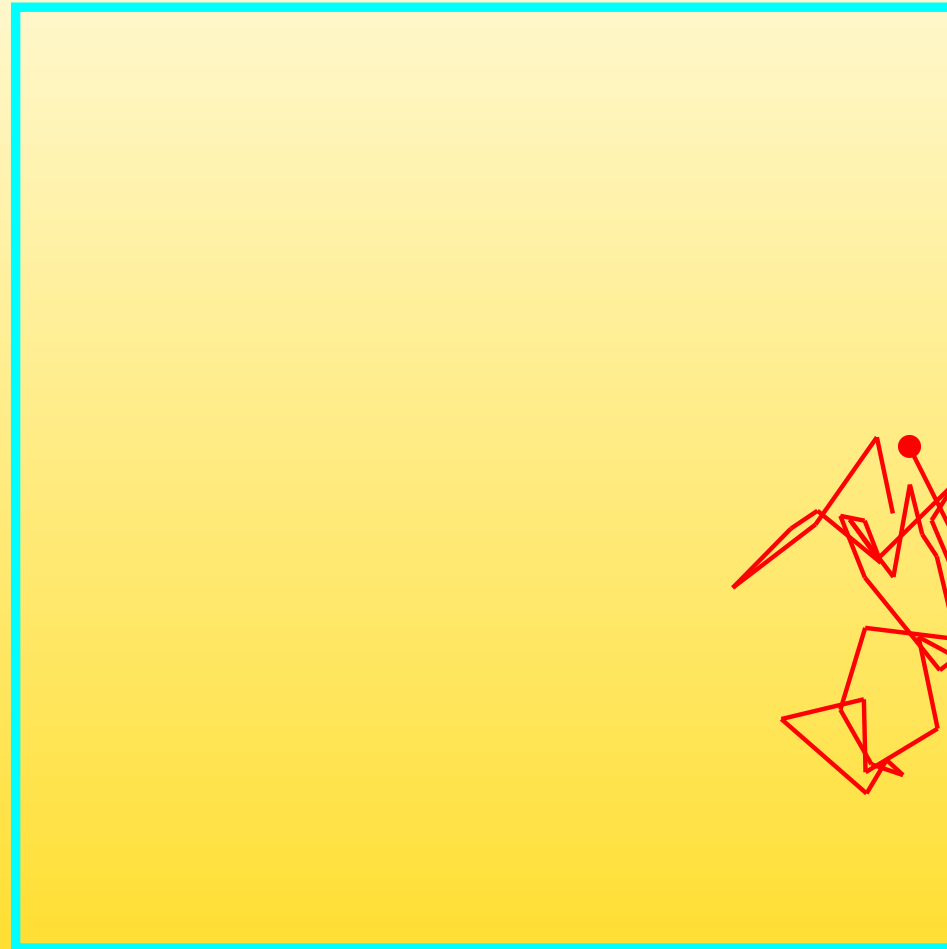


Figure 5: Random walk

End of animation

## 7 – Random walk

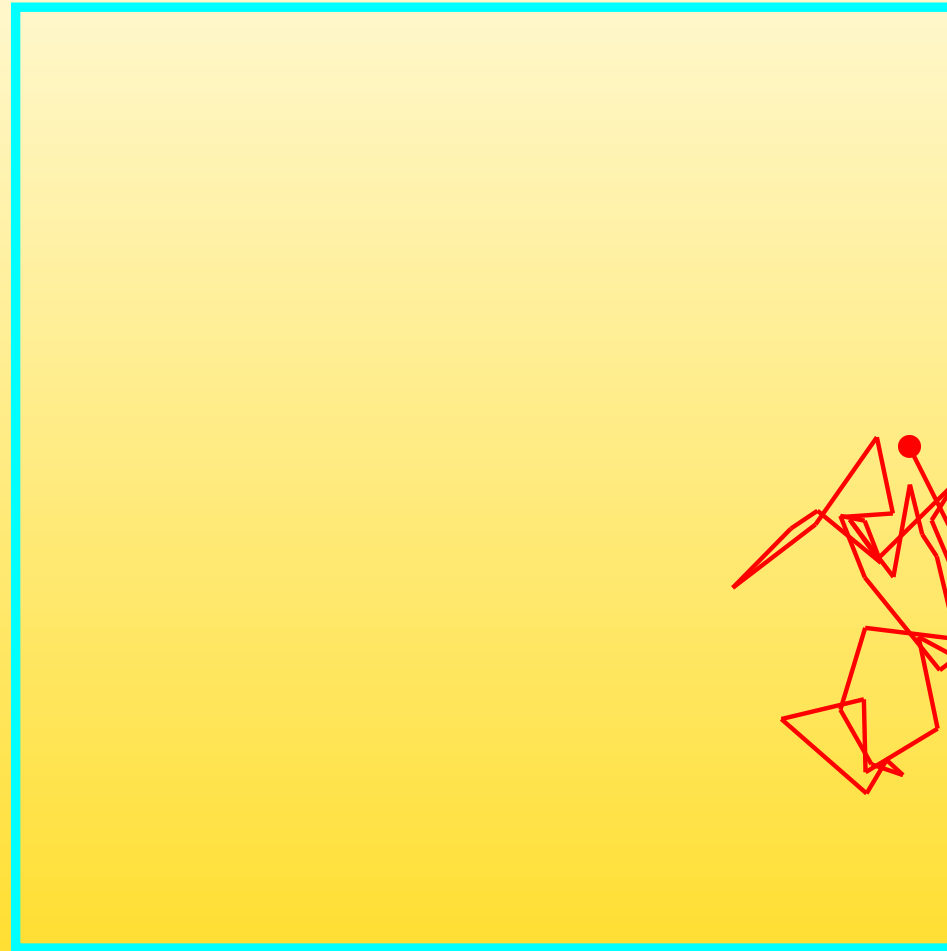


Figure 5: Random walk

End of animation

## 7 – Random walk

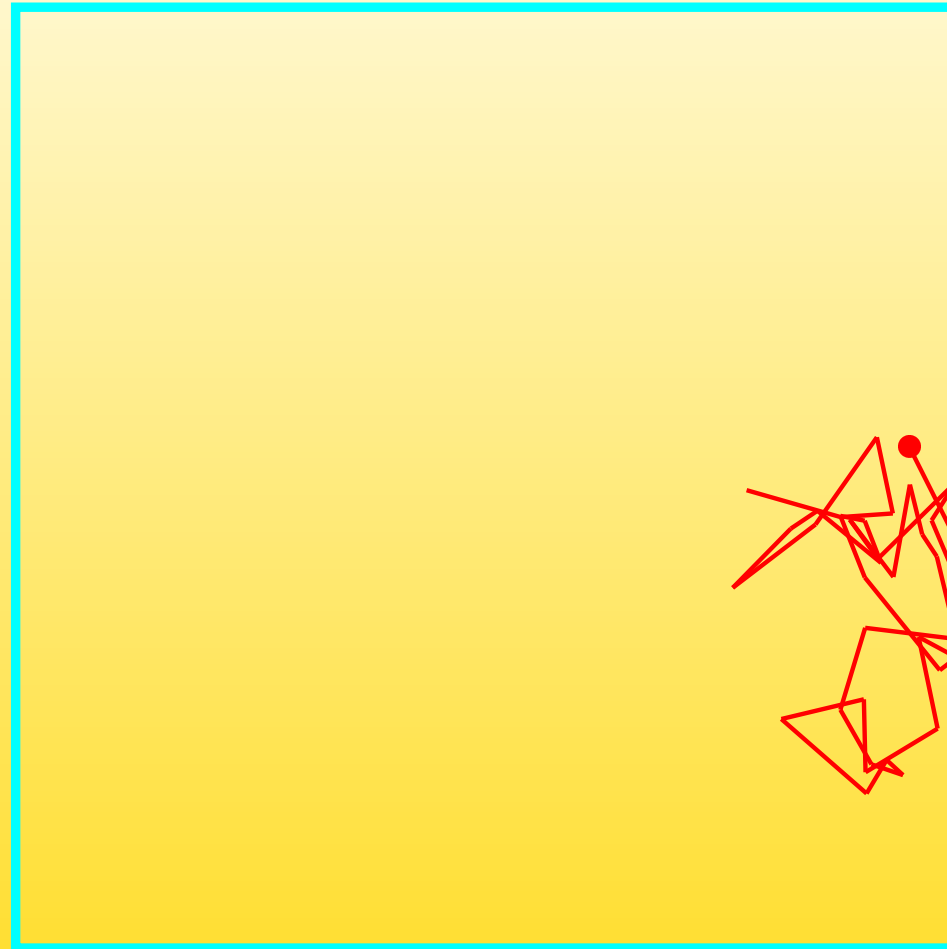


Figure 5: Random walk

End of animation

## 7 – Random walk

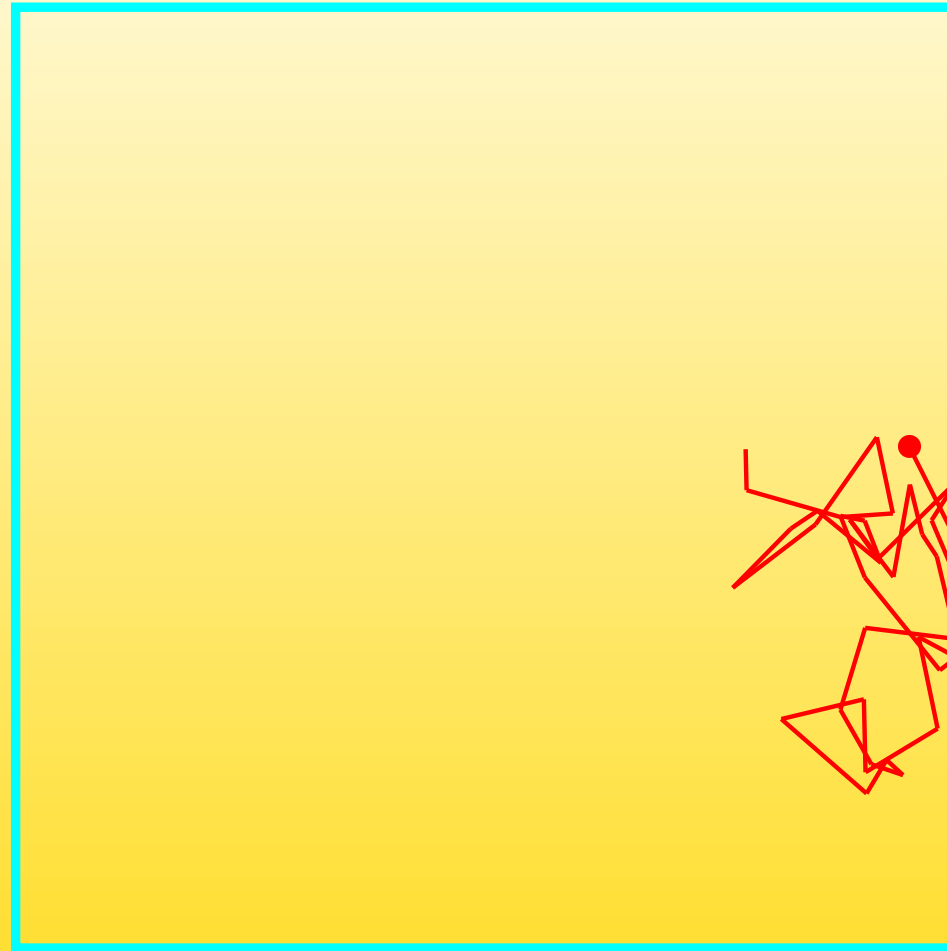


Figure 5: Random walk

End of animation

## 7 – Random walk

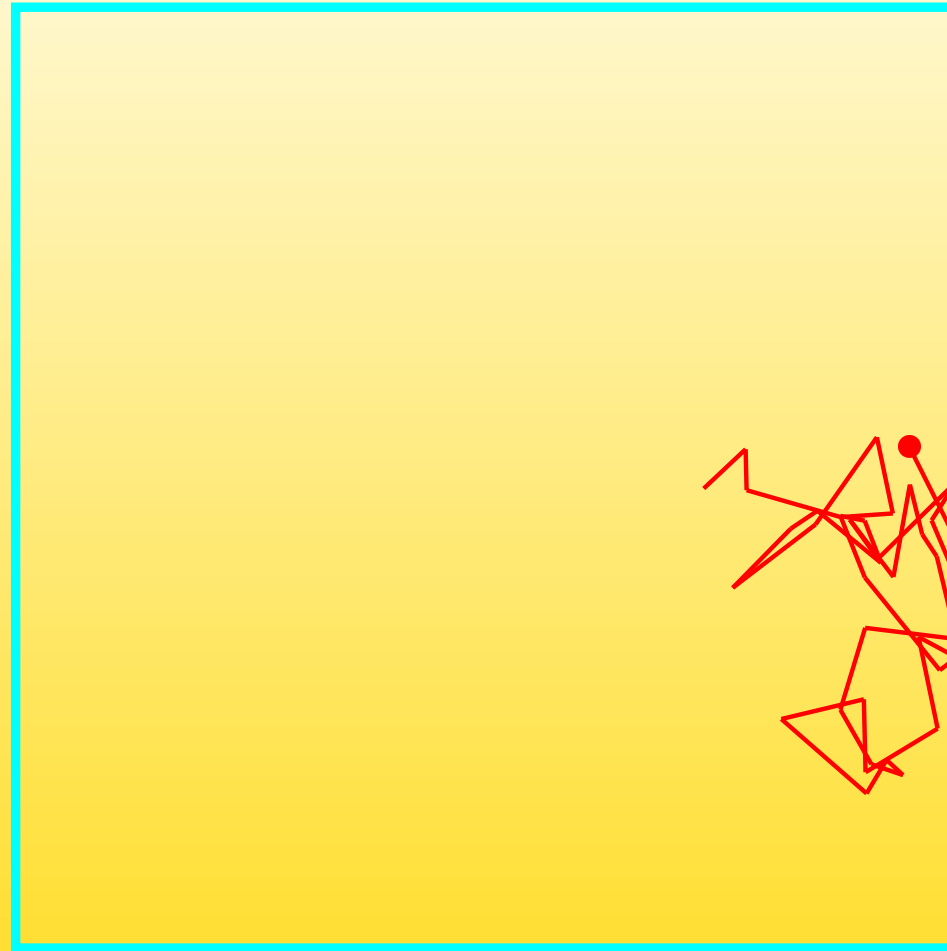


Figure 5: Random walk

End of animation

## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée.	Puisque de vous seules,
Quoi ? — L'Éternité.	Braises de satin,
C'est la mer allée	Le devoir s'exhale
Avec le soleil.	Sans qu'on dise : enfin.

Âme sentinelle	Là pas d'espérance,
Murmurons l'aveu	Nul orietur.
De la nuit si nulle	Science avec patience,
Et du jour en feu.	Le supplice est sûr.

Des humains suffrages	Elle est retrouvée.
Des communs élans	Quoi ? — L'Éternité.
Là tu te dégages	C'est la mer allée
Et voles selon.	Avec le soleil.


**Arthur Rimbaud**

End of animation



## 8 – Text shown through a lens

### L'Éternité



Elle est retrouvée.  
Quoi ? — L'Éternité.

Puisque de vous seules,  
Braises de satin,  
Le devoir s'exhale  
Sans qu'on dise : enfin.

Là pas d'espérance,  
Nul orietur.  
Science avec patience,  
Le supplice est sûr.

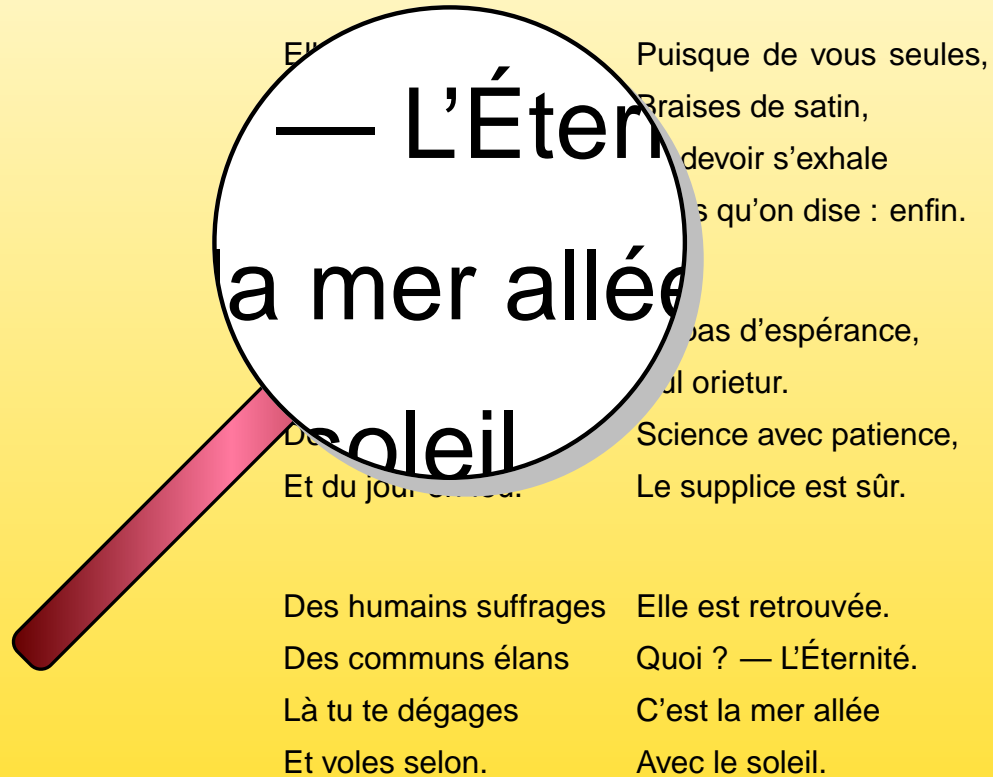
Des humains suffrages  
Des communs élans  
Là tu te dégages  
Et voles selon.

**Arthur Rimbaud**

End of animation

## 8 – Text shown through a lens

### L'Éternité



Arthur Rimbaud

End of animation

## 8 – Text shown through a lens

### L'Éternité



Elle est retrouvée. Puisque de vous seules,  
Quoi ? — Braises de satin,  
C'est la mer allée devoir s'exhale  
C'est la mer allée qu'on dise : enfin.  
C'est la mer allée d'espérance,  
C'est la mer allée etur.  
C'est la mer allée avec patience,  
C'est la mer allée supplice est sûr.

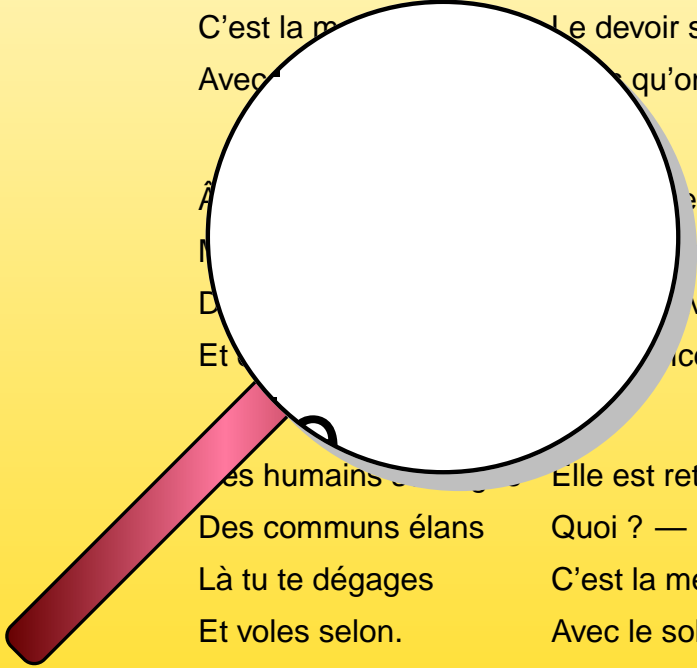
Des humains suffrages Elle est retrouvée.  
Des communs élans Quoi ? — L'Éternité.  
Là tu te dégages C'est la mer allée  
Et voles selon. Avec le soleil.

**Arthur Rimbaud**

End of animation

## 8 – Text shown through a lens

### L'Éternité



Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée. Le devoir s'exhale  
Avec le soleil. Et qu'on dise : enfin.  
À l'espérance,  
Moi. . .  
D'avec patience,  
Et la confiance est sûr.  
Des humains. Elle est retrouvée.  
Des communs élans. Quoi ? — L'Éternité.  
Là tu te dégages. C'est la mer allée  
Et voles selon. Avec le soleil.

**Arthur Rimbaud**

End of animation

## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme...spérance,  
Mur...  
De...patience,  
Et d...est sûr.

Des...retrouvée.  
D...communs...? — L'Éternité.  
Et tu te dégages C'est la mer allée  
Et voles selon. Avec le soleil.

Arthur Rimbaud

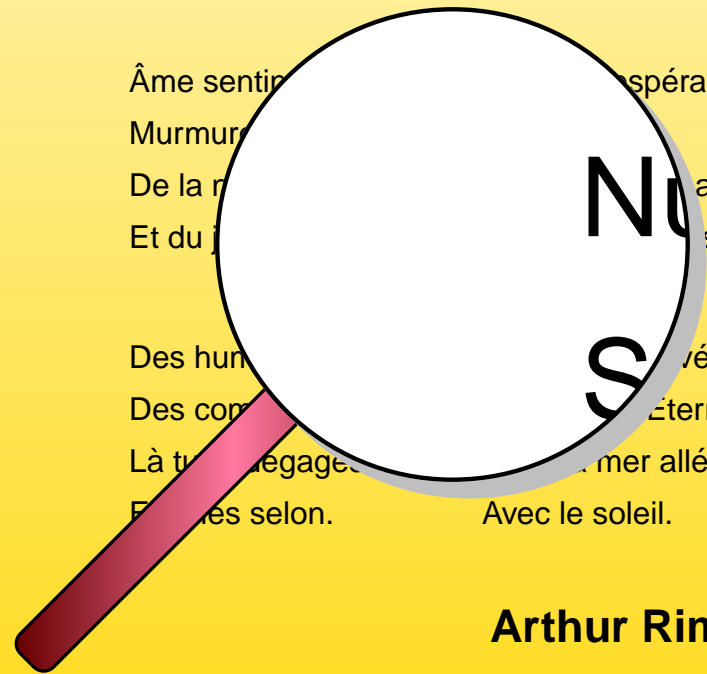
End of animation

## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme sentinelle, espérance,  
Murmure, patience,  
De la mer allée sûr.  
Et du jour, sûr.  
Des humides, vée.  
Des comètes, Éternité.  
Là tout est engagé, mer allée  
Faites selon. Avec le soleil.



Arthur Rimbaud

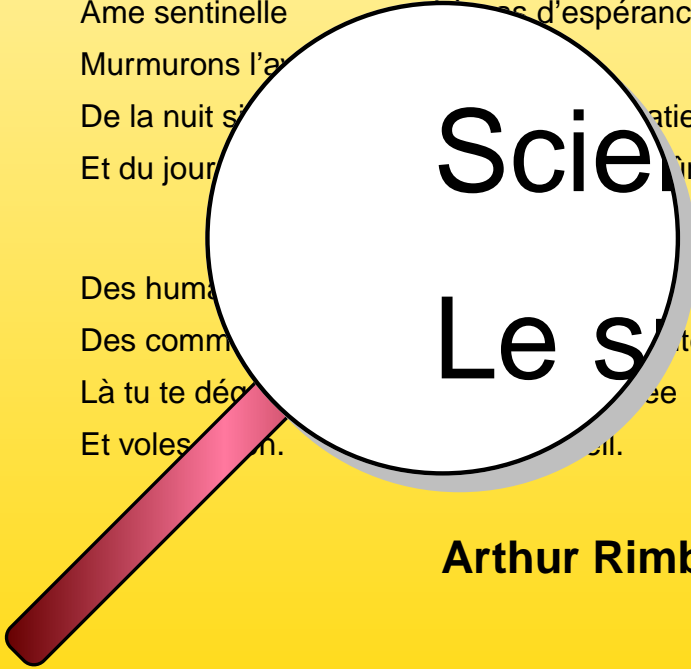
End of animation

## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme sentinelle  
Murmurons l'a  
De la nuit s  
Et du jour  
Des huma  
Des comm  
Là tu te déc  
Et voles



... d'espérance,  
... patience,  
... ir.  
... té.  
... ee  
... il.

Arthur Rimbaud

End of animation

## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme sentinelle Là pas d'espérance,  
Murmurons l'aveu Nul orietur.  
De la nuit si nulle patience,  
Et du jour en fr. fr.

Des humain  
Des commu  
Là tu te déga  
Et voles selon.

Le sup

Arthur Rimbaud

End of animation



## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme sentinelle Là pas d'espérance,  
Murmurons l'aveu Nul orietur.  
De la nuit si nulle Science avec patience,  
Et du jour en feu. sûr.

Des humains si  
Des communs  
Là tu te dégag  
Et voles selon. Elle est re  
aud

End of animation

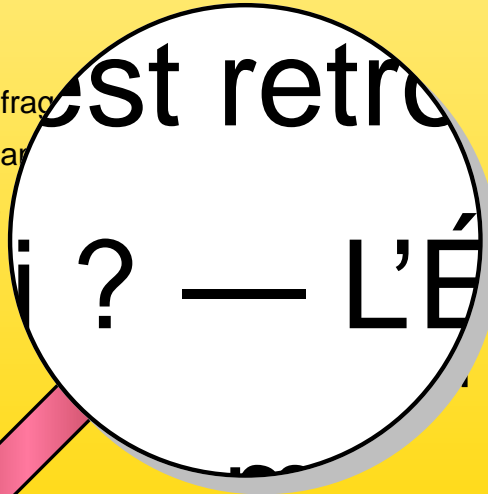
## 8 – Text shown through a lens

### L'Éternité

Elle est retrouvée. Puisque de vous seules,  
Quoi ? — L'Éternité. Braises de satin,  
C'est la mer allée Le devoir s'exhale  
Avec le soleil. Sans qu'on dise : enfin.

Âme sentinelle Là pas d'espérance,  
Murmurons l'aveu Nul orietur.  
De la nuit si nulle Science avec patience,  
Et du jour en feu. Le supplice est sûr.

Des humains suffragant est retrouvée  
Des communs élargi ? — L'É  
Là tu te dégages  
Et voles selon.



End of animation

**9 – Text progressively shown**

End of animation

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End of animation

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9 – Text progressively shown

Do not do like

End of animation

9 – Text progressively shown

Do not do like

End of animation

9 – Text progressively shown

Do not do like m

End of animation

9 – Text progressively shown

Do not do like me

End of animation

9 – Text progressively shown

Do not do like me!

End of animation

# Demonstration of animated graphics

10 – Text progressively vanished

End of animation

# Demonstration of animated graphics

10 – Text progressively vanished

Oh! my dear friends...

It is time to tell you

good bye!

See you again soon!

End of animation

# Demonstration of animated graphics

10 – Text progressively vanished

Oh! my dear friends...

It is time to tell you

good bye!

See you again soon!

End of animation



# Demonstration of animated graphics

10 – Text progressively vanished

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See you again soon!

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See you again soon!

End of animation



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## 10 – Text progressively vanished

Oh! my dear friends...

It is time to tell you

good bye!

See you again soon!

End of animation

# Demonstration of animated graphics

## 10 – Text progressively vanished

Oh! my dear friends...

It is time to tell you

good bye!

See you again soon!

End of animation

## 11 – Building of a regular polygon of seventeen sides

Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

1: Definition of the center  $O$  of the polygon



Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

2: Definition of the point  $P_1$  at 5 units from  $O$



Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

3: Circle of center  $O$  with the point  $P_1$  on it

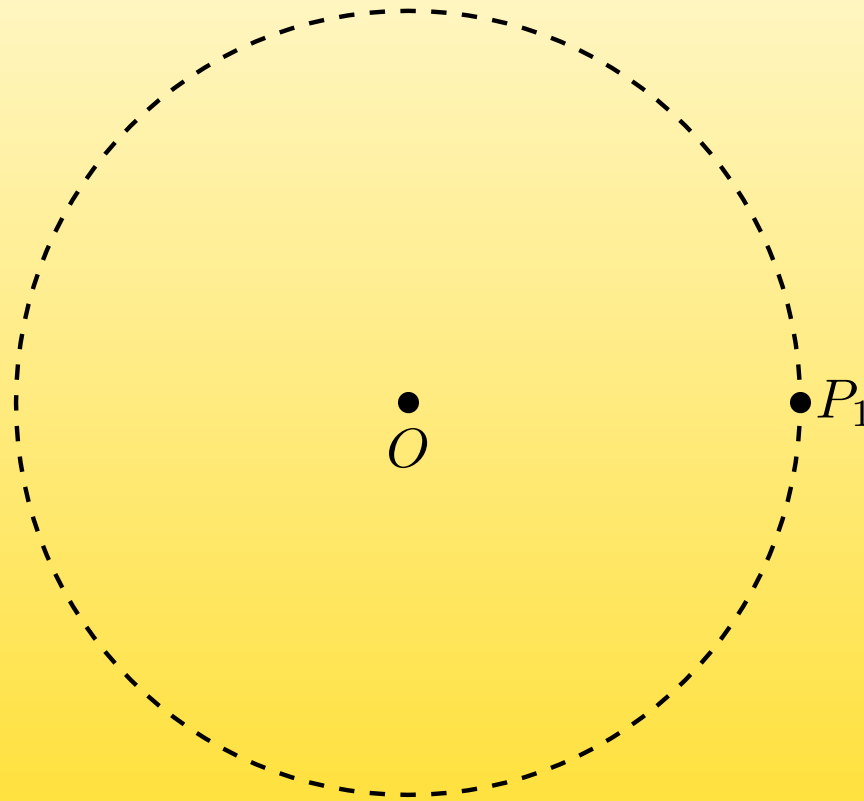


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

4: Definition of the point  $PP_1$ , symmetric to the point  $P_1$

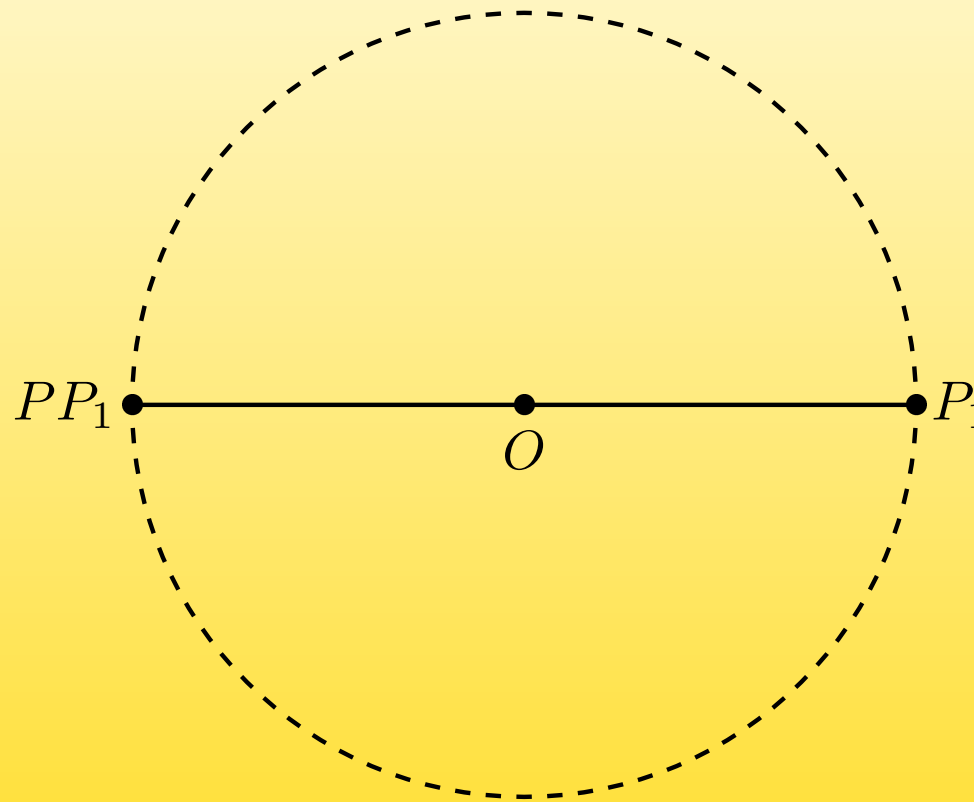


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

5: Definition of the point  $B$ , with  $P_1-O-B$  a right angle

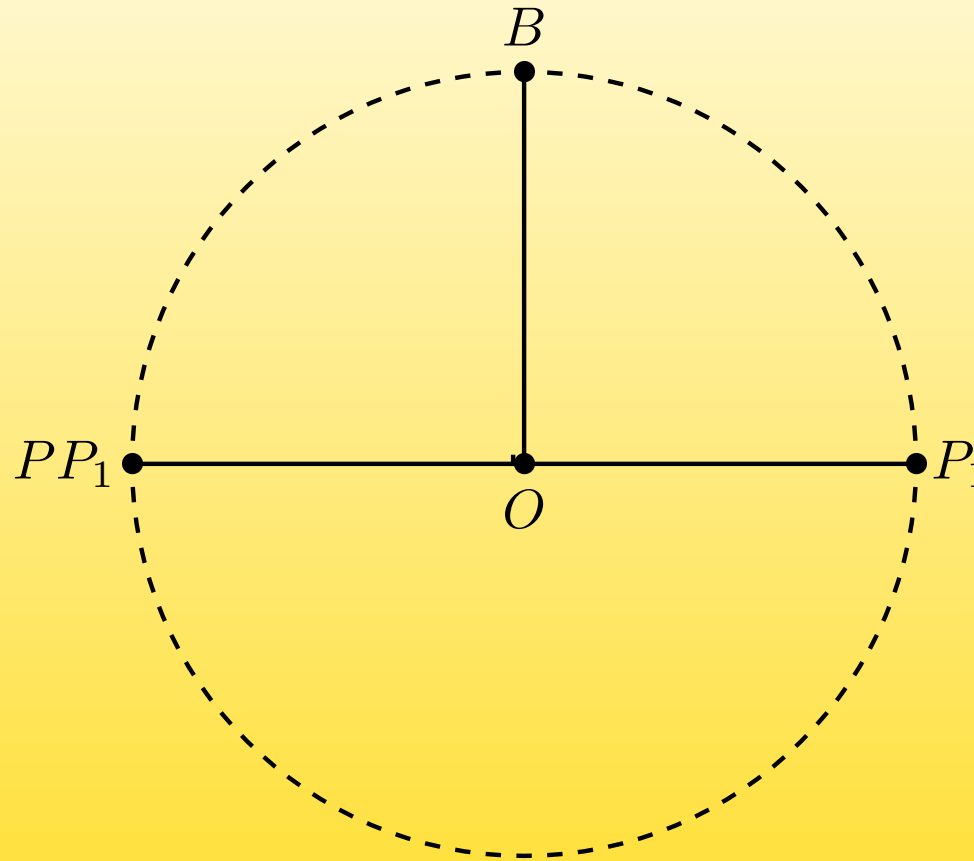


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

6: Definition of the point  $J$ , as 0.25 of  $O-B$

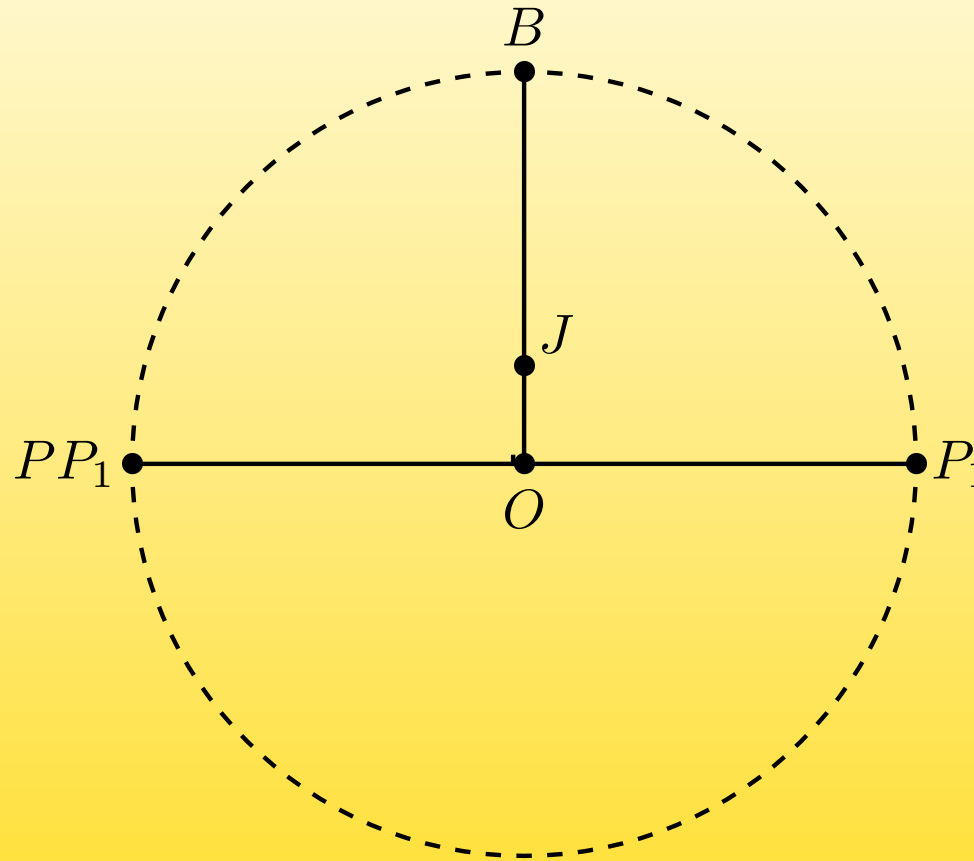


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

7: Line between the points  $J$  and  $P_1$

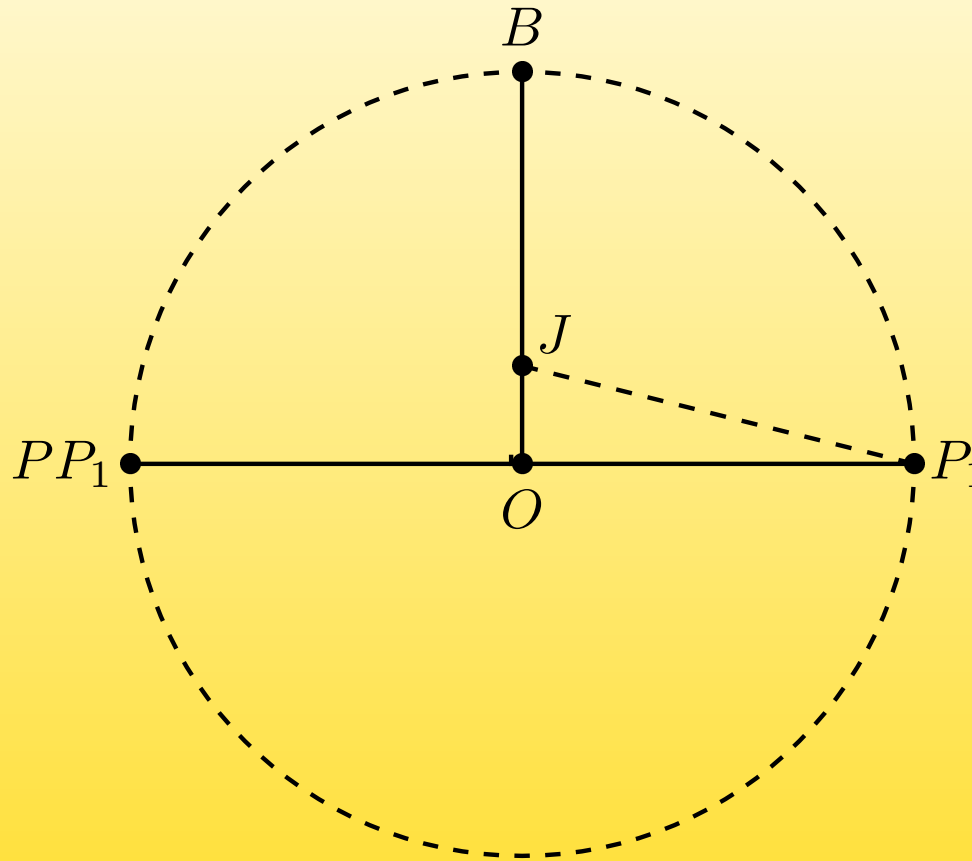


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

8: Bissectrisse of the angle defined by the points  $J$ ,  $O$ , and  $P_1$ , which define the point  $PE1$

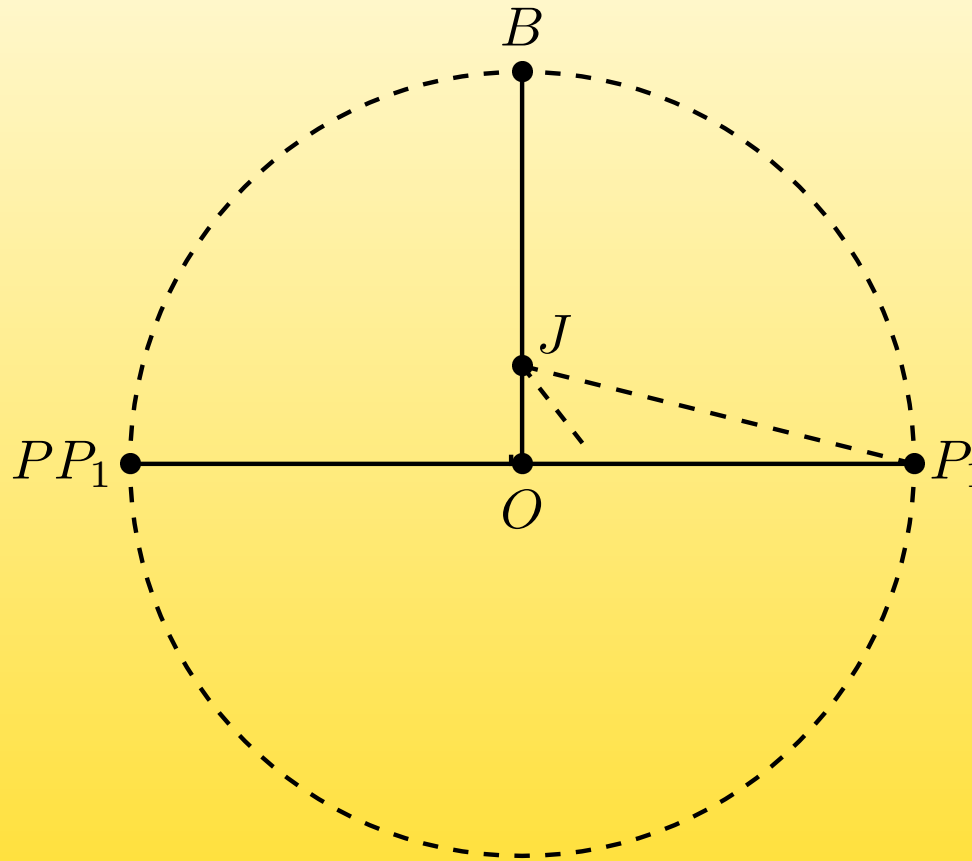


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

9: Bissectrisse of the angle defined by the points  $J$ ,  $O$ , and  $PE1$ , which define the point  $PE2$

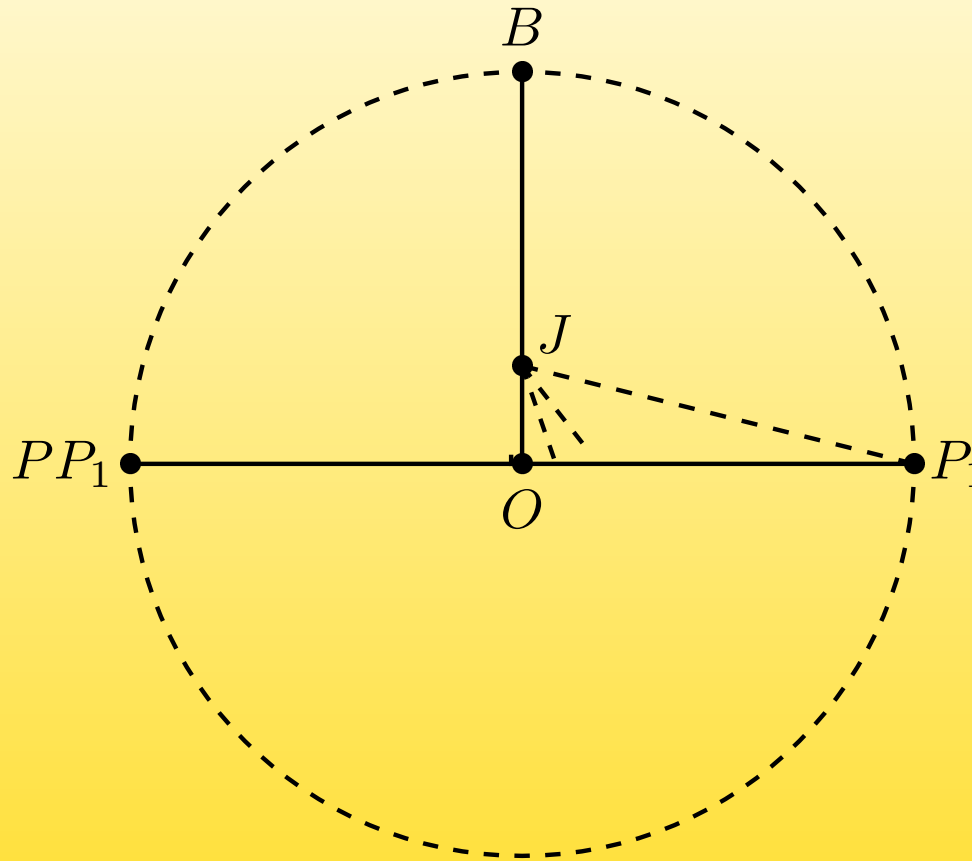


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

10: Definition of the point  $E$ , as intersection of the two lines  $O-P_1$  and  $J-PE2$

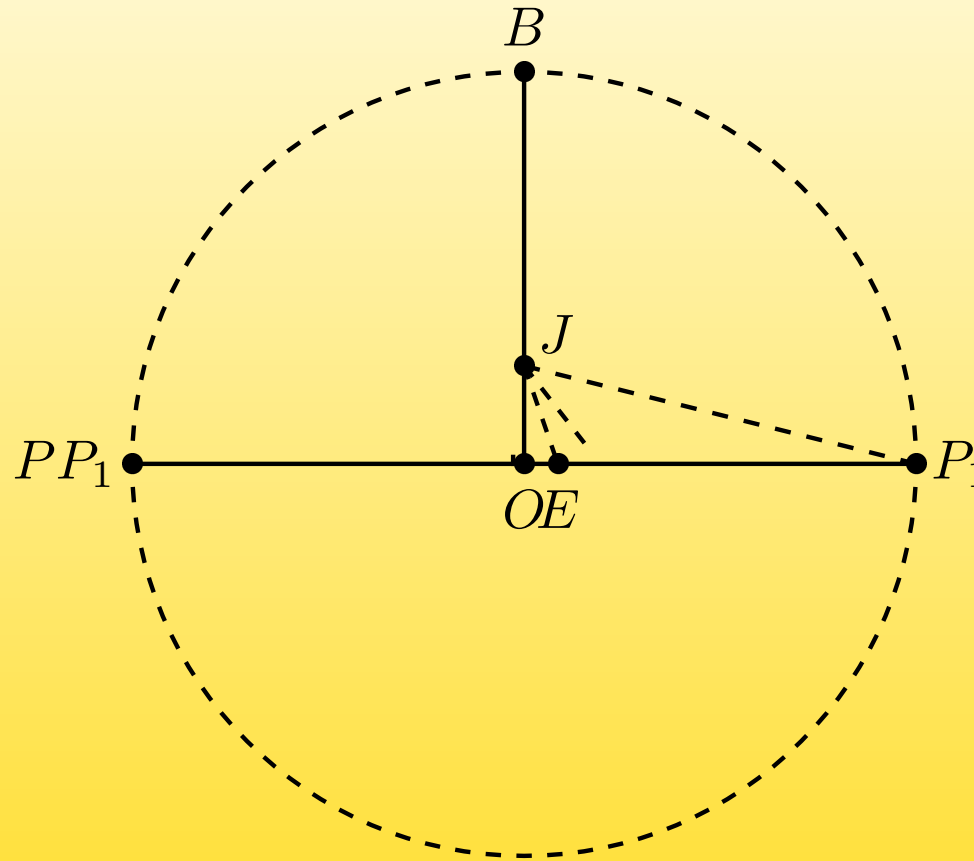


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

11: Definition of the point **F**, as intersection of the two lines **O-P<sub>1</sub>** and **J-PF<sub>1</sub>**, with **PF<sub>1</sub>** defined by **J** and **E**

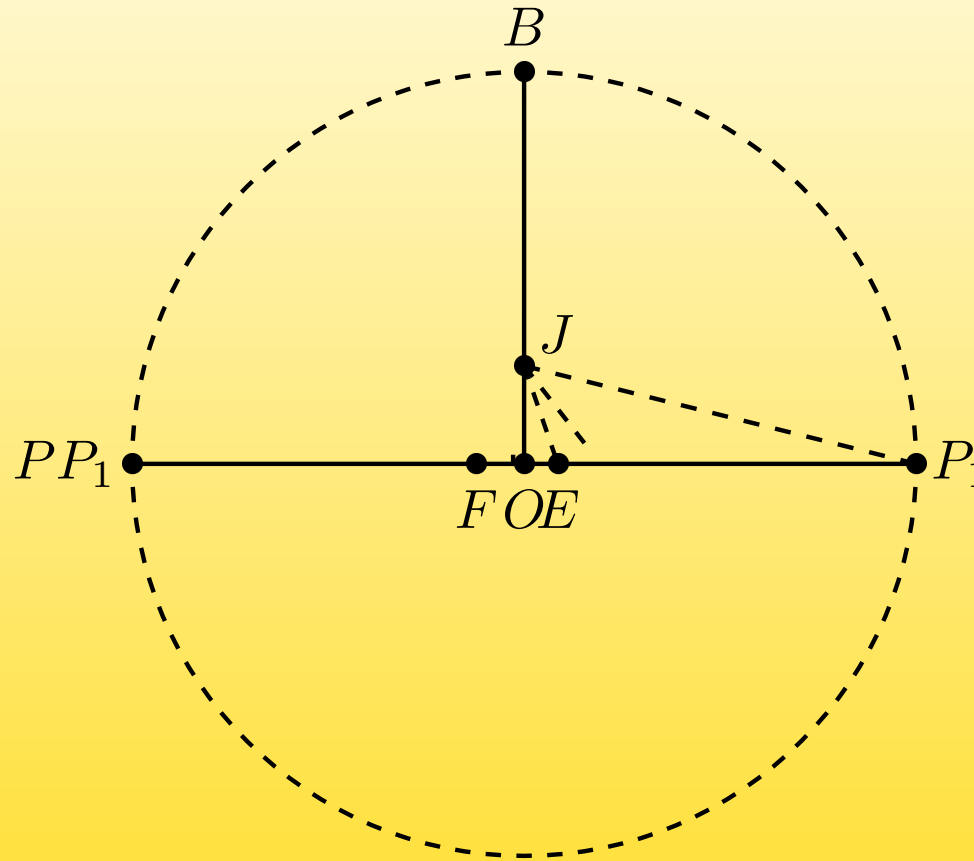


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

12: Definition of the point  $MFP1$ , as middle of the line  $F-P_1$

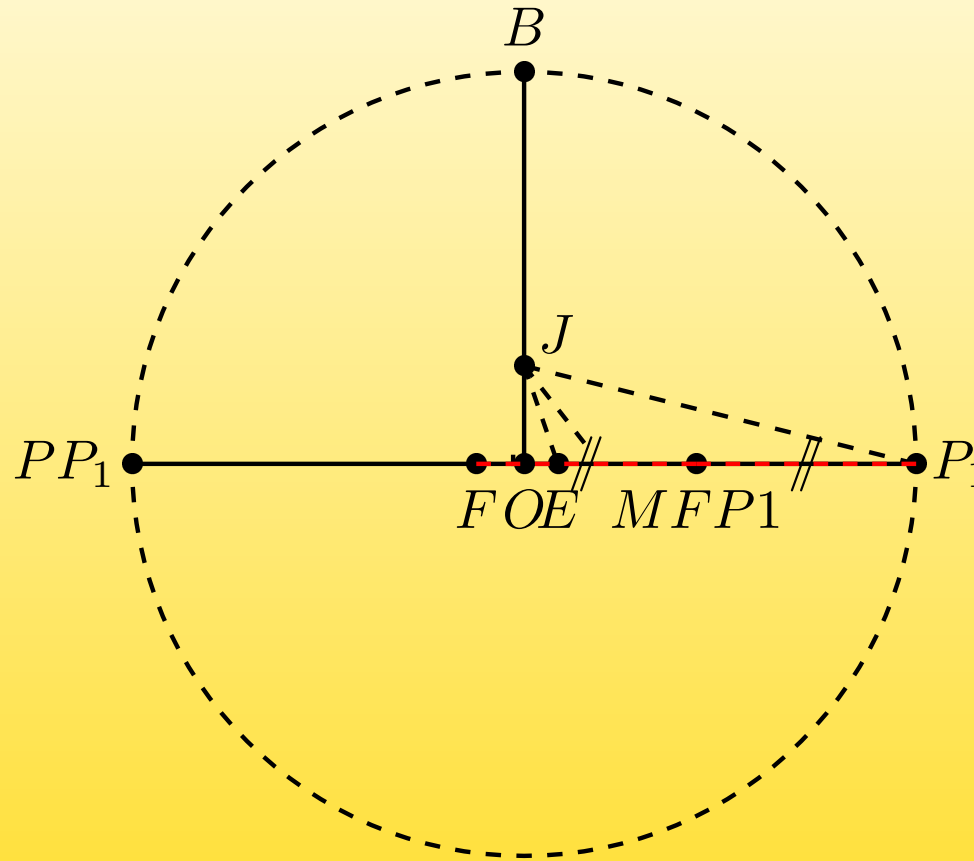


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

13: Circle of center  $MFP1$  with point  $P_1$  on it

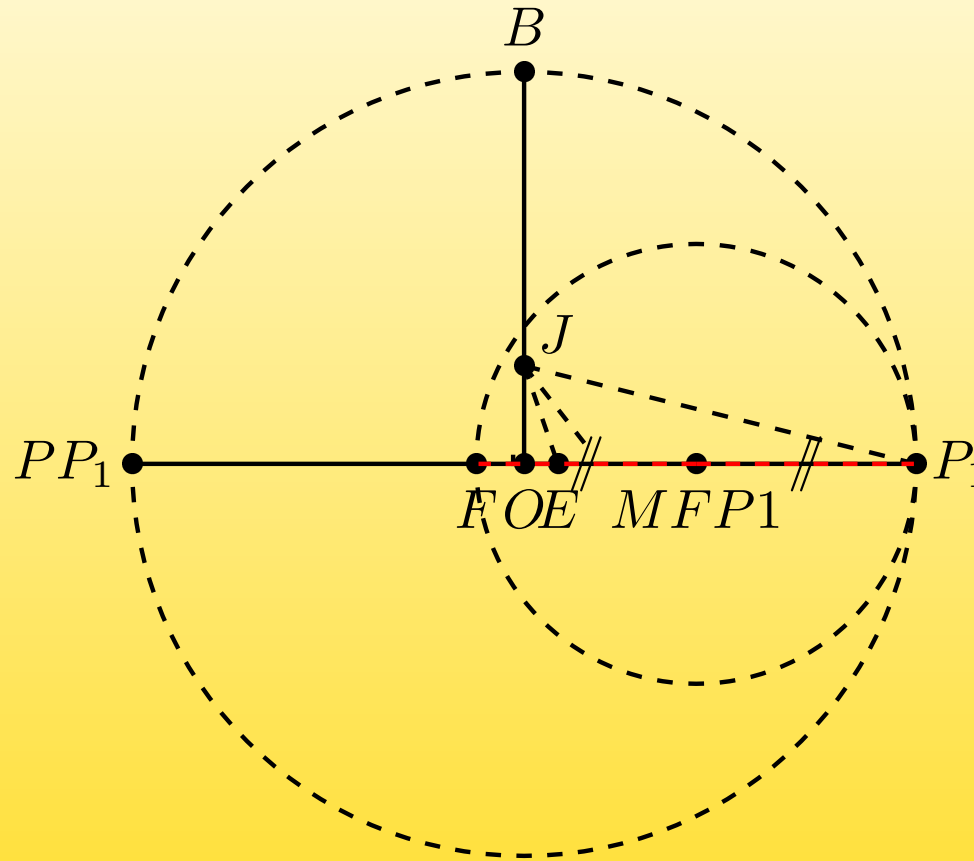


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

14: Definition of the point  $K$ , as intersection of the line  $O-B$  and the circle of center  $MFP1$  and radius  $P_1$

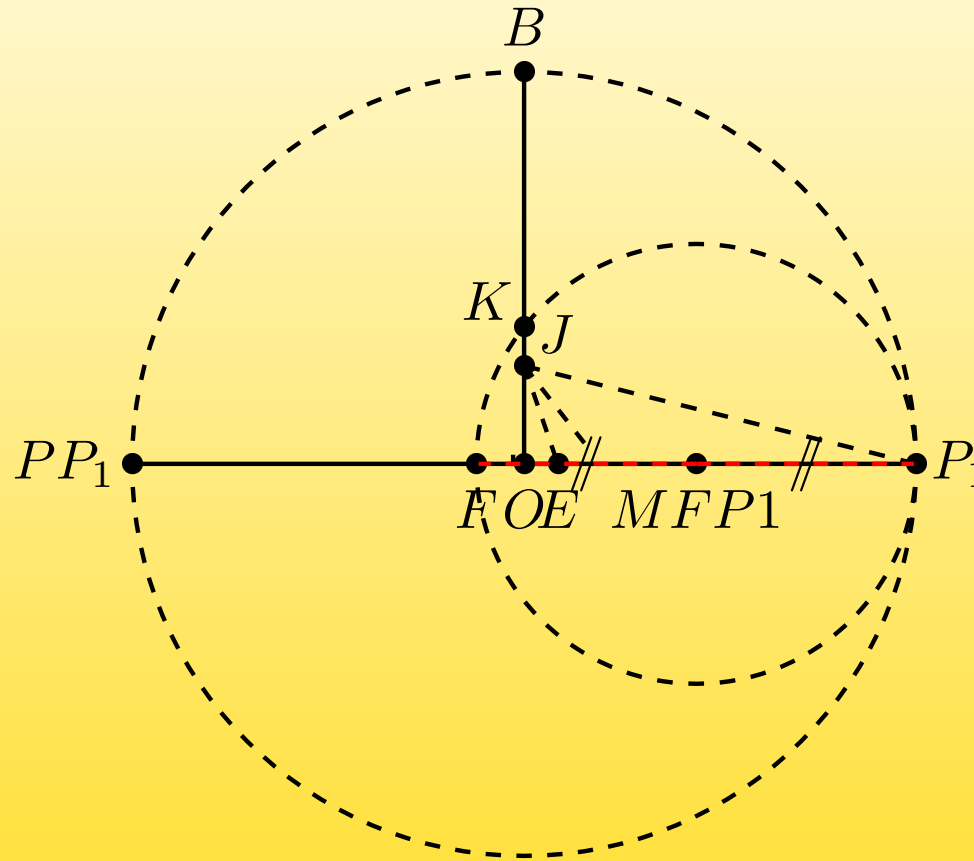


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

15: Circle of center **E** with point **K** on it

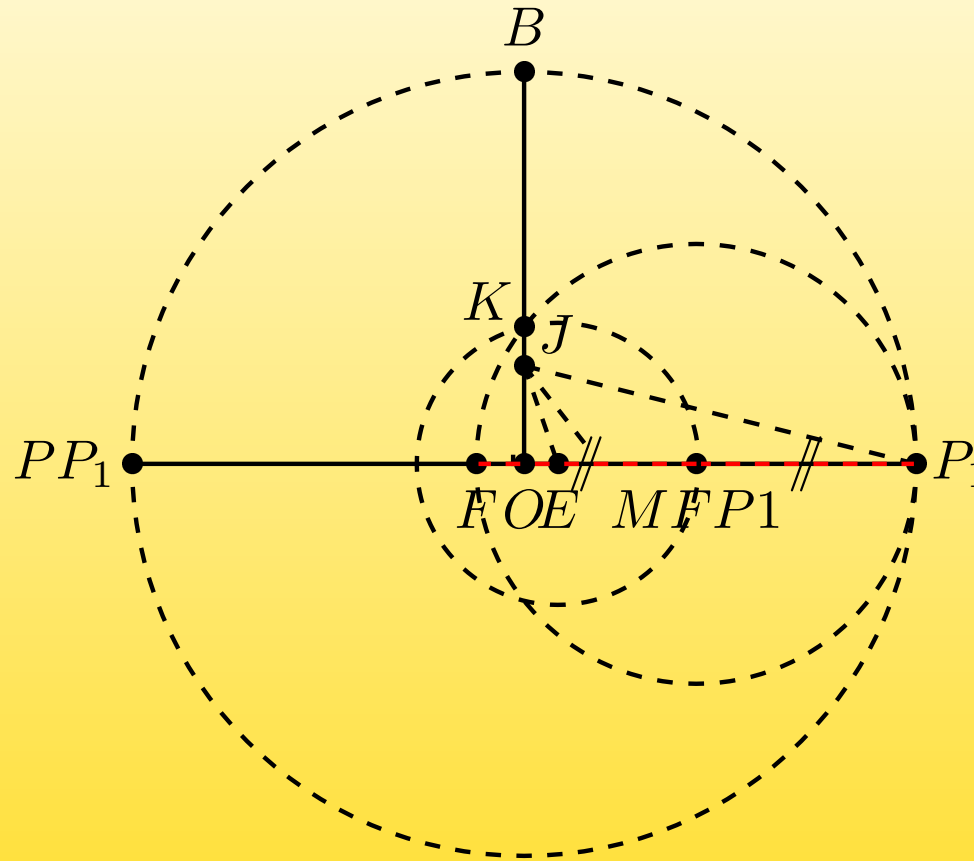


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

16: Definition of the points  $N_4$  and  $N_6$ , as intersection of the line  $P_1-E$  and the circle of center  $E$  radius  $K$

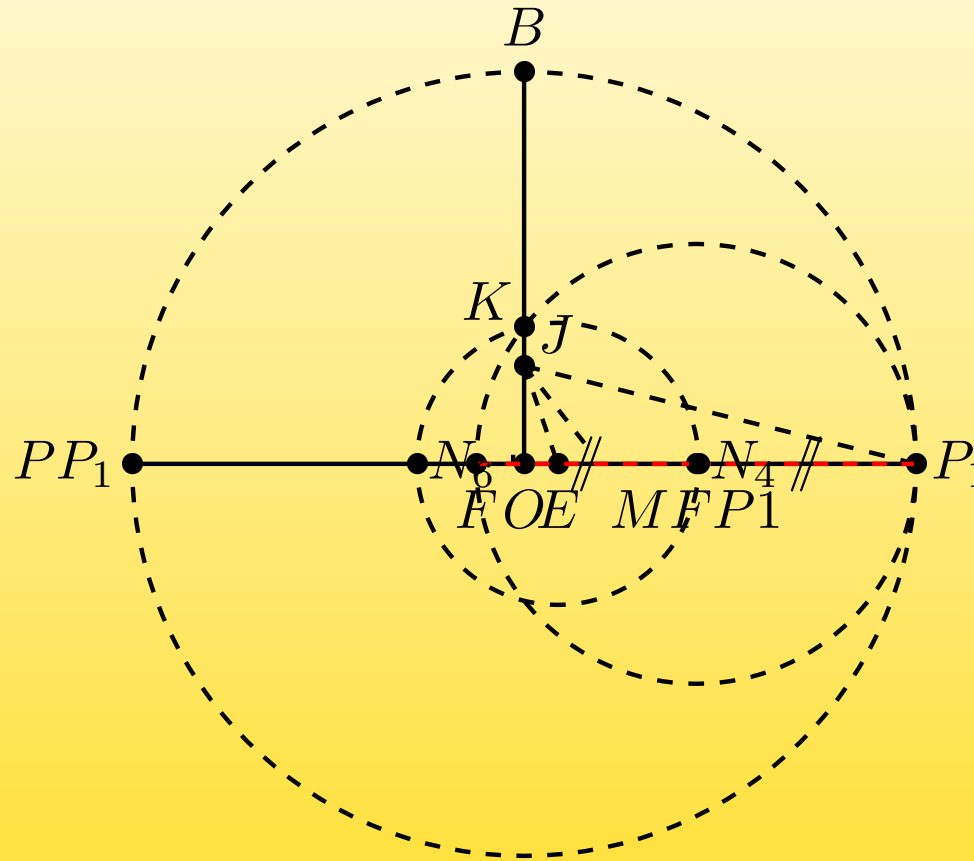


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

18: Definition of the points  $P_4$  and  $P_{15}$ , as intersection of the line  $N_4-PP_4$  and the original circle

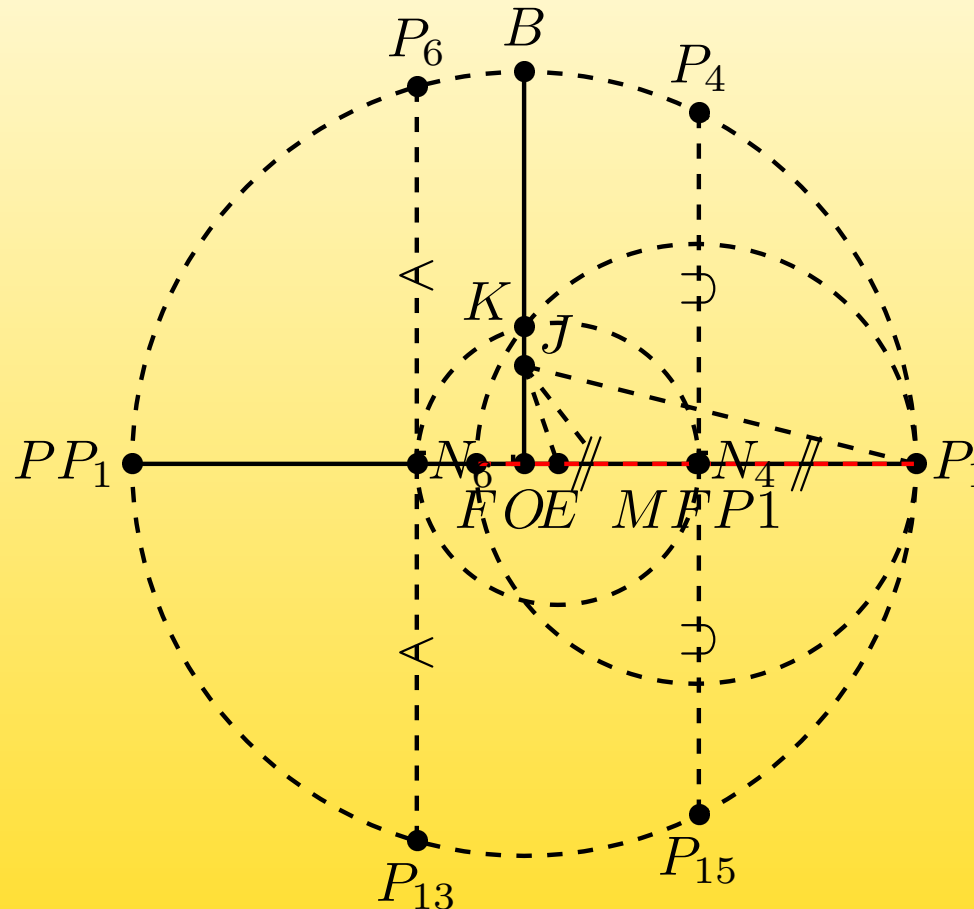


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

19: Bissectrice of the angle defined by the points  $P_4$ ,  $O$ , and  $P_6$ , which define the point  $P_5$

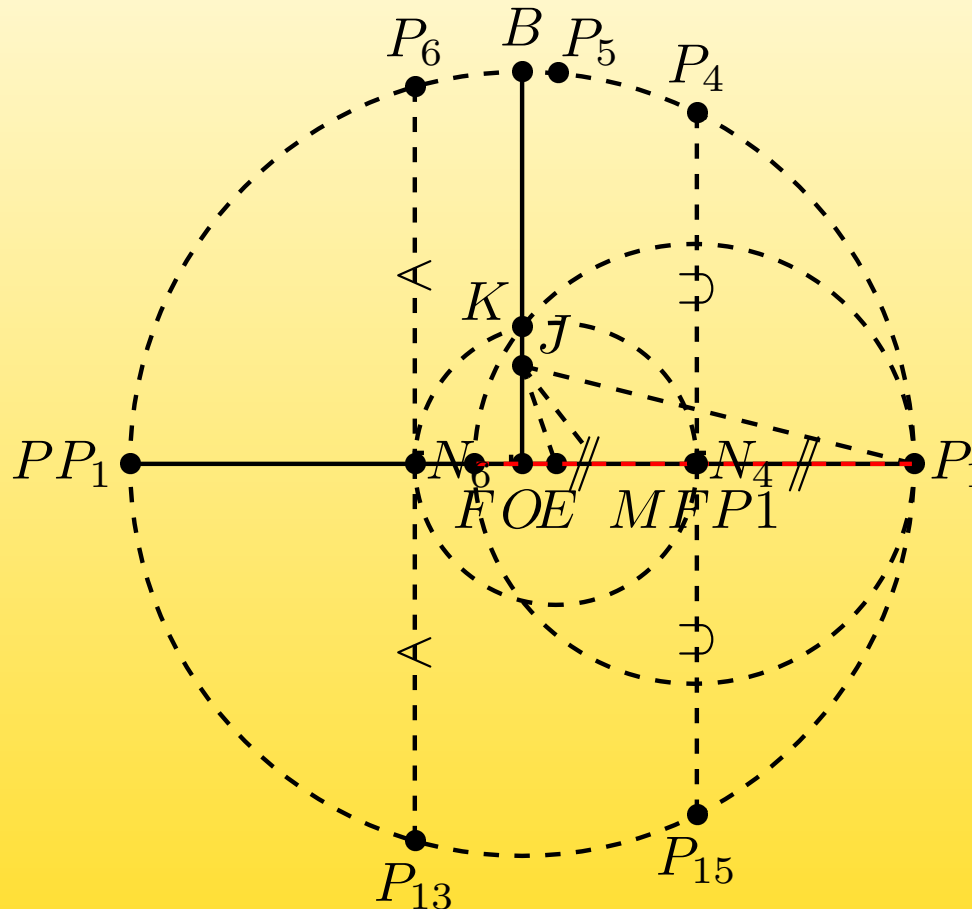


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

21: Definition of the point  $P_3$  on the original circle, by intersection of two circles

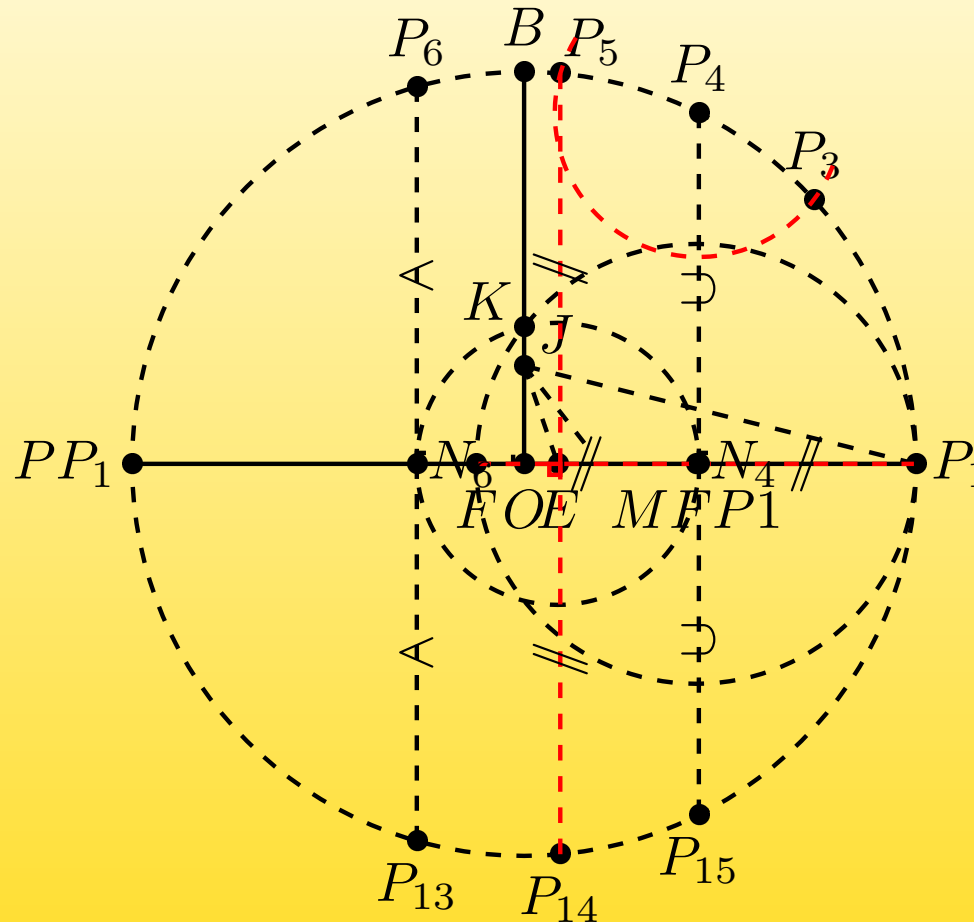


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

22: Definition of the point  $P_{16}$  on the original circle, by orthogonal symmetry with the point  $P_3$

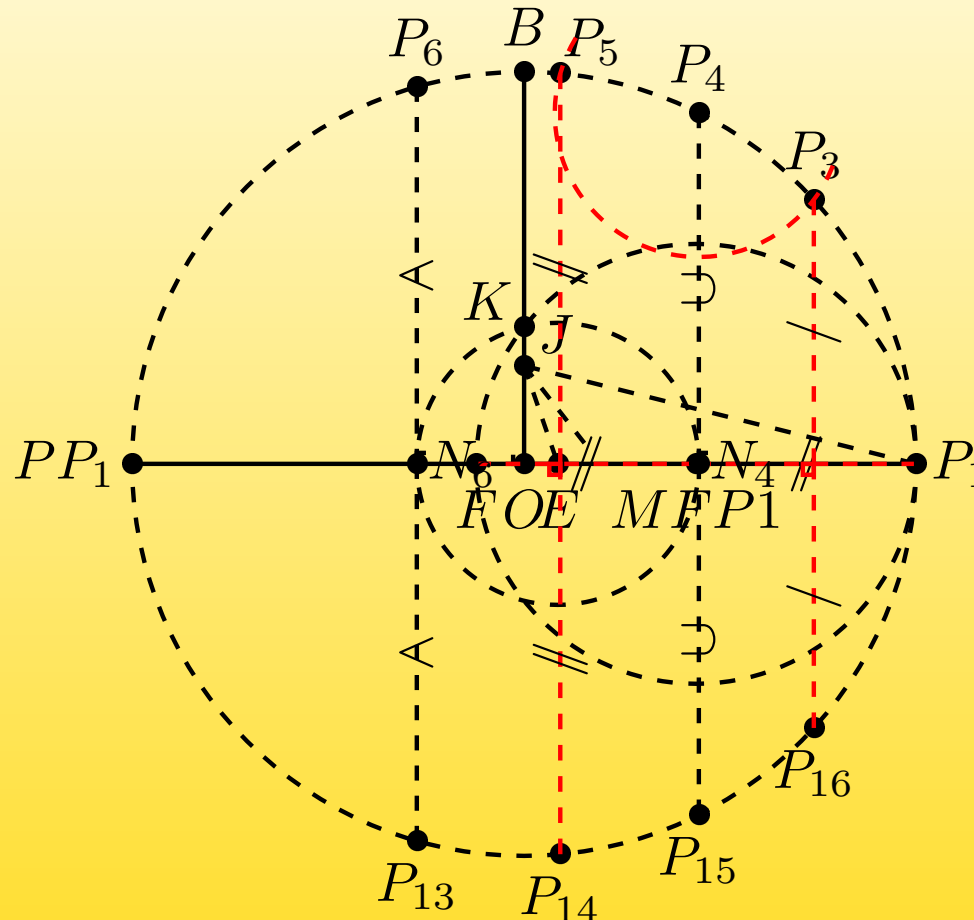


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

23: Definition of the point  $P_2$  on the original circle, by intersection of two circles

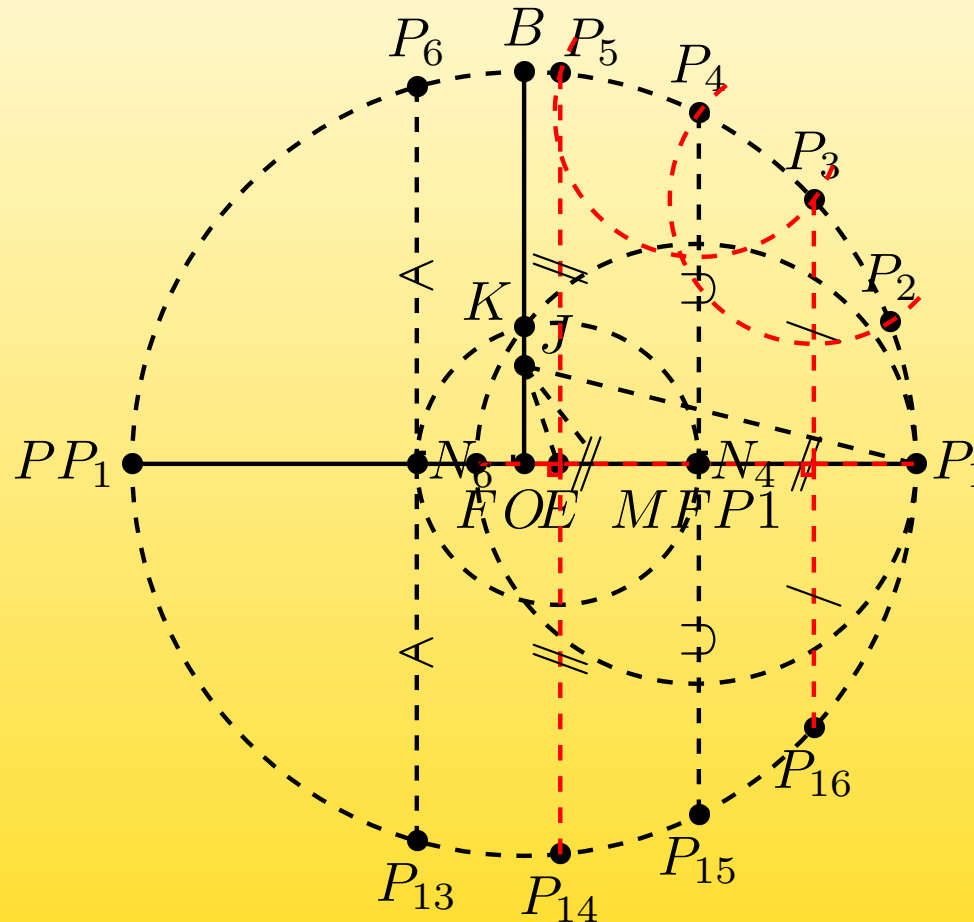


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

24: Definition of the point  $P_{17}$  on the original circle, by orthogonal symmetry with the point  $P_2$

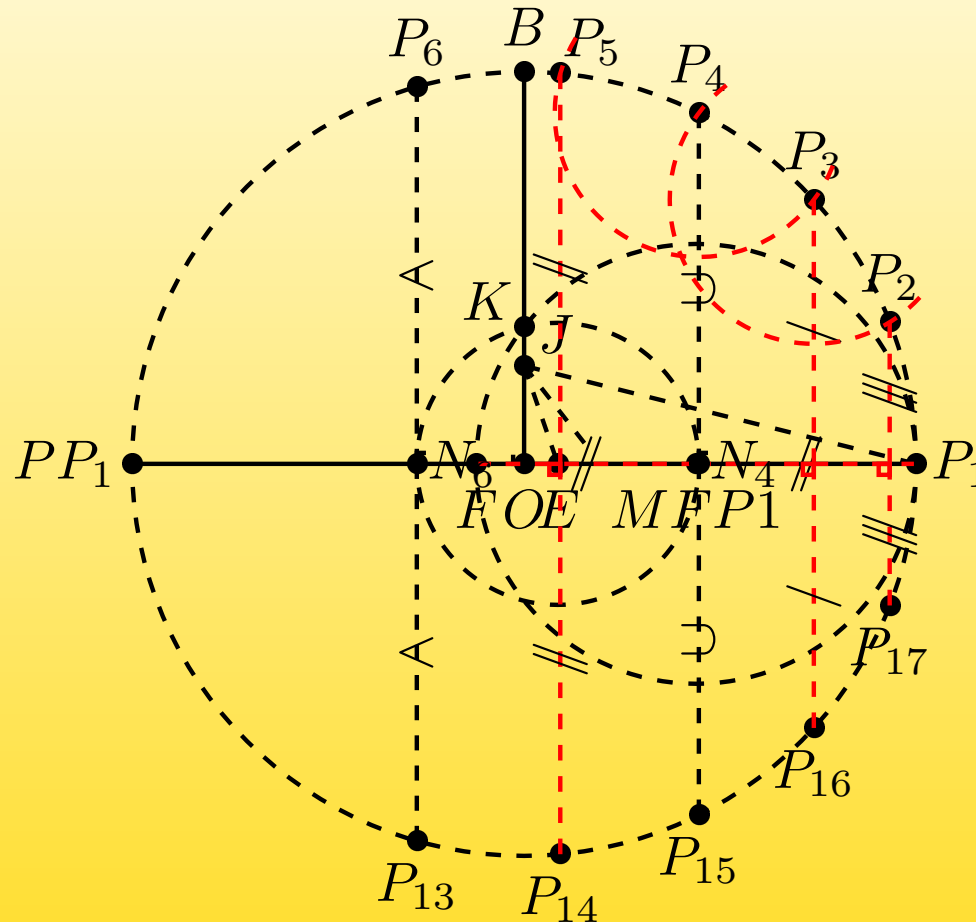


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

26: Definition of the point  $P_{12}$  on the original circle, by orthogonal symmetry with the point  $P_7$

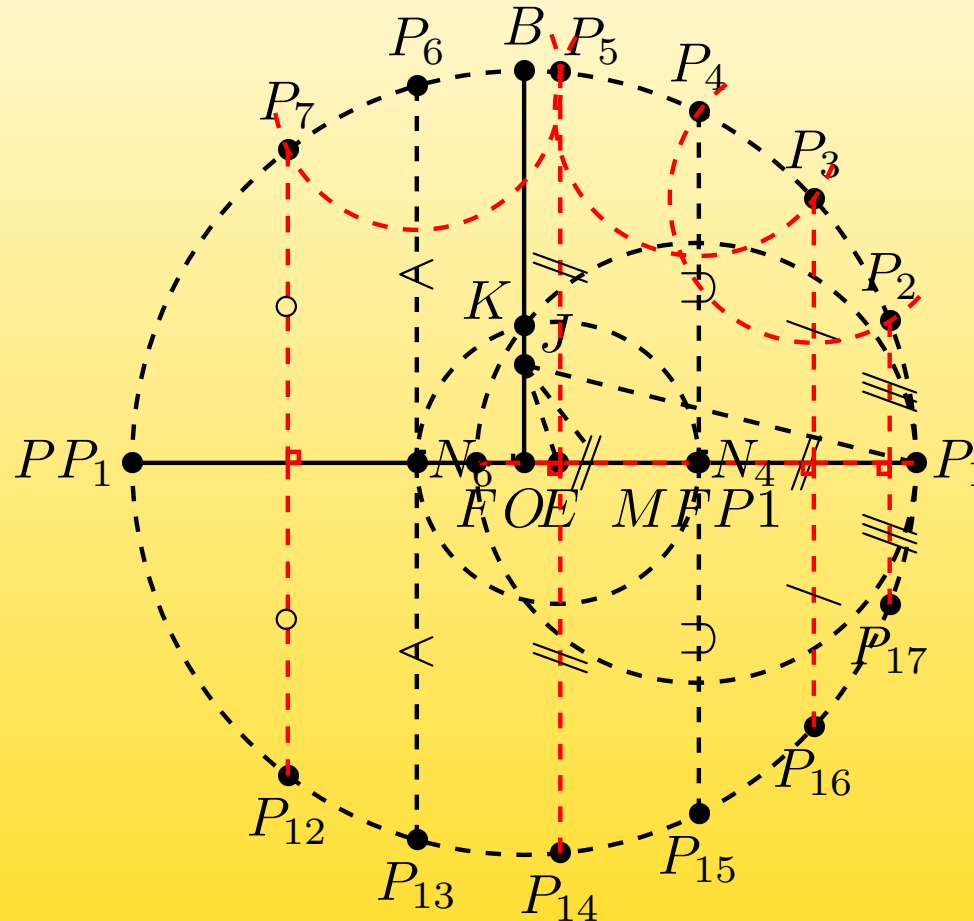


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

28: Definition of the point  $P_{11}$  on the original circle, by orthogonal symmetry with the point  $P_8$

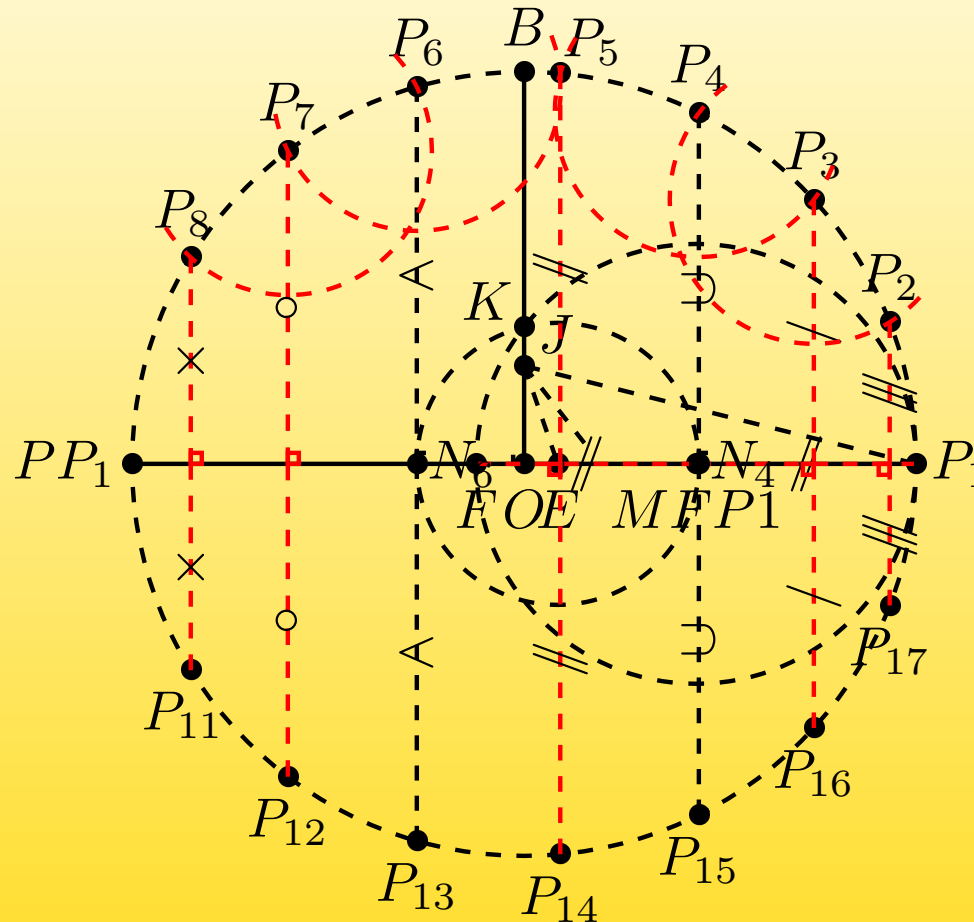


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

29: Definition of the point  $P_9$  on the original circle, by intersection of two circles

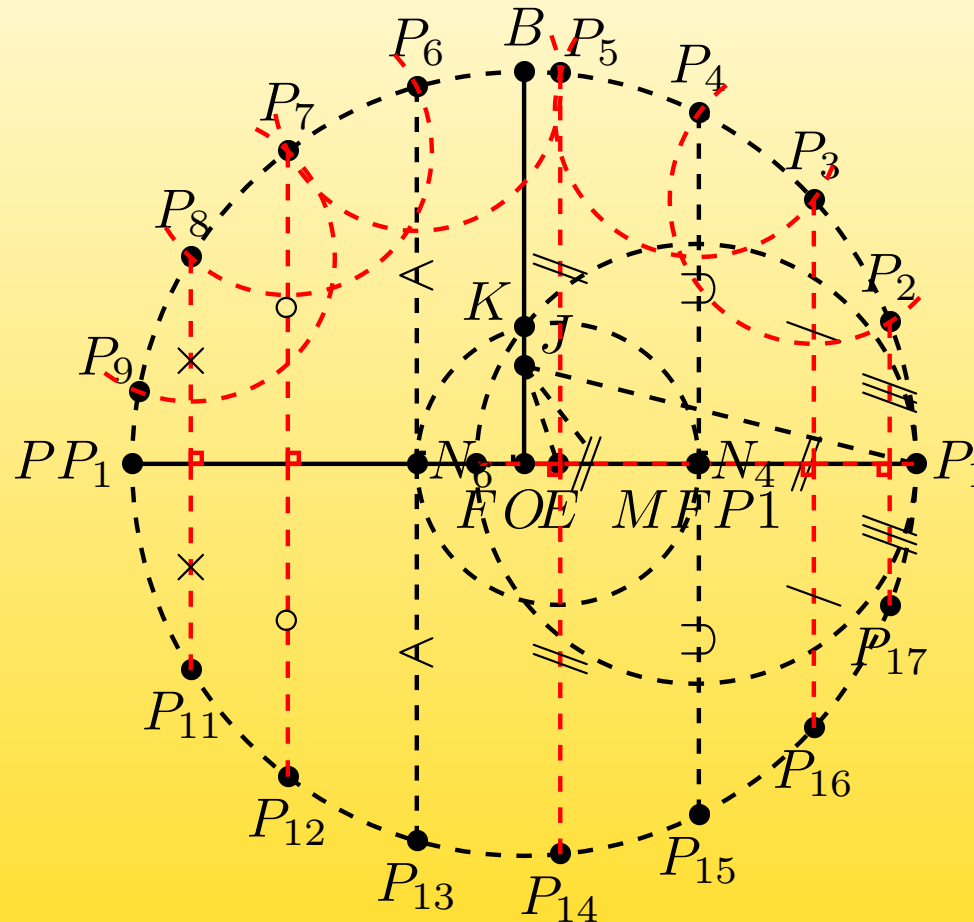


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

30: Definition of the point  $P_{10}$  on the original circle, by orthogonal symmetry with the point  $P_9$

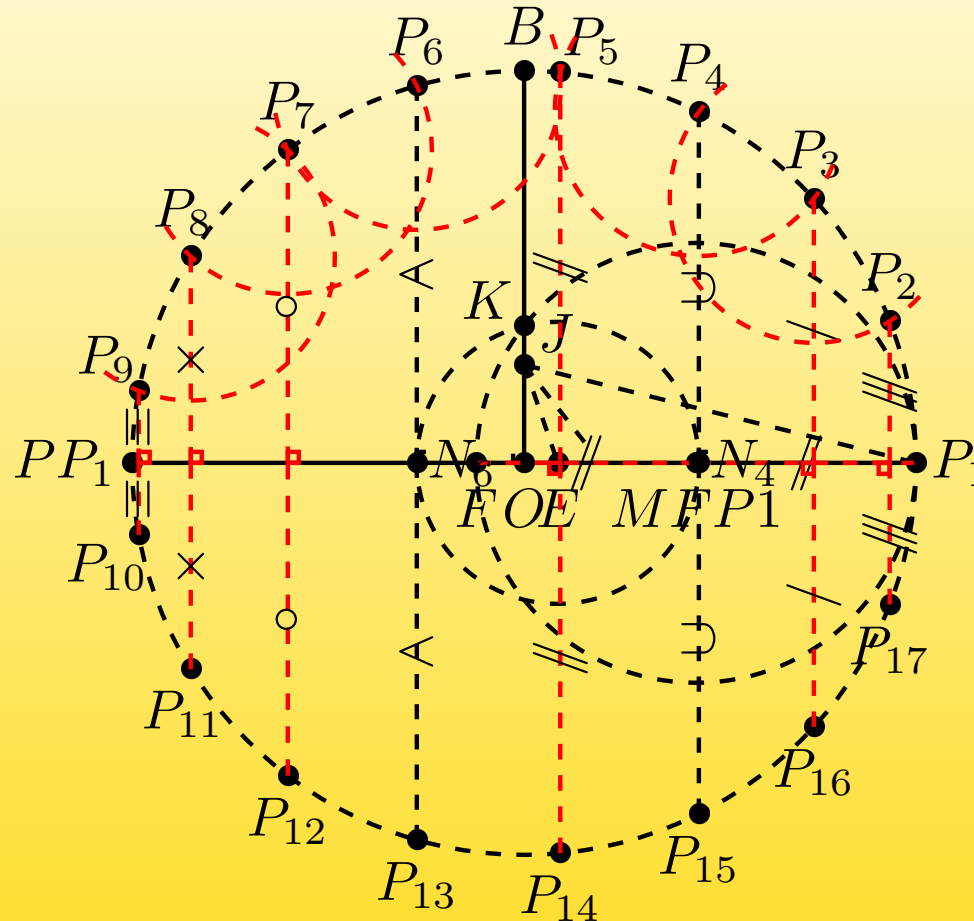


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

31: Side number 1 of the polygon

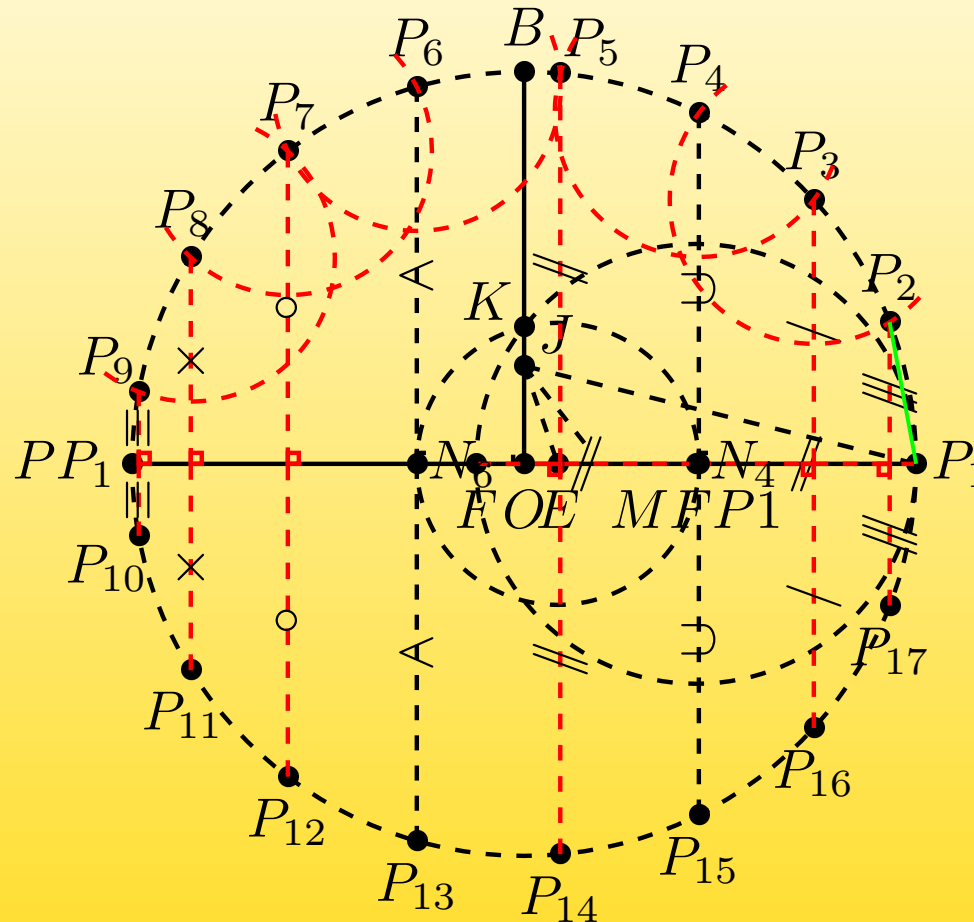


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation







## 11 – Building of a regular polygon of seventeen sides

35: Side number 5 of the polygon

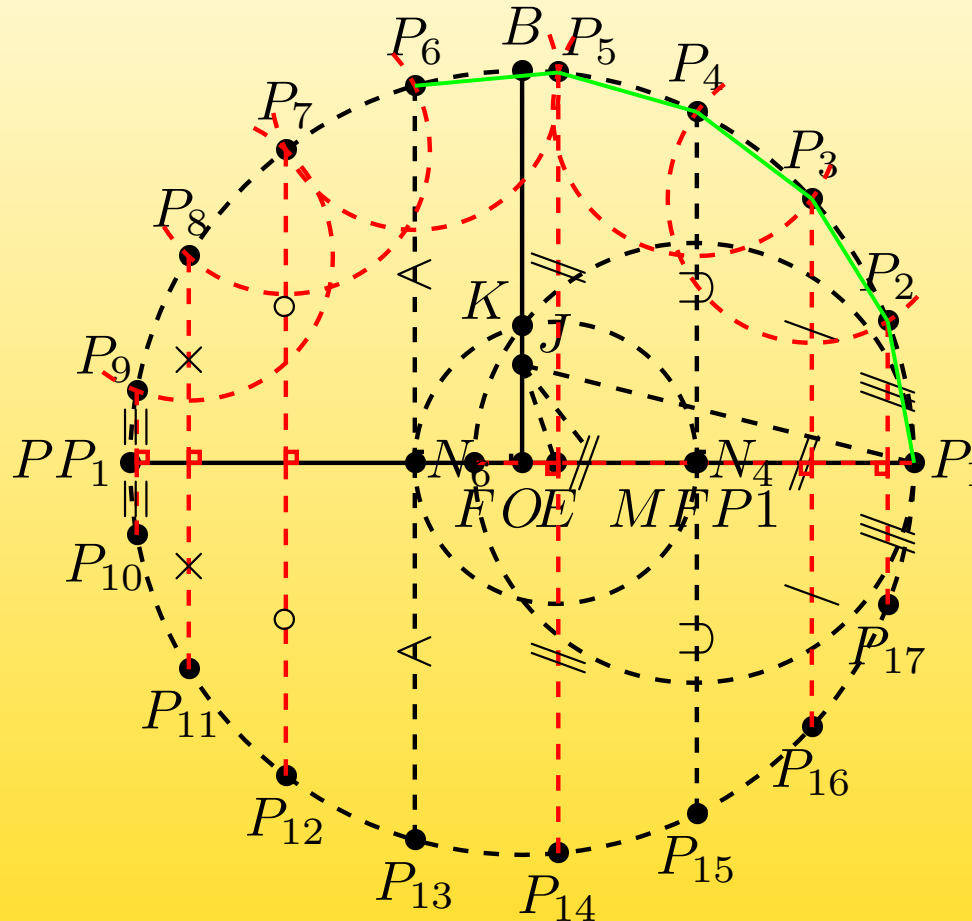


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

36: Side number 6 of the polygon

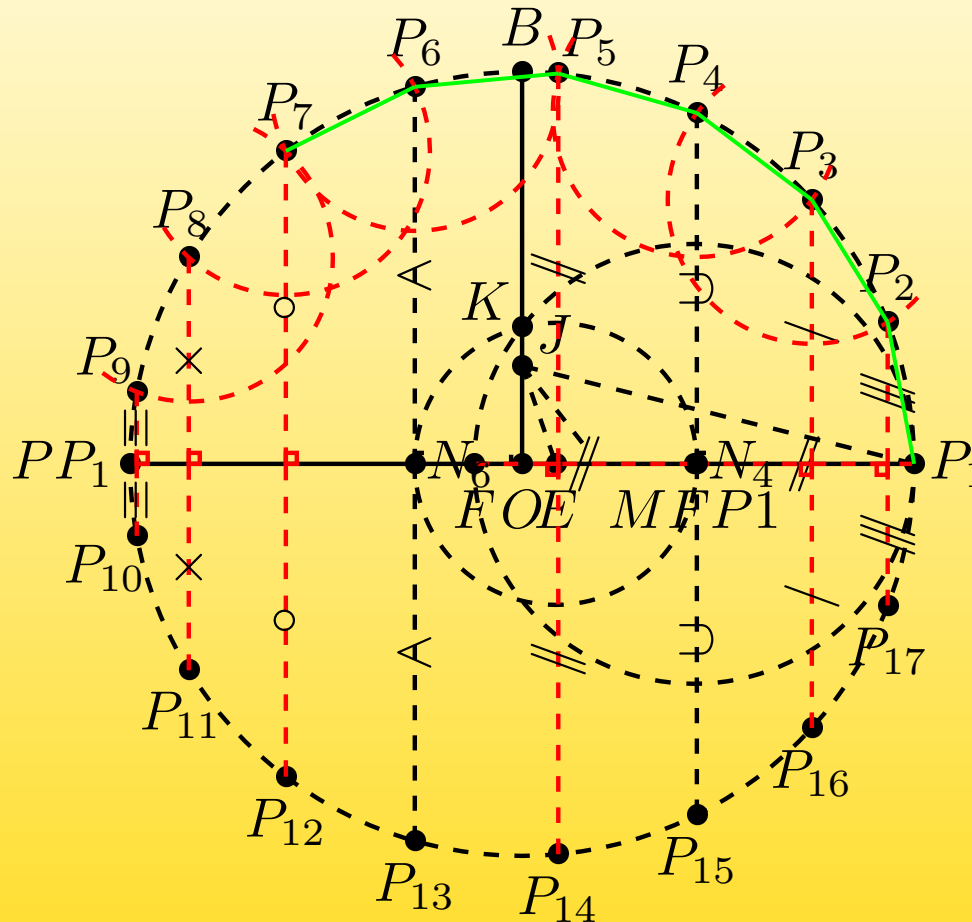


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

37: Side number 7 of the polygon

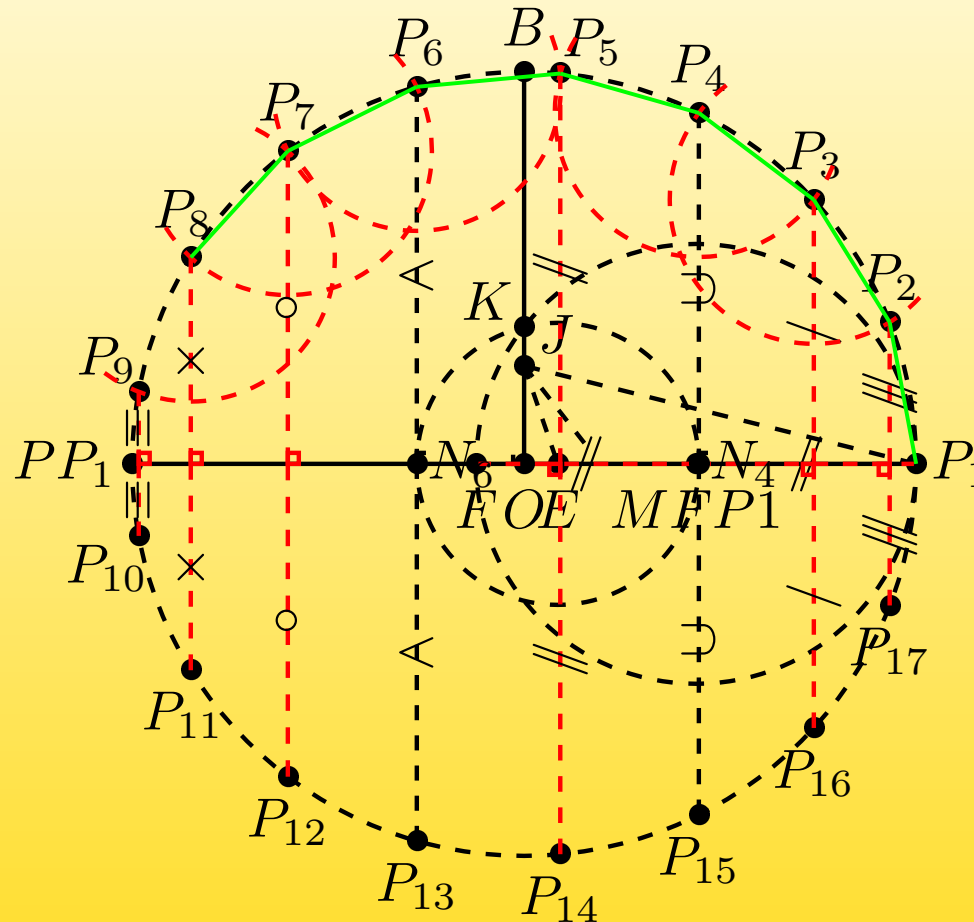


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

38: Side number 8 of the polygon

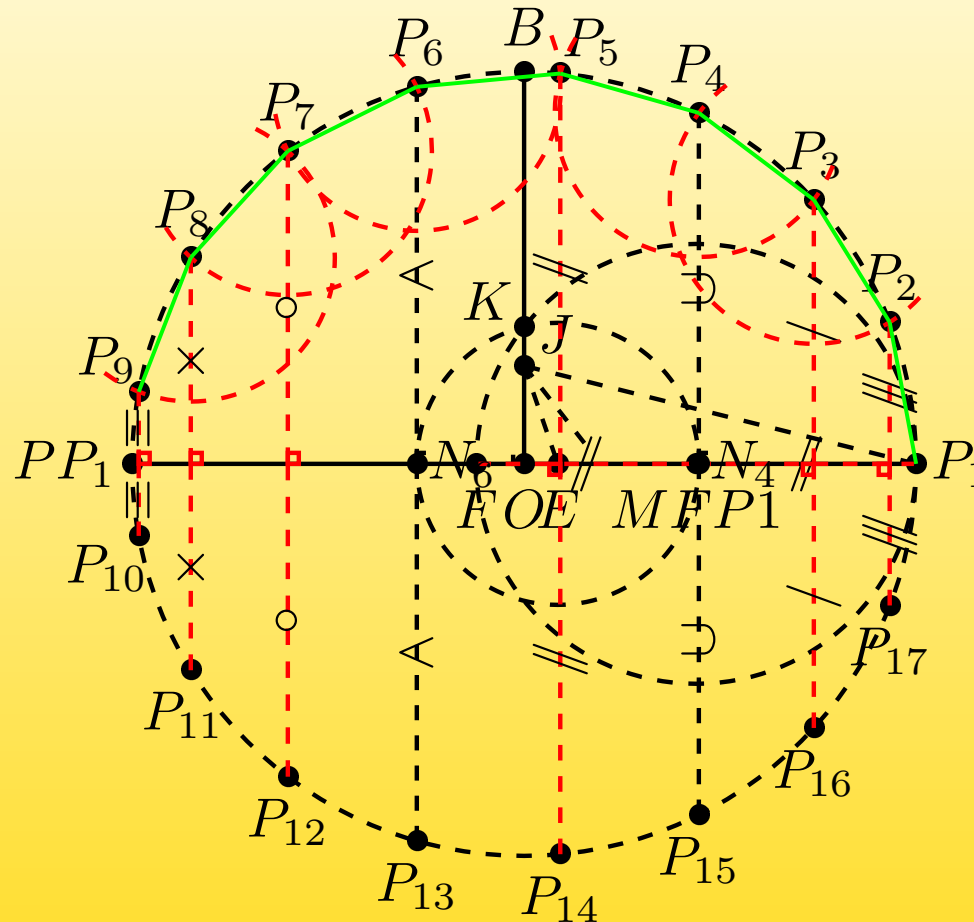


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

39: Side number 9 of the polygon

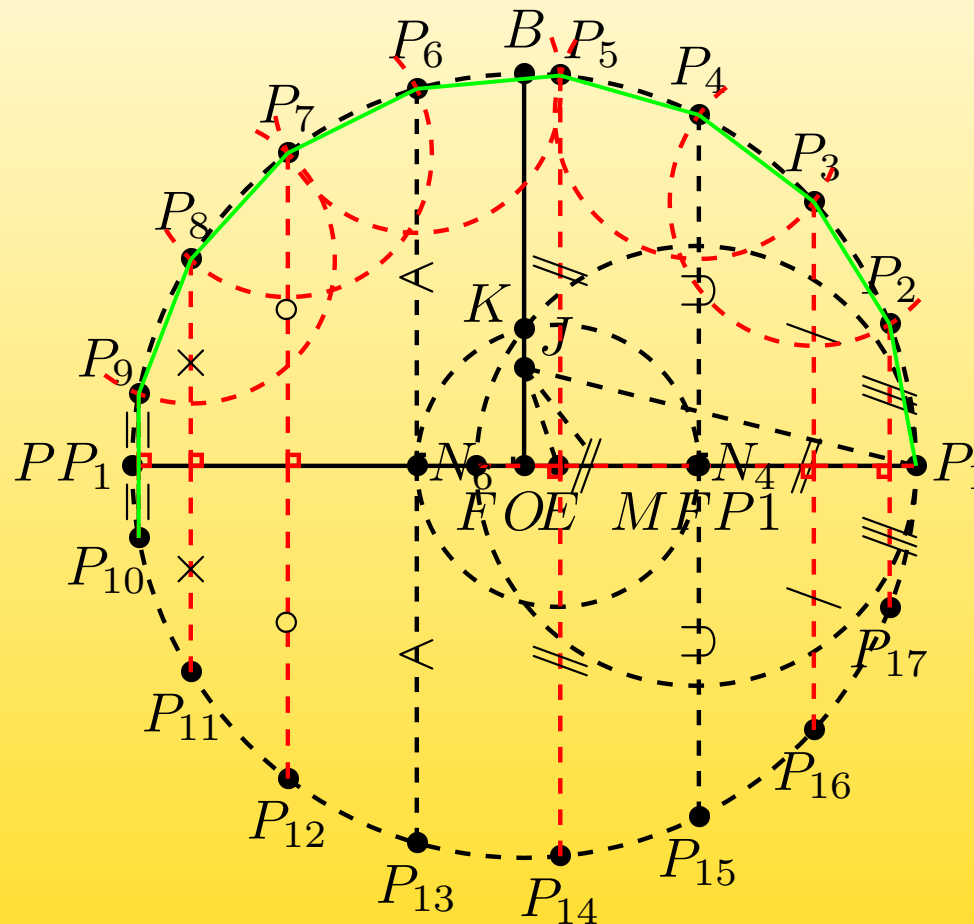


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

40: Side number 10 of the polygon

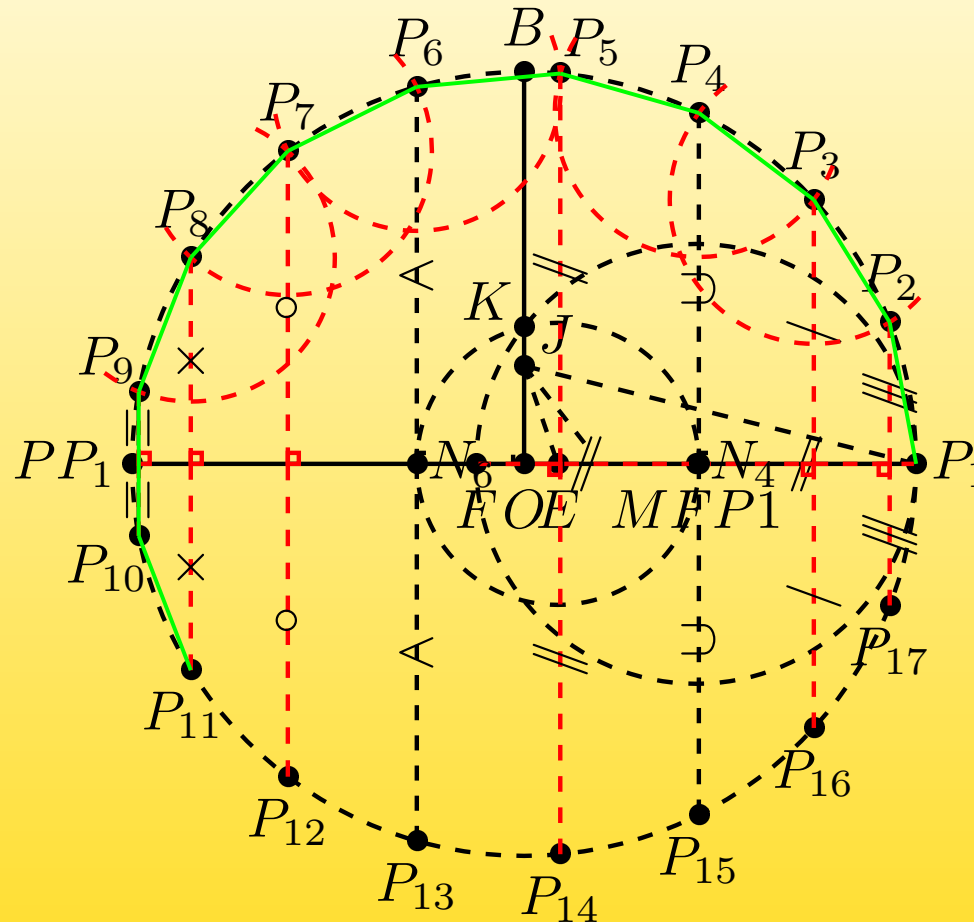


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

41: Side number 11 of the polygon

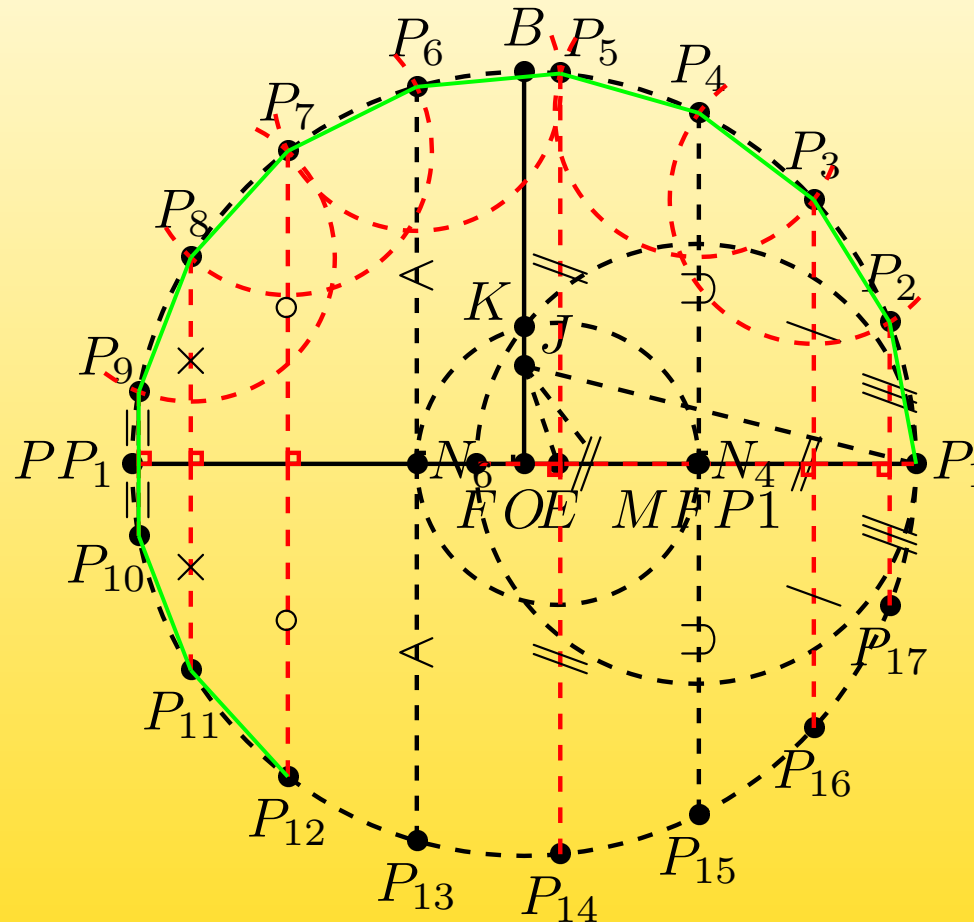


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

42: Side number 12 of the polygon

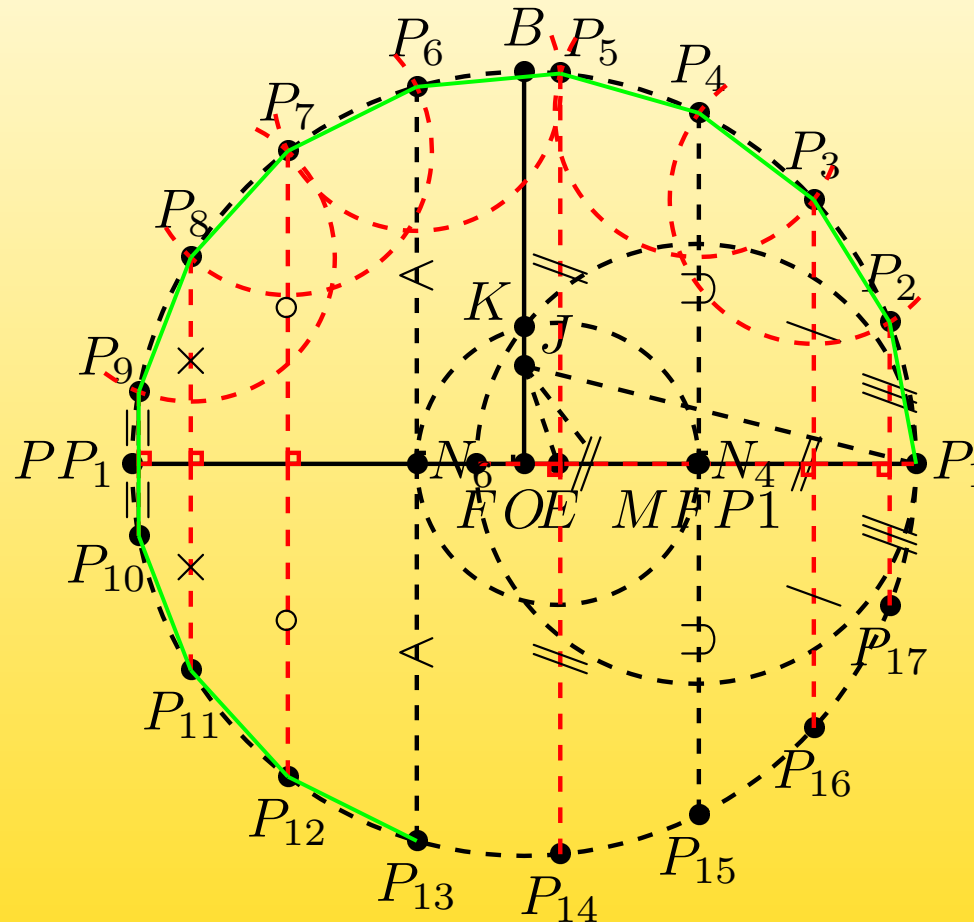


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

43: Side number 13 of the polygon

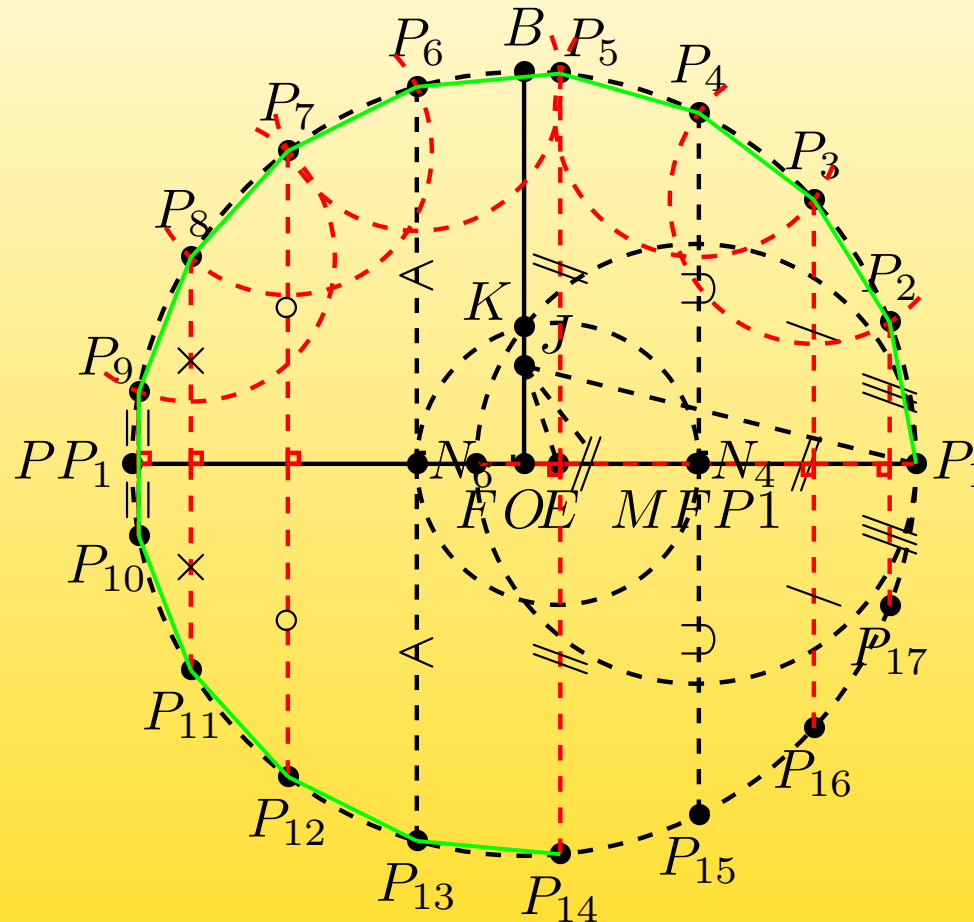


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

44: Side number 14 of the polygon

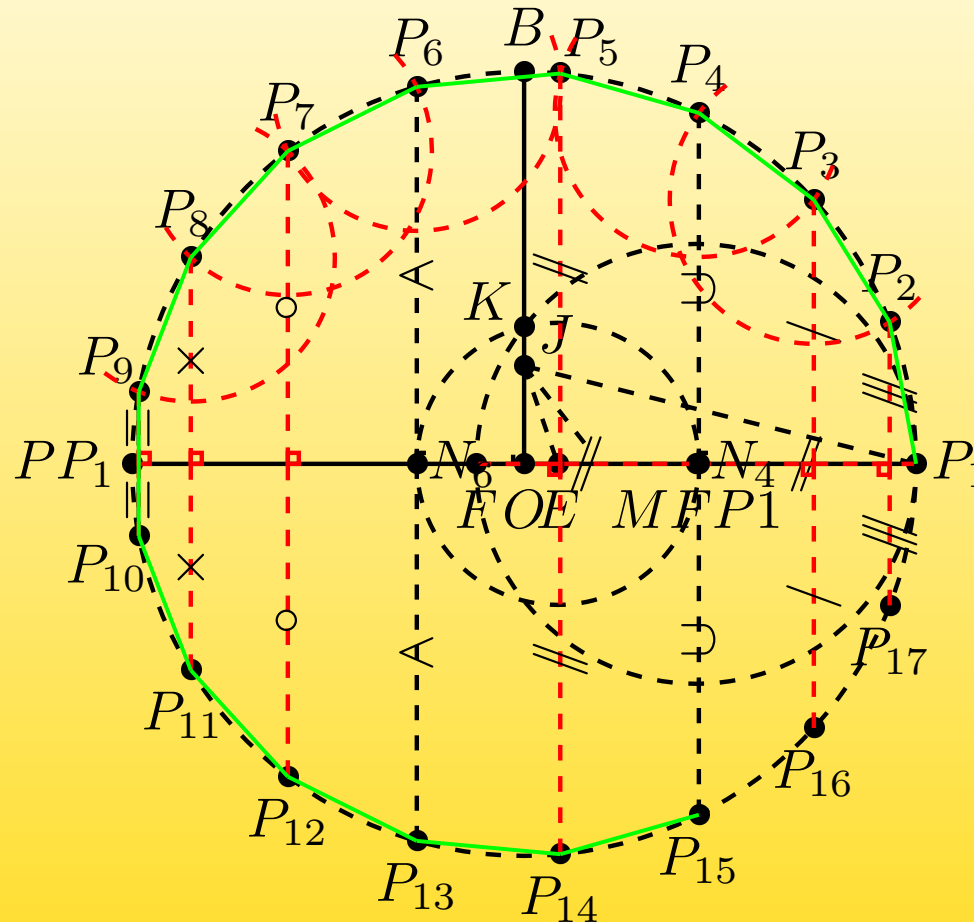


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

45: Side number 15 of the polygon

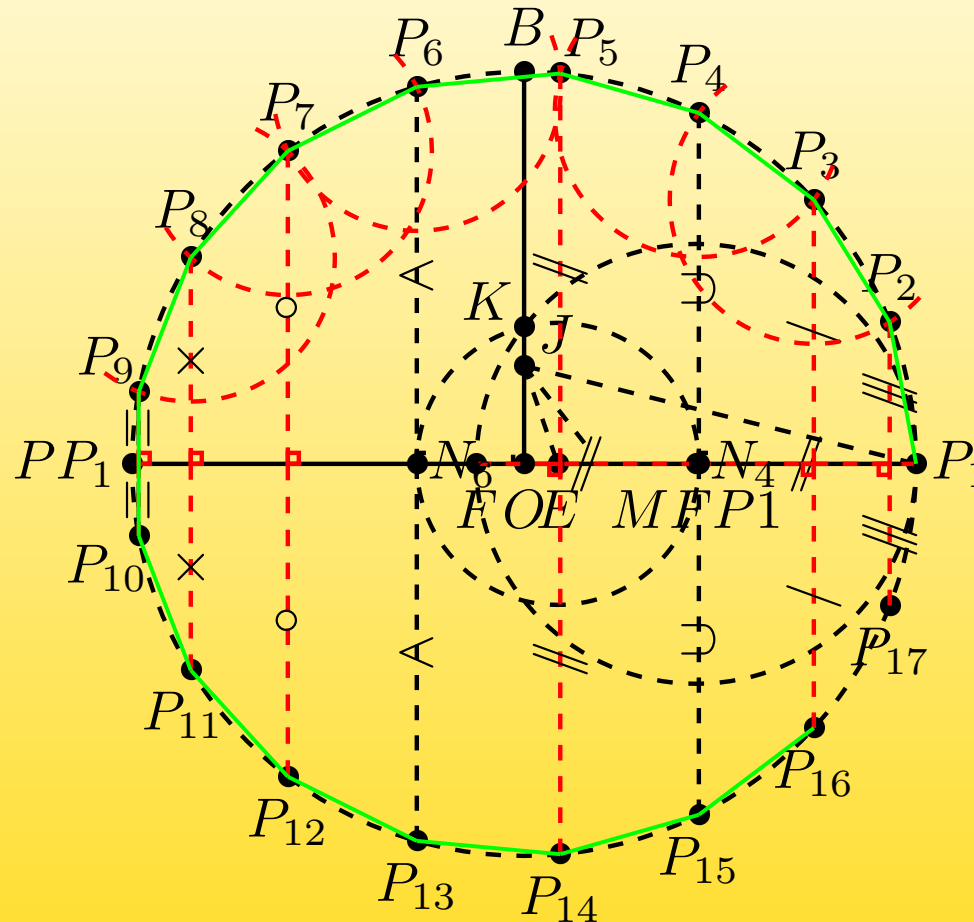


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation



## 11 – Building of a regular polygon of seventeen sides

46: Side number 16 of the polygon

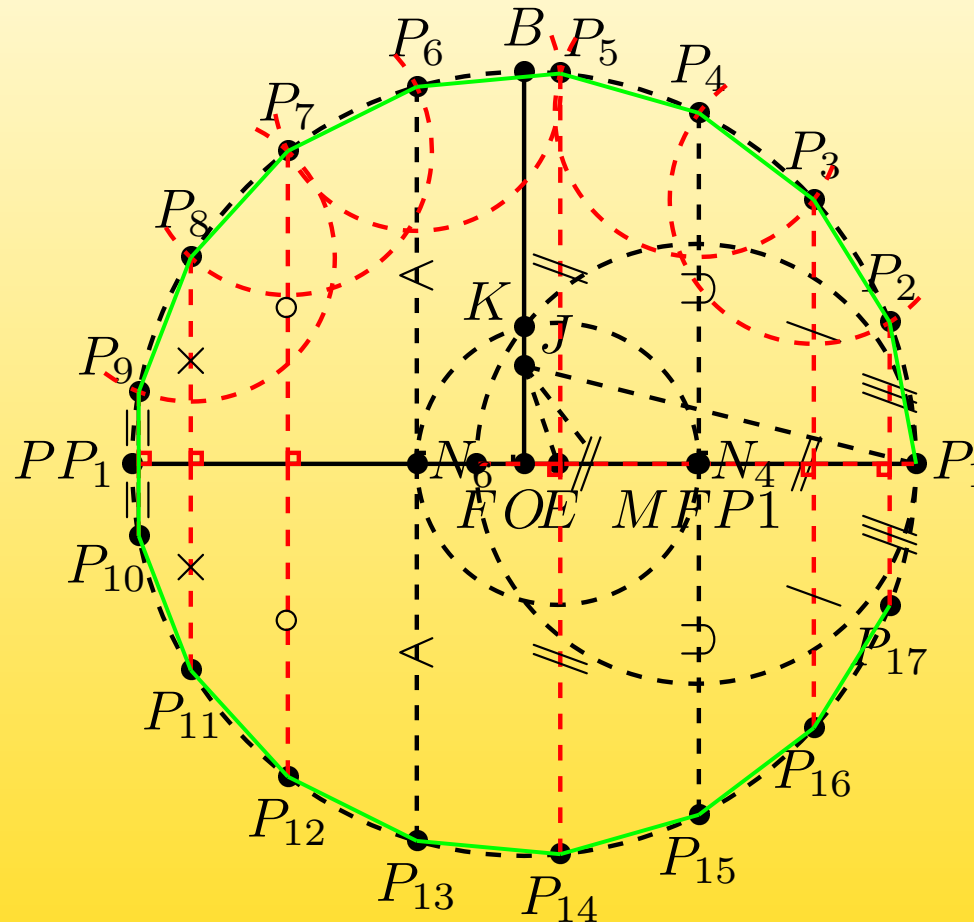


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 11 – Building of a regular polygon of seventeen sides

47: Side number 17 of the polygon

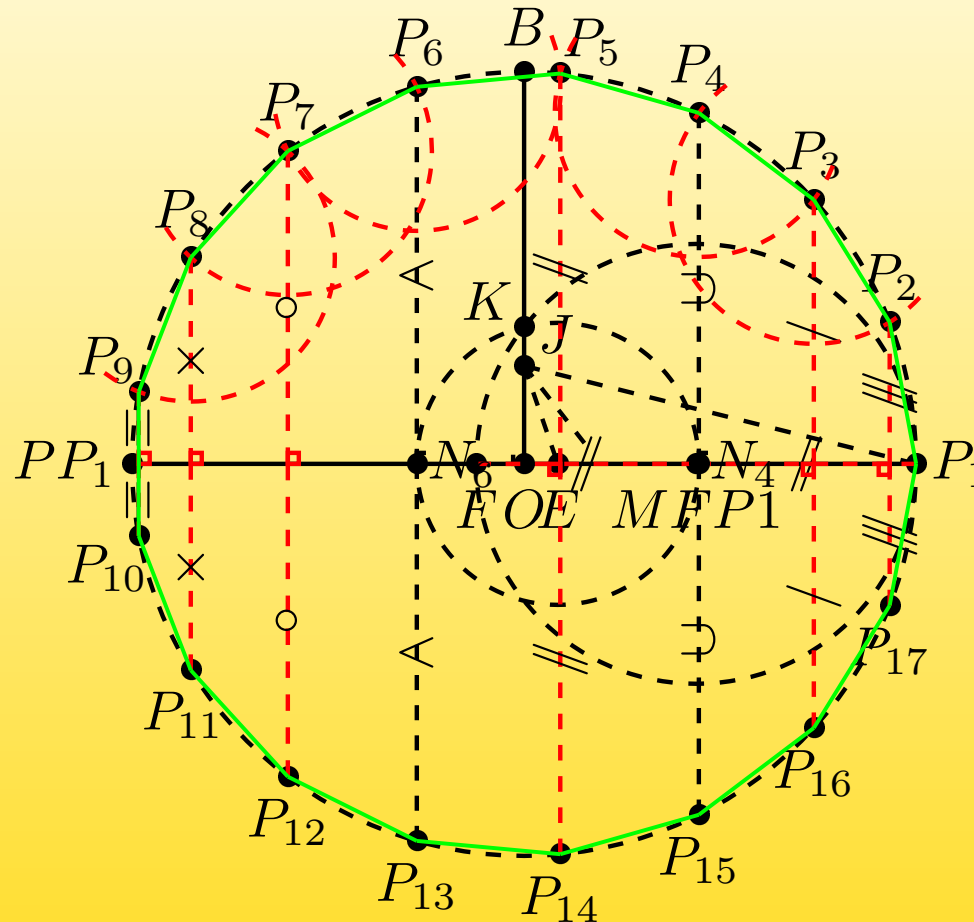


Figure 6: Building of a regular polygon of seventeen sides, according to the method introduced by Carl Friedrich GAUSS.

This code is from Dominique RODRIGUEZ, part of the examples of his 'pst-eucl' PSTricks package for Euclidian geometry.

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

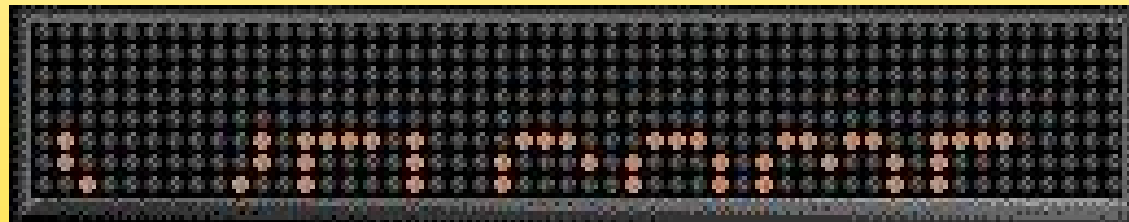


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

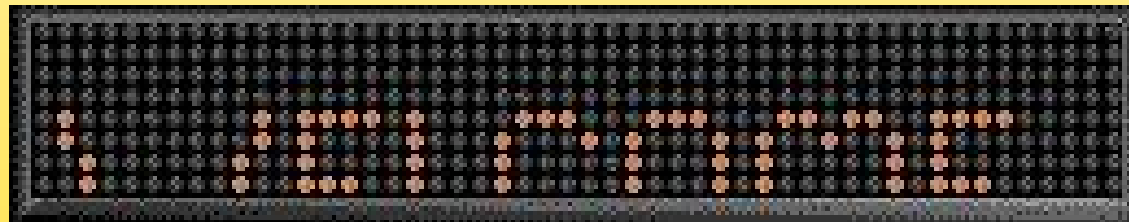


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

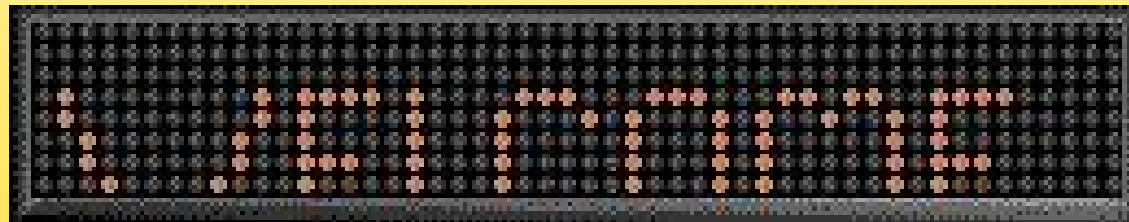


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

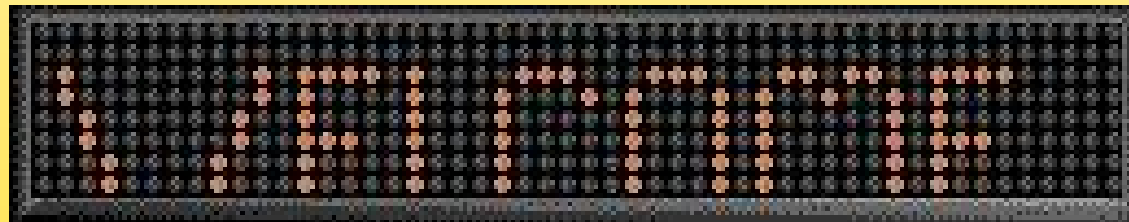


Figure 7: External files inclusion

End of animation



## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

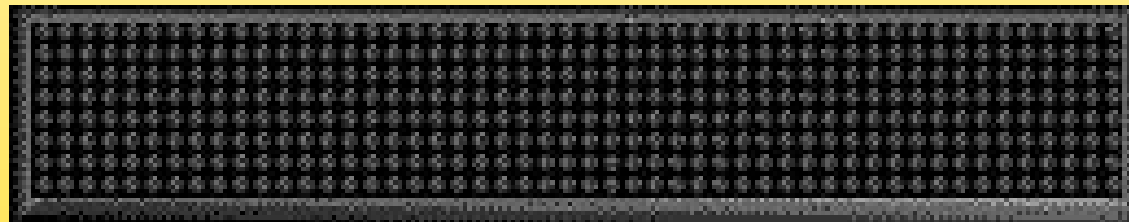


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

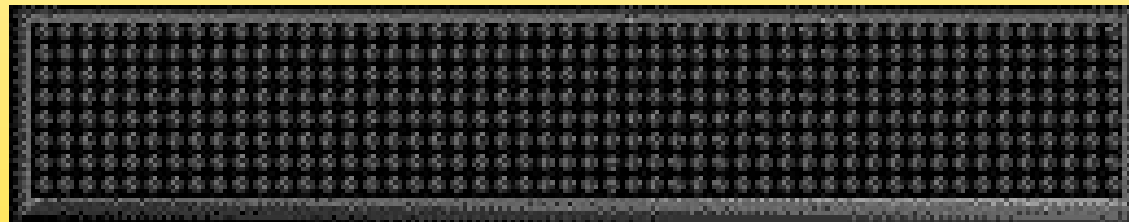


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

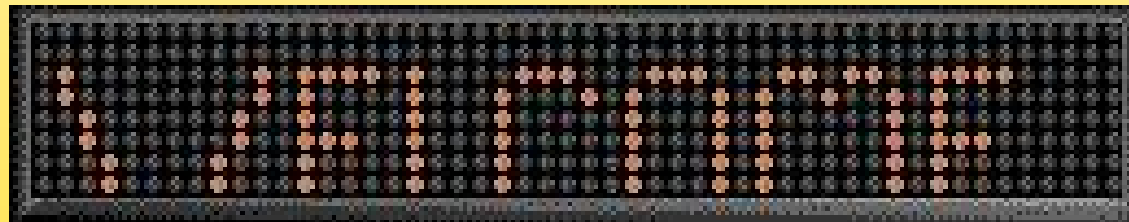


Figure 7: External files inclusion

End of animation



## 12 – External files inclusion

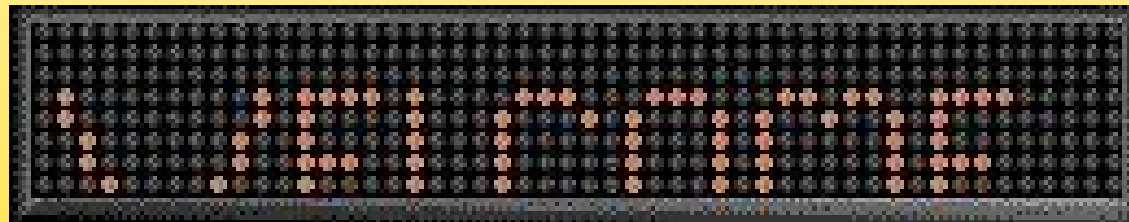


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

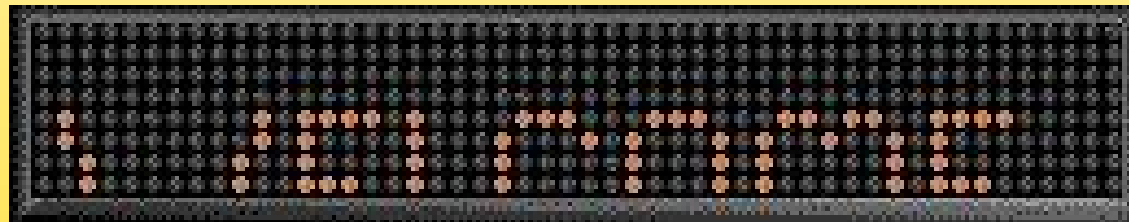


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

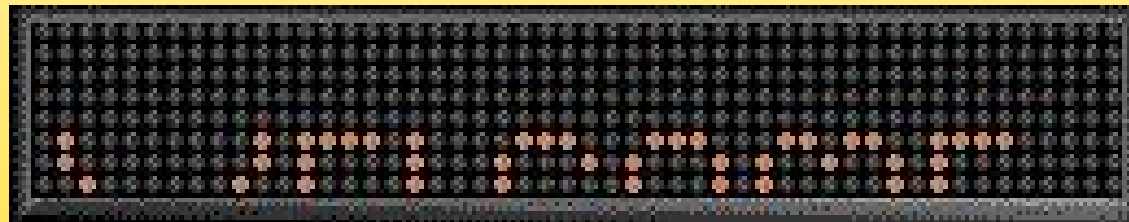


Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion



Figure 7: External files inclusion

End of animation

## 12 – External files inclusion

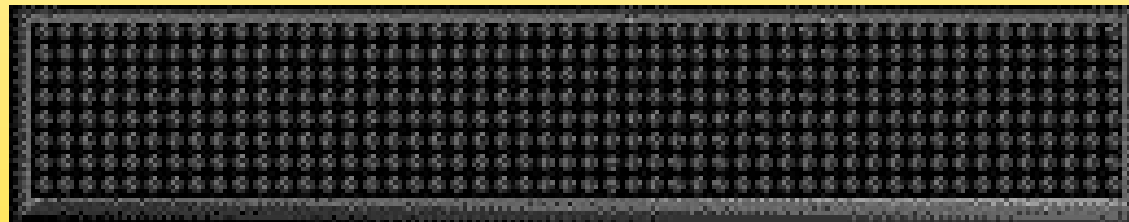


Figure 7: External files inclusion

End of animation